FII Simulation Progress

- Ion oscillation frequencies for uniform and Gaussian charge distributions consistent
- Small amplitudes
 - Near the beam axis, Gaussian is nearly uniform
 - Gaussian frequency equal to uniform frequency (with appropriate charge density)
- Large amplitudes
 - Far from the beam axis, Gaussian and uniform approach line charges
 - Gaussian frequency equal to uniform frequency

Frequency Comparisons (CO⁺)

$$r_{beam}$$
 = 2 mm, l_{bunch} = 1 cm

 $N = 10^{10} \,\mathrm{e}^{-} /\mathrm{bunch}$

 $\sigma_x = \sigma_y = 2 \text{ mm}, \sigma_z = 5 \text{ mm}$

Bunch spacing = 14 ns

| | | Small amplitude (1 µm) | Large amplitude (1 cm) |
|--------------------|---------|------------------------|------------------------|
| Uniform (C++) | Solid | 272,598 Hz | 95,833 Hz |
| | Bunched | 274,696 | 96,090 |
| Uniform (Fortran) | Solid | 272,598 | 95,833 |
| | Bunched | 274,696 | 96,090 |
| Gaussian (Fortran) | Solid | 272,599 | 94,242 |
| | Bunched | 274,686 | 94,501 |

CO⁺ Oscillation Frequency vs. Amplitude

