

# Recent CLEO-c Results on $D$ and $D_S$ Mesons

Run: 202742  
Event: 98595

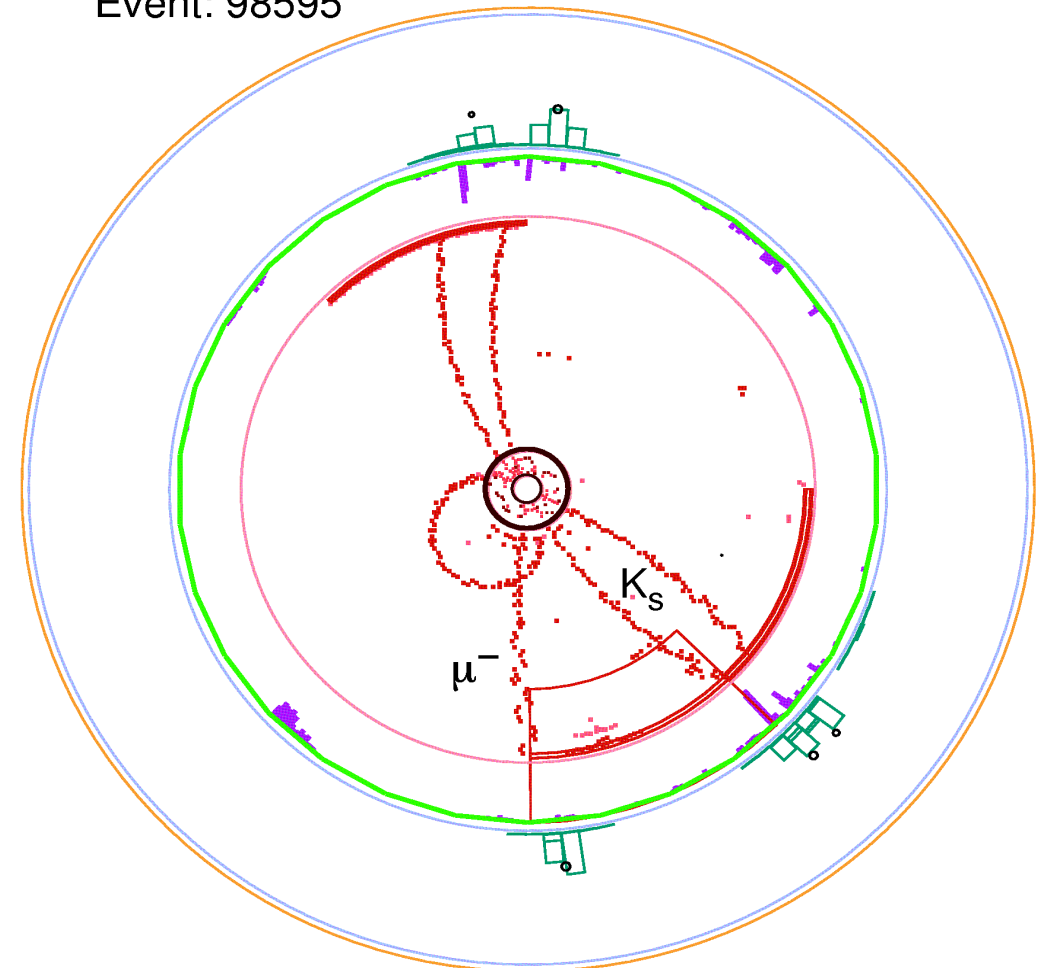
1630804-076

Anders Ryd  
Cornell University

LBL, Oct. 3, 2006

## Outline:

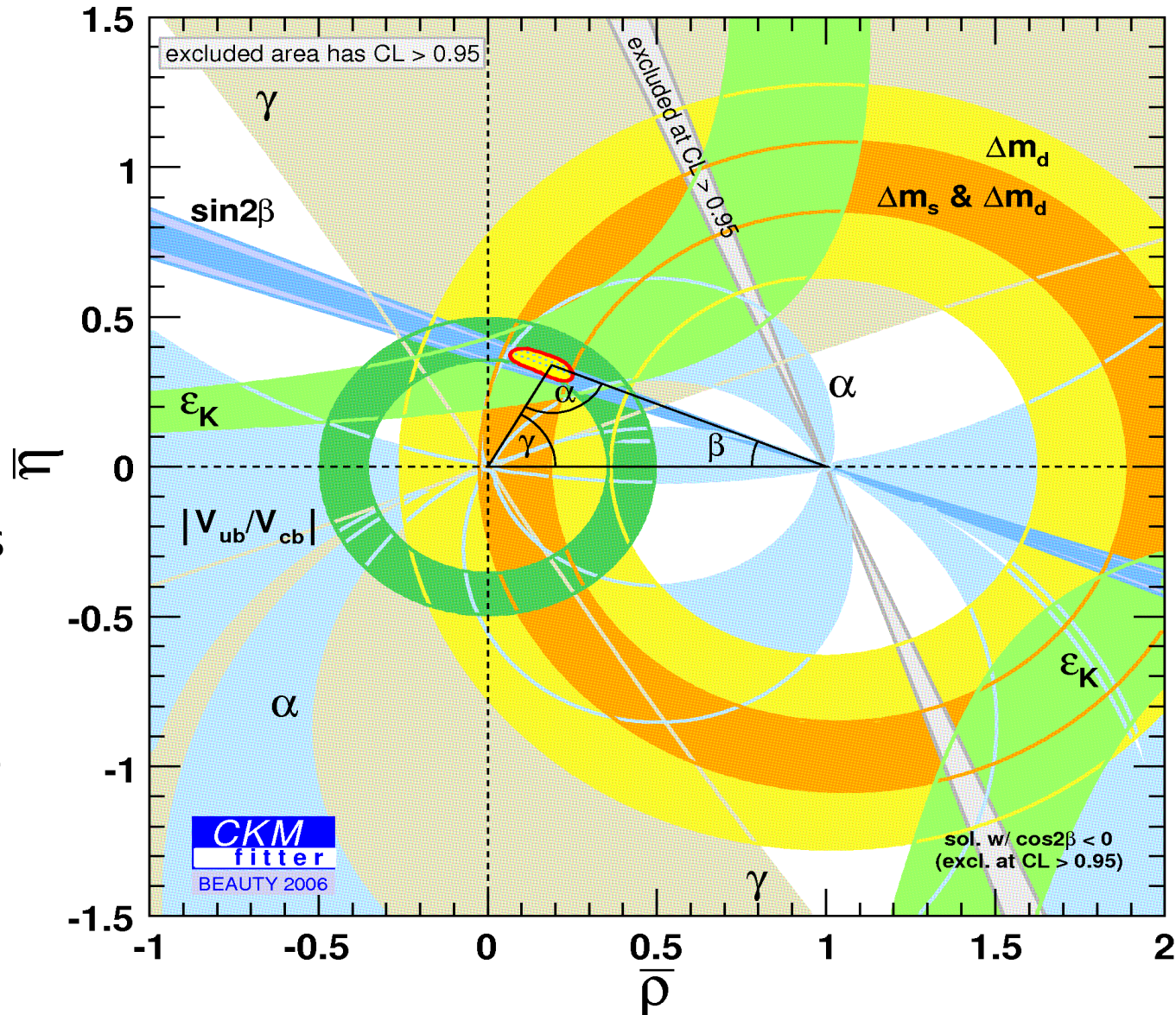
- The CLEO-c program
- Physics at the  $\psi(3770)$
- $D_S$  scan
- Hadronic  $D$  and  $D_S$  decays
- Leptonic  $D$  and  $D_S$  decays
- Semileptonic  $D$  decays



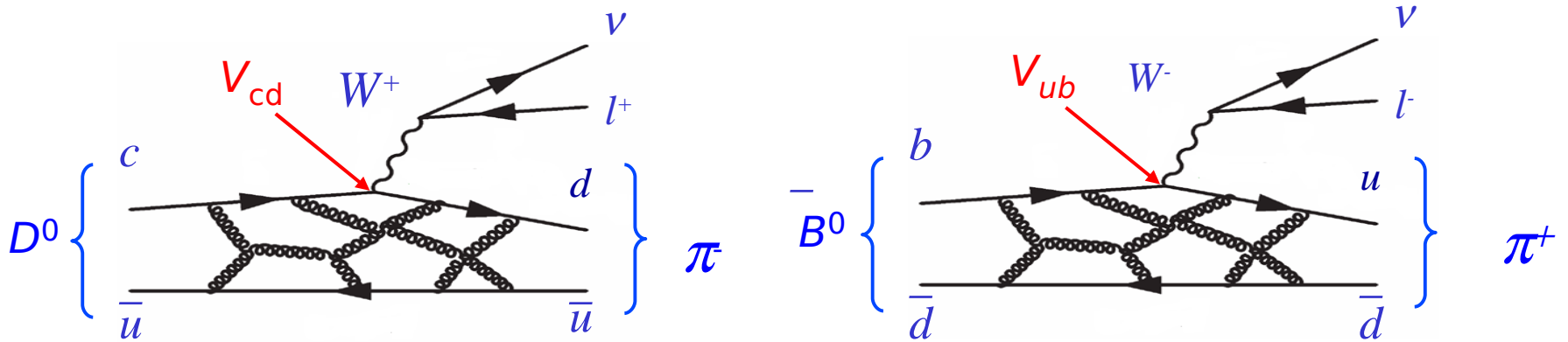
$K_S \pi^- \pi^+ \pi^+$  Tag

# Physics Motivation

- The CLEO-c program impacts many of the CKM parameters
- In particular, leptonic  $D$  and  $D_s$  decays allow measurements of the decay constants
- This will help the determination of  $V_{td}$
- Semileptonic  $D$  decays will check form factor calculations and improve  $V_{ub}$
- Hadronic  $D$  decays are important for normalization of  $B$  decays

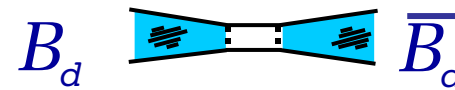


# Testing Theories of Strong Interactions

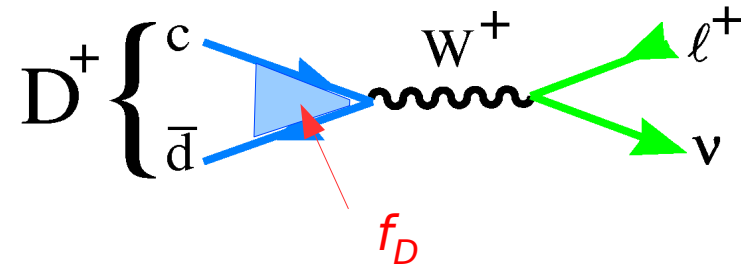


- Measure form factors in  $D \rightarrow \pi l \nu$  and validate theoretical calculations
  - Can then use this to extract  $|V_{ub}|$  from  $B \rightarrow \pi l \nu$

- $B$  mixing is well measured
  - $\Delta m_d = (0.502 \pm 0.007) \times 10^{-12} \text{ s}$
- But  $|V_{td}|$  from  $\Delta m_d$  has large uncertainties from  $f_B$
- CLEO-c can measure  $f_D$



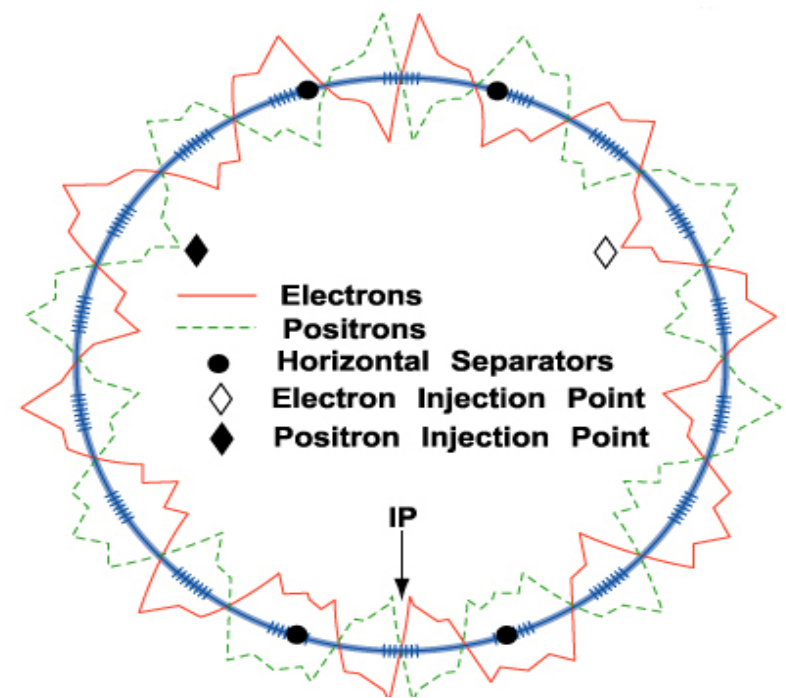
$$\Delta m_d = \frac{G_F^2}{6} M_B M_t^2 |V_{td} V_{tb}^*|^2 \eta_B S_0(x_t) f_B^2 B_B$$



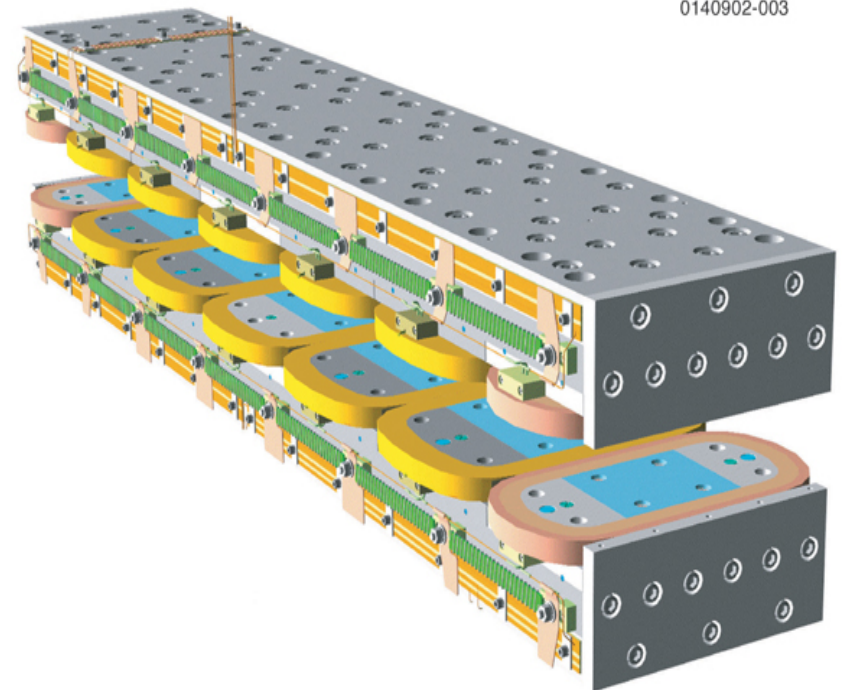


# CESR-c

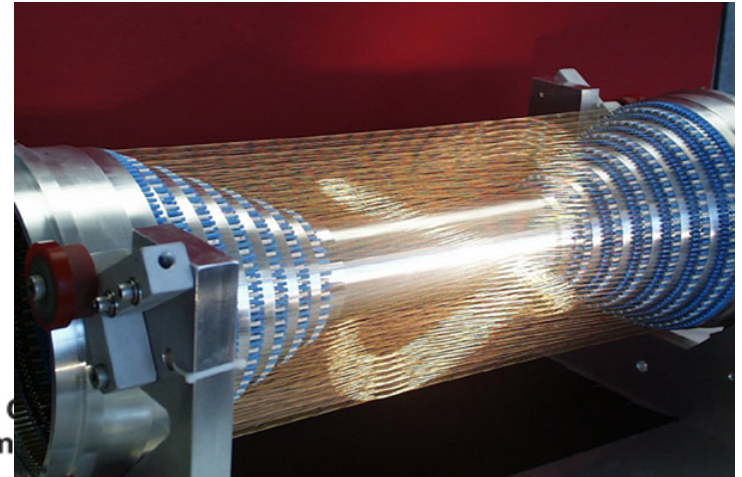
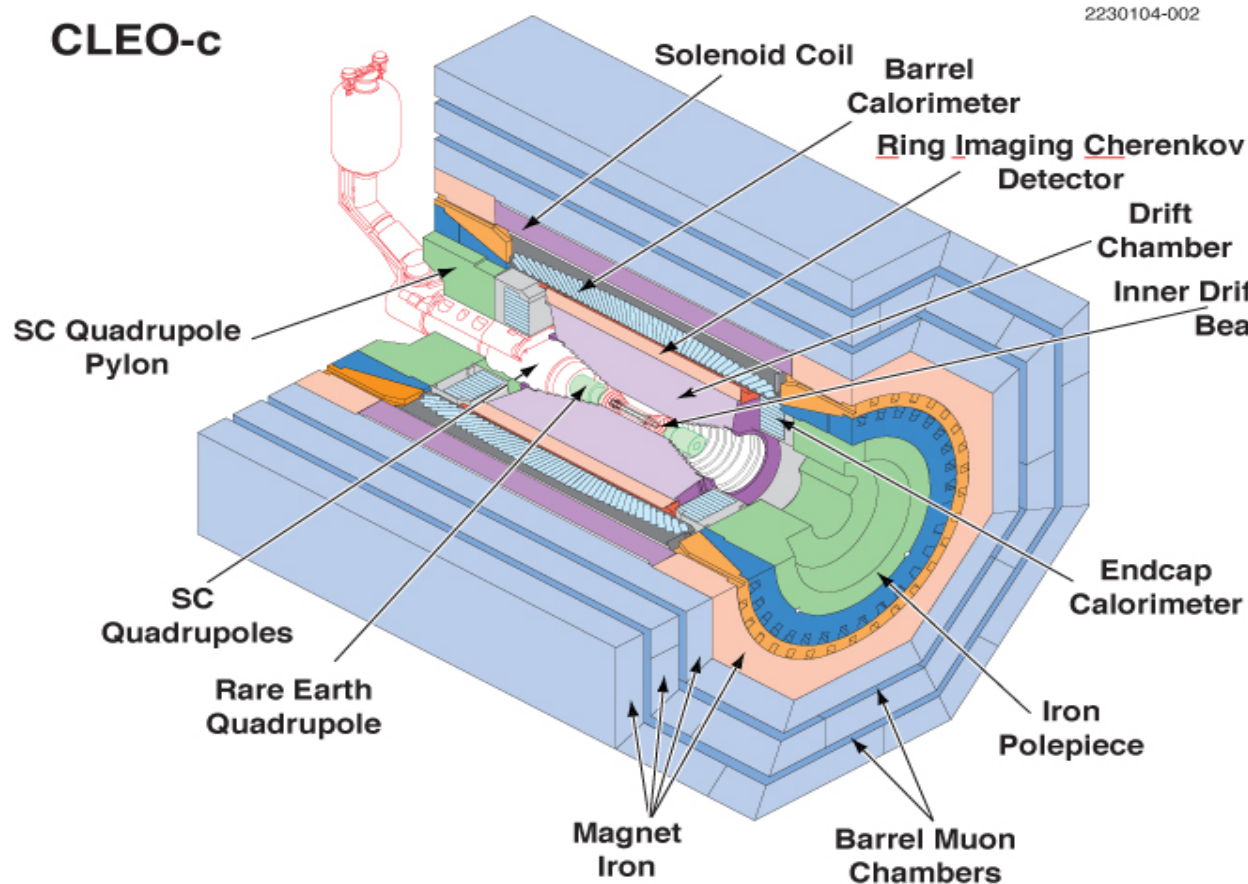
- CESR was upgraded with wiggler magnets to increase damping at lower energies
- These super conducting magnets have worked very well
- However, the currents that can be stored are lower than planned
  - Luminosity about  $\frac{1}{4}$  of design
- Compensating solenoids were installed last winter
  - The compensations with the skew quads used at 5GeV does not work well at lower energy



0140902-003



# CLEO-c Experiment

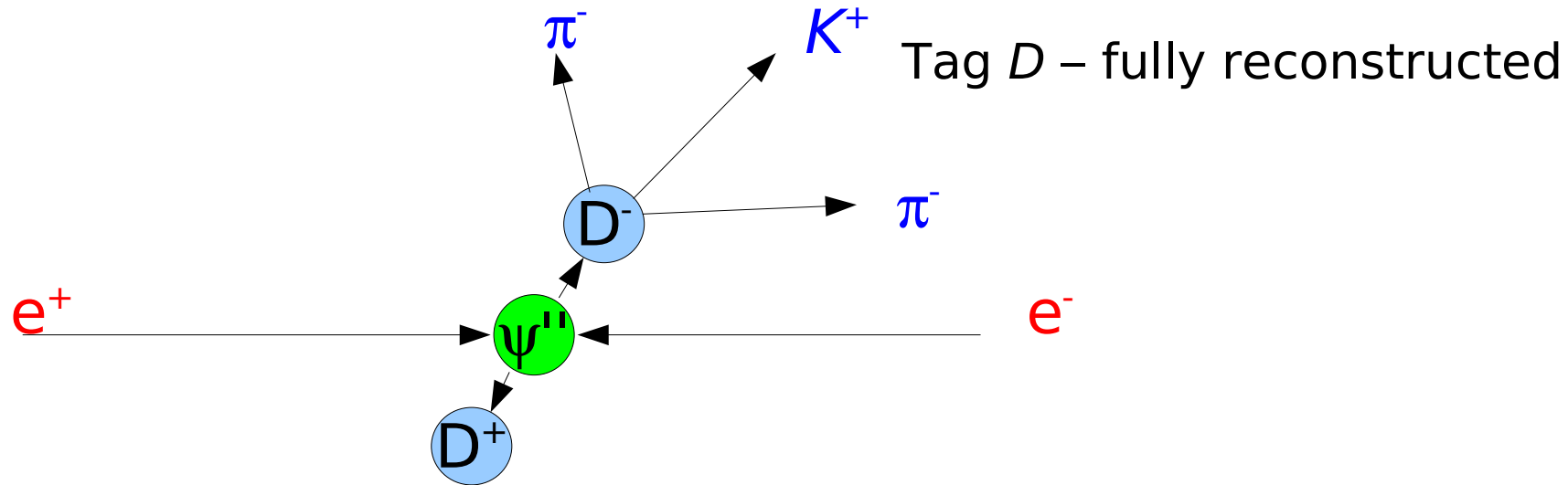


- ◆ New inner drift chamber
- ◆ Tracking in 1.0 T field
  - ◆  $\sigma_p/p \approx 0.6\%$  at 1 GeV
- ◆ Excellent E-M calorimeter
  - ◆  $\sigma_E/E \approx 2\%$  at 1 GeV
- ◆ Hadron PID from RICH
  - ◆ Very good below 1 GeV

# CLEO-c Data Samples and Plans

- With a better understanding of the performance of CESR-c and looking at the physics case we are now looking at a somewhat modified run plan
    - $\sim 750 \text{ pb}^{-1}$  at  $\psi(3770)$
    - $\sim 750 \text{ pb}^{-1}$  at  $D_s D_s$  threshold
    - $\sim 5\%$  of running time at  $\psi(2S)$ , 30M events
  - Solid motivation for  $J/\psi$  running was hard to find. The  $f_j(2220)$  no longer there. Studying this was an important goal for the  $J/\psi$  program
  - We have done a scan in the  $D_s$  threshold region to understand where to run and measure the cross-section
  - Will continue running until March 31, 2008
- Recorded:  
281 pb<sup>-1</sup>  
330 pb<sup>-1</sup>  
27M events

# Physics at the $\psi(3770)$



- At threshold produce only  $D^+D^-$  and  $D^0\bar{D}^0$ 
  - No additional pions.
- By reconstructing one  $D$  meson we know that we had another  $D$  produced with opposite momentum in the  $\psi(3770)$  frame.
- This tag technique is used in many CLEO-c analysis and was pioneered by MARK III.

# Quantum Correlations

The two  $D^0$  mesons are correlated:  $C=-1$

PRD 73 034024 (2006)  
Asner and Sun

	$f$	$l^+$	$CP+$	$CP-$
$f$	$R_M(1+r^2(2-z^2))$			
$f^-$	$1+r^2(2-z^2)$			
$l^-$	1	1		
$CP+$	$1+rz$	1	0	
$CP-$	$1-rz$	1	2	0
$X$	$1+rzy$	1	$1-y$	$1+y$

Correction to BR  
as compared to  
incoherent decay

$$x = \frac{\Delta m}{\Gamma}$$

$$y = \frac{\Delta \Gamma}{2\Gamma}$$

$$R_M = (x^2 + y^2)/2$$

$$r e^{i\delta} = \frac{\langle \bar{D}^0 | K^- \pi^+ \rangle}{\langle D^0 | K^- \pi^+ \rangle}$$

$$z = 2 \cos \delta$$

- For  $CP$  vs  $CP$  eigenstates the correlation is a large effect
- E.g the decay  $D^0 \rightarrow K_S \pi^0$  where the other  $D$  decays generically (single tag)

$$N(D^0 \rightarrow K_S^0 \pi^0) = 2 N_{D^0 \bar{D}^0} B(D^0 \rightarrow K_S^0 \pi^0) (1+y)$$

- Where the other  $D$  is a flavor tag  $D \rightarrow f$

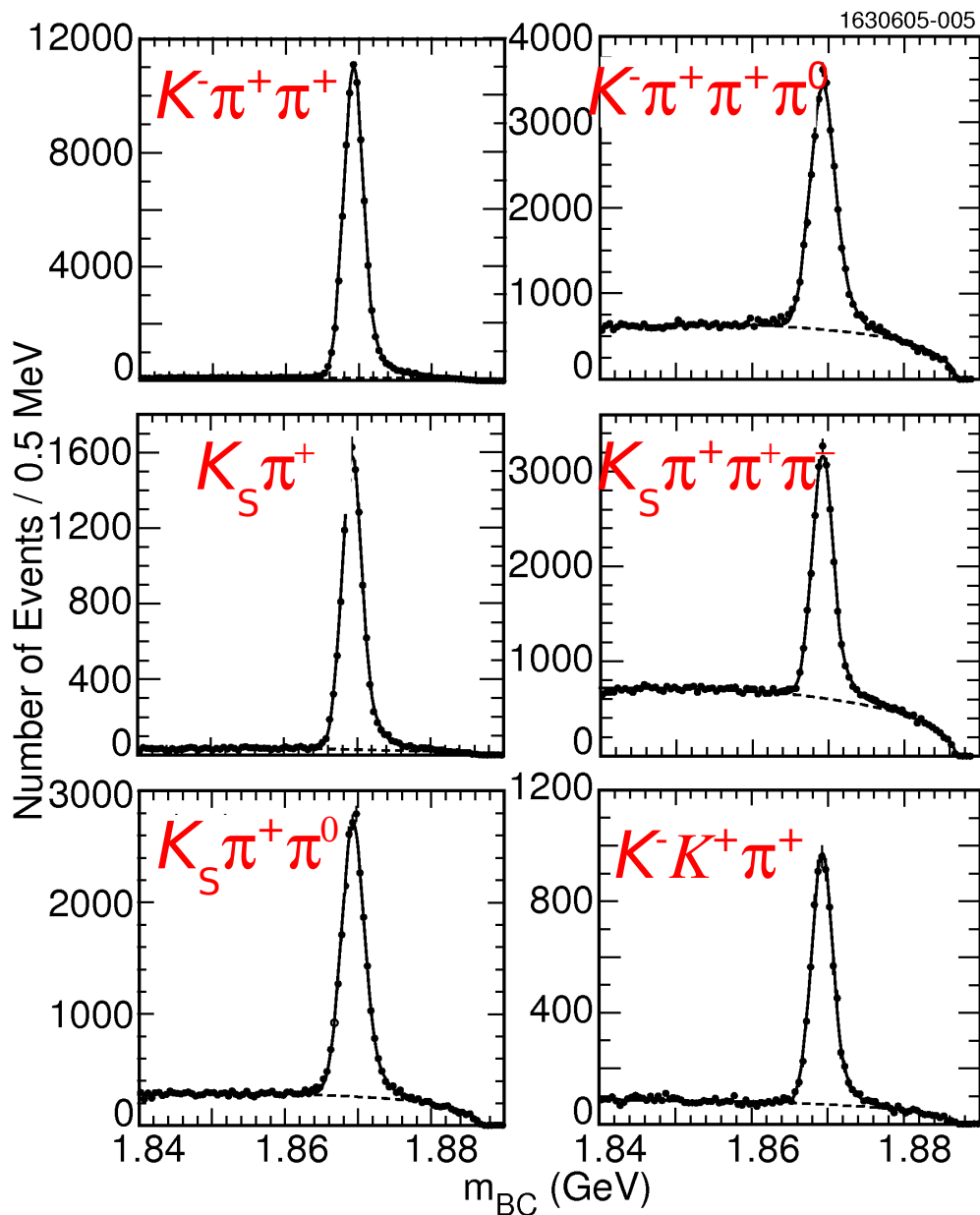
$$N(D^0 \rightarrow K_S^0 \pi^0) = N_{D^0 \bar{D}^0} B(D^0 \rightarrow K_S^0 \pi^0) (1 - 2r_f \cos \delta_f)$$

Allow us to measure  
phase  $\delta_f$ , in 280 pb<sup>-1</sup>

$$\sigma_{\cos \delta_{K\pi}} = \pm 0.64$$



# CLEO-c $D$ -tag Reconstruction



- From  $D \rightarrow \mu\nu$  analysis
- 281 pb<sup>-1</sup>
- Six tag modes used
- ~160,000 reconstructed  $D^\pm$
- ~300,000 reconstructed  $D^0$
- Cut on  $E_D - E_{\text{beam}}$

Mode	Signal	Background
$K^+ \pi^- \pi^-$	$77387 \pm 281$	1868
$K^+ \pi^- \pi^- \pi^0$	$24850 \pm 214$	12825
$K_S \pi^-$	$11162 \pm 136$	514
$K_S \pi^- \pi^- \pi^+$	$18176 \pm 255$	8976
$K_S \pi^- \pi^0$	$20244 \pm 170$	5223
$K^+ K^- \pi^-$	$6535 \pm 95$	1271
Sum	$158354 \pm 496$	30677

$$M_{BC} = \sqrt{E_{\text{beam}}^2 - |p(D)|^2}$$

# Initial State Radiation

- We run at  $E_{cm} = 3.77$  GeV to produce the  $\psi(3770)$ 
  - The spread in  $E_{cm}$  is about 2 MeV
  - The width of the  $\psi(3770)$  is about 25 MeV
- However, the beam particles can radiate a photon and produce the  $\psi(3770)$  at a lower energy.
  - In fact in every interaction many photons are emitted, but at such a low energy that we can not detect them. The distribution of energy radiated by (soft) photons is given by:

$$f(E_y) \propto E_y^{\beta-1} \quad \beta = \frac{2\alpha}{\pi} \left[ 2 \ln \frac{E_{cm}}{m_e} - 1 \right] \approx 0.07$$

- Many analyses use a first principle lineshape for the  $m_{BC}$  fit

# ISR in Data vs. MC

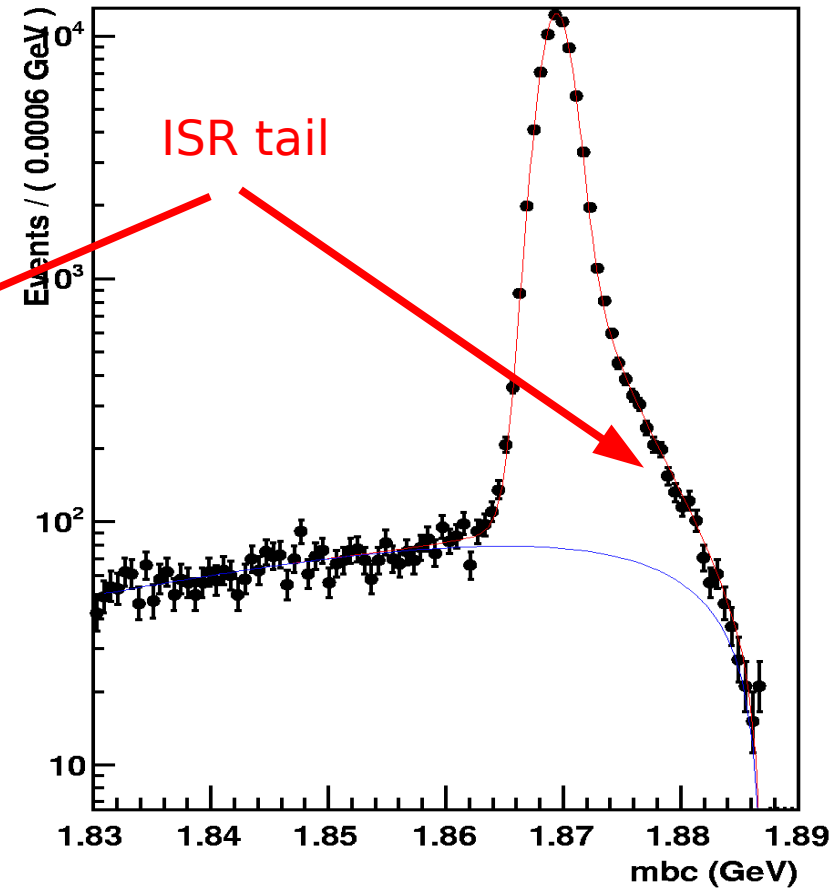
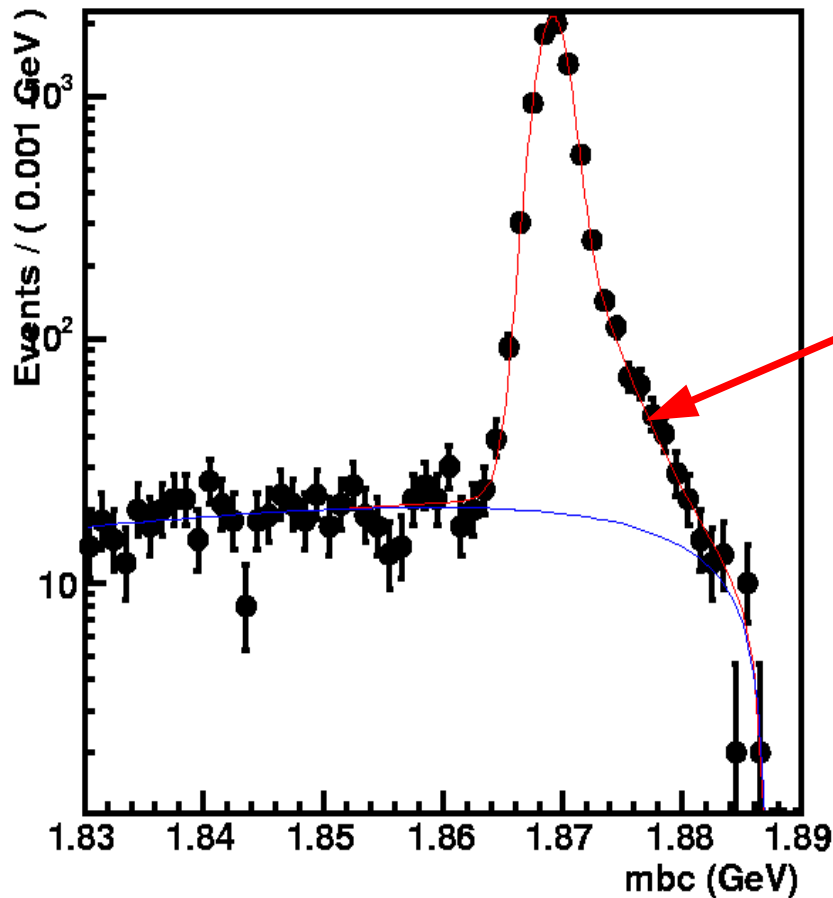


D<sup>+</sup> → K<sup>-</sup> π<sup>+</sup> π<sup>+</sup>

DATA

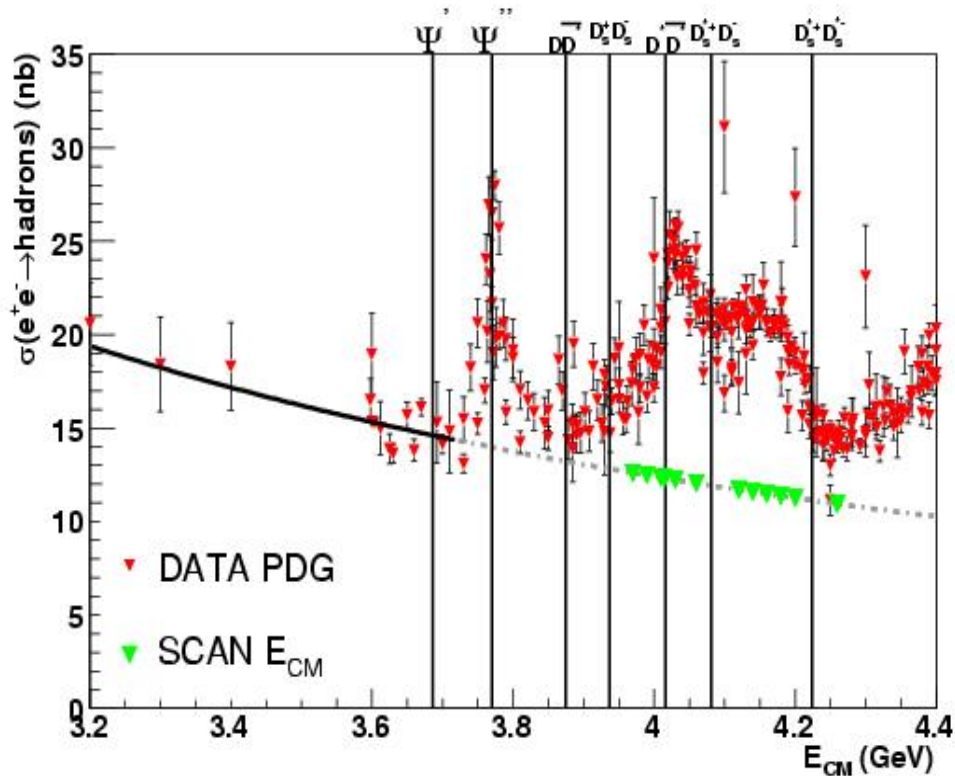
D<sup>+</sup> → K<sup>-</sup> π<sup>+</sup> π<sup>+</sup>

Monte Carlo



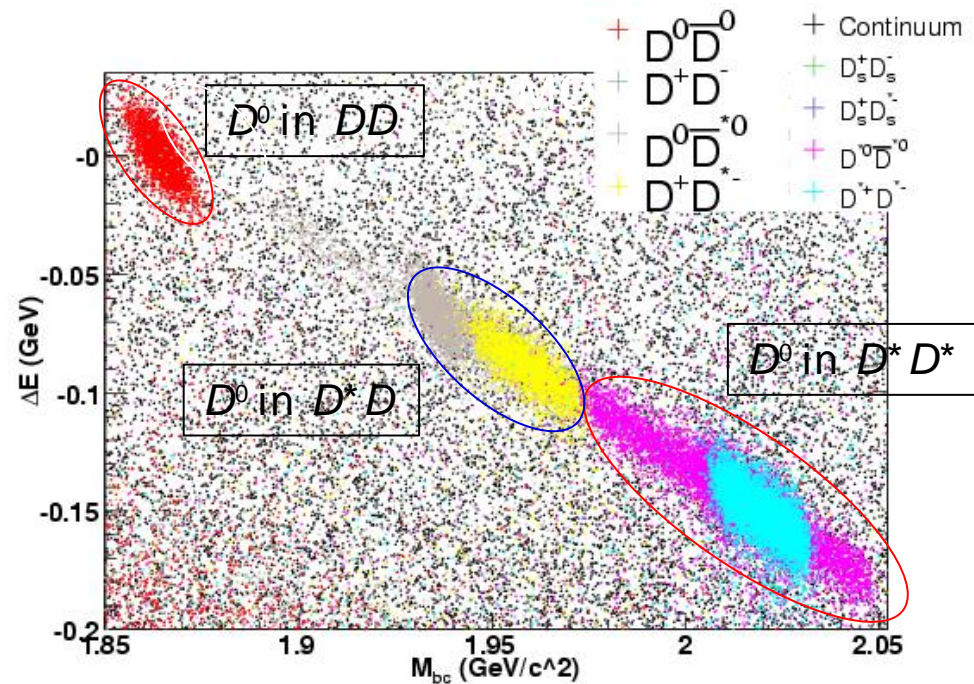
$$M_{BC} = \sqrt{E_{\text{beam}}^2 - |p(D)|^2}$$

# $D_S$ Scan



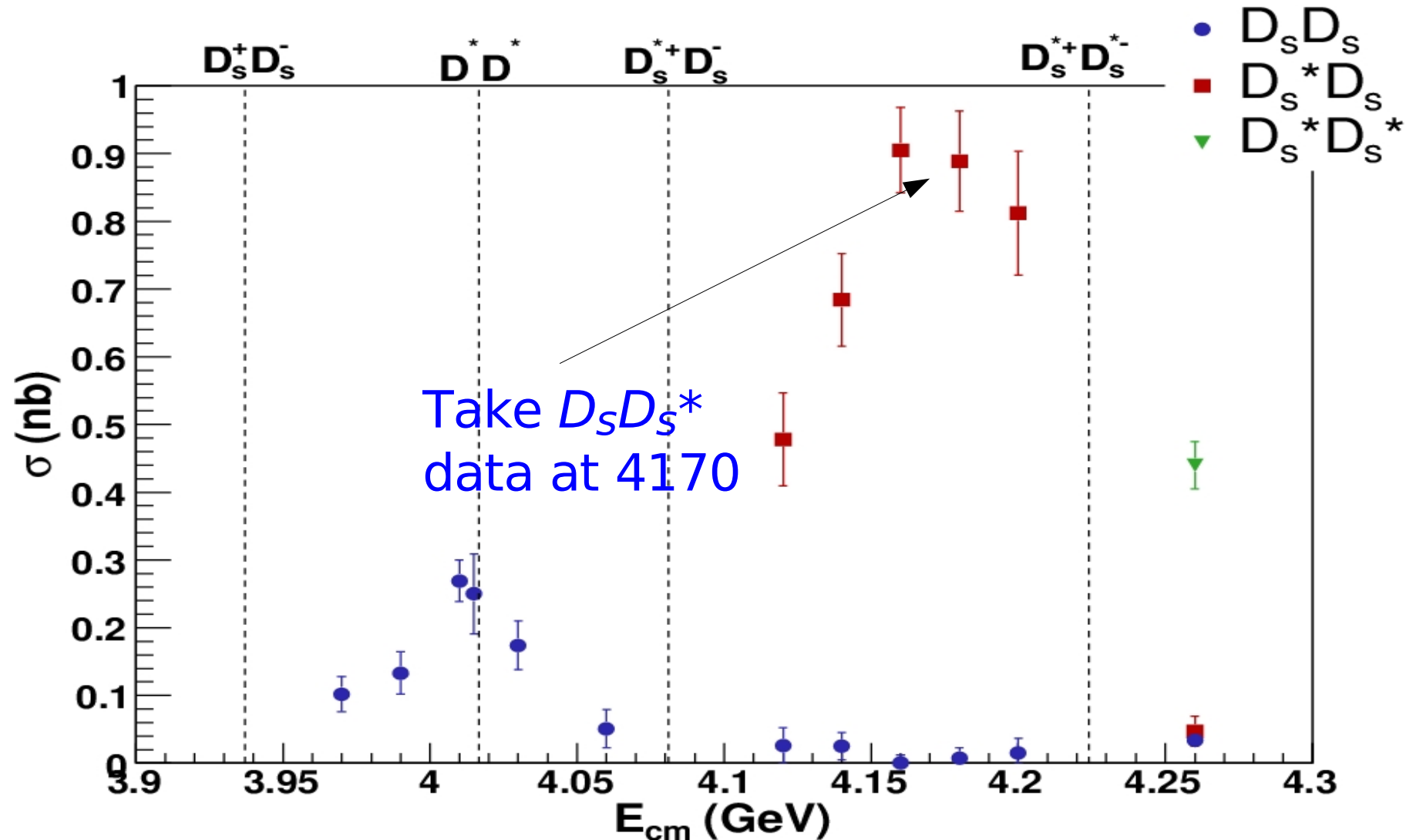
- Took 12 scan points in the energy from 3.97 to 4.26 GeV

- Identify the final states  $D^0 D^0$ ,  $D^+ D^-$ ,  $D^0 D^{*0}$ ,  $D^+ D^{*-}$ ,  $D^{*0} D^{*0}$ ,  $D^{*+} D^{*-}$ ,  $D_S D_S$ ,  $D_S D_S^*$ , and  $D_S^* D_S^*$  based on the reconstructed momentum of  $D^0$ ,  $D^+$  and  $D_S$  mesons



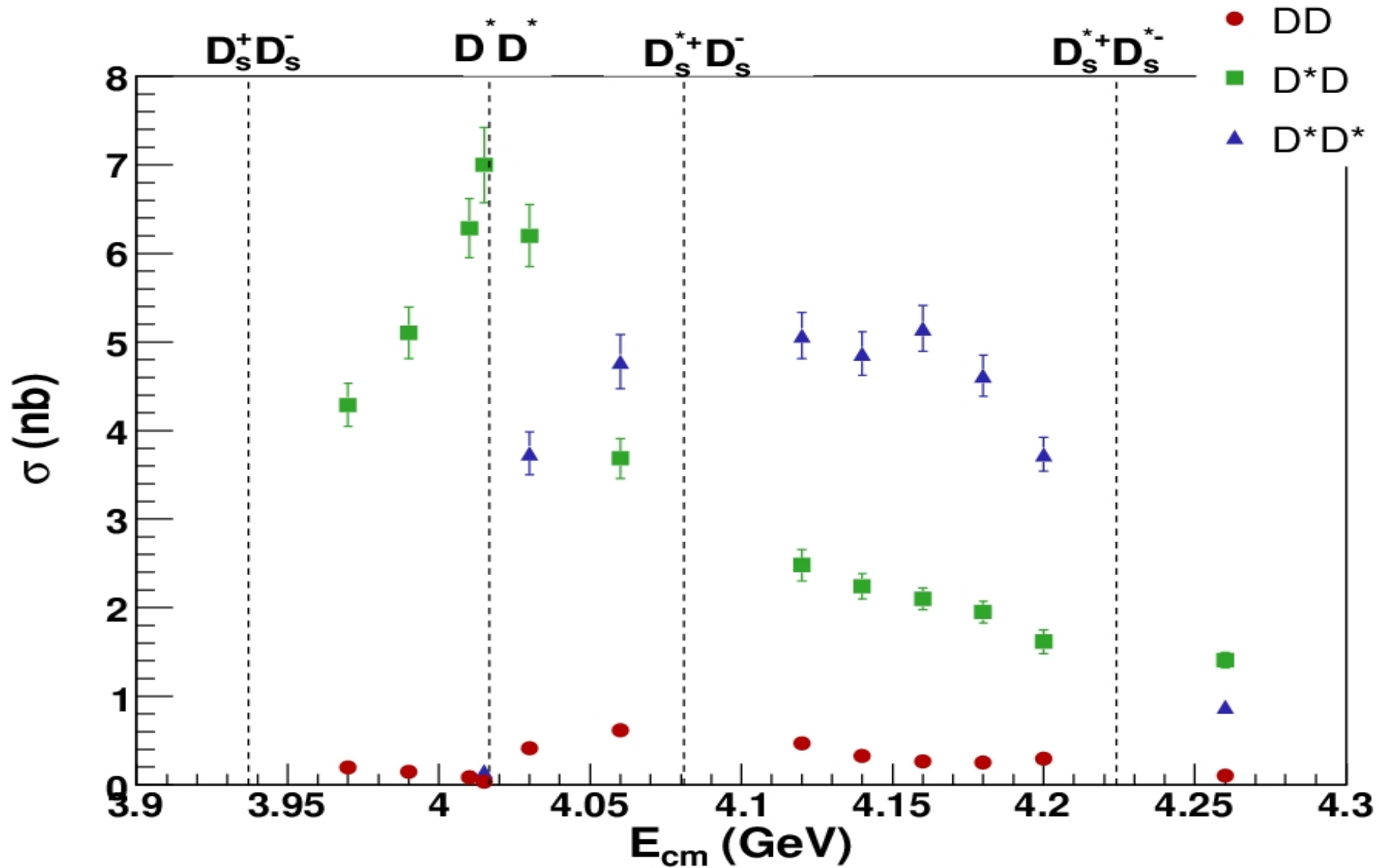
$$M_{BC} = \sqrt{E_{\text{beam}}^2 - |p(D)|^2}$$

# Scan Results: $D_S D_S$ , $D_S D_S^*$ , and $D_S^* D_S^*$





# Scan Results: $DD$ , $D^*D$ , and $D^*D^*$



# Absolute Hadronic $D$ Branching Fractions and $\sigma(e^+e^- \rightarrow D\bar{D})$

- The  $\psi(3770)$  decays to pairs of  $D$  mesons – and no other particles

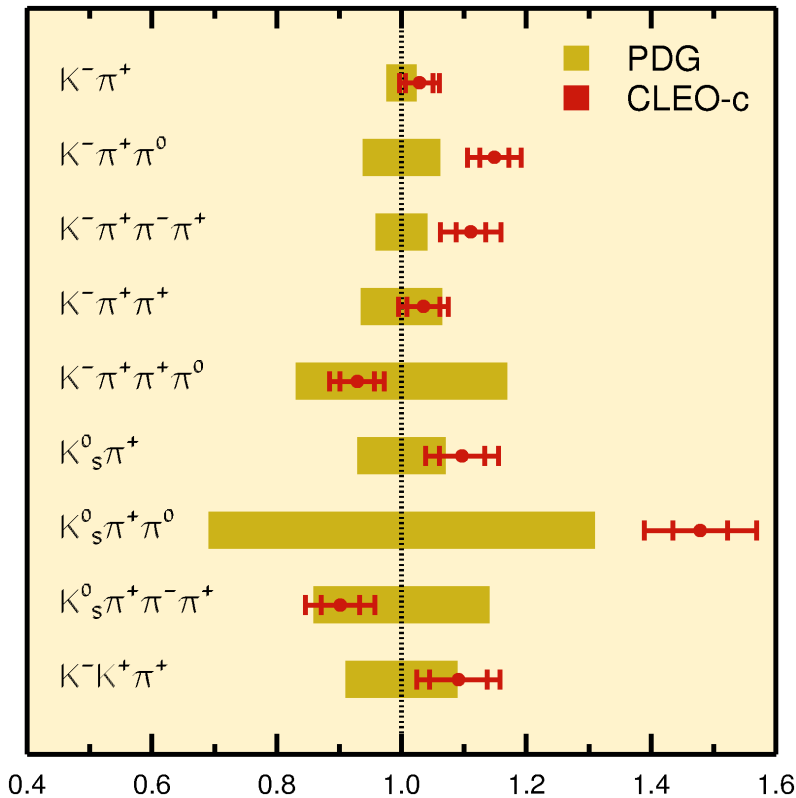
- Use a 'double tag' technique, pioneered by MARK III

$$\begin{aligned}
 N_i &= \epsilon_i B_i N_{D\bar{D}} \\
 \bar{N}_j &= \bar{\epsilon}_j B_j N_{D\bar{D}} \\
 N_{ij} &= \epsilon_{ij} B_i B_j N_{D\bar{D}}
 \end{aligned}
 \quad
 N_{D\bar{D}} = \frac{N_i \bar{N}_j \epsilon_{ij}}{N_{ij} \epsilon_i \bar{\epsilon}_j}
 \quad
 B_i = \frac{N_{ij} \epsilon_j}{N_j \epsilon_{ij}}$$

- Use 3  $D^0$  modes ( $K^-\pi^+$ ,  $K^-\pi^+\pi^0$ , and  $K^-\pi^+\pi^-\pi^+$ ) and 6  $D^+$  modes ( $K^-\pi^+\pi^+$ ,  $K_S^-\pi^+$ ,  $K^-\pi^+\pi^+\pi^0$ ,  $K_S^-\pi^+\pi^-\pi^+$ ,  $K_S^-\pi^+\pi^0$ , and  $K^-\pi^+\pi^+$ )
- Determine separately the  $D$  and  $\bar{D}$  yields
  - This gives 18 single tag yields and 45 ( $=3^2+6^2$ ) double tag yields
- In a combined  $\chi^2$  fit we extract 9 branching fractions and  $D^0\bar{D}^0$  and  $D^+D^-$  yields. The fit includes the systematic errors.
- Many systematics cancel in the  $D\bar{D}$  yield (e.g. tracking eff., PID eff.).

# Results from 56 pb<sup>-1</sup> (PRL 95, 121801)

Parameter	Fitted Value	$\Delta_{\text{FSR}}$
$N_{D^0\bar{D}^0}$	$(2.01 \pm 0.04 \pm 0.02) \times 10^5$	-0.2%
$\mathcal{B}(D^0 \rightarrow K^- \pi^+)$	$(3.91 \pm 0.08 \pm 0.09)\%$	-2.0%
$\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0)$	$(14.9 \pm 0.3 \pm 0.5)\%$	-0.8%
$\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-)$	$(8.3 \pm 0.2 \pm 0.3)\%$	-1.7%
$N_{D^+D^-}$	$(1.56 \pm 0.04 \pm 0.01) \times 10^5$	-0.2%
$\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)$	$(9.5 \pm 0.2 \pm 0.3)\%$	-2.2%
$\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0)$	$(6.0 \pm 0.2 \pm 0.2)\%$	-0.6%
$\mathcal{B}(D^+ \rightarrow K_S^0 \pi^+)$	$(1.55 \pm 0.05 \pm 0.06)\%$	-1.8%
$\mathcal{B}(D^+ \rightarrow K_S^0 \pi^+ \pi^0)$	$(7.2 \pm 0.2 \pm 0.4)\%$	-0.8%
$\mathcal{B}(D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-)$	$(3.2 \pm 0.1 \pm 0.2)\%$	-1.4%
$\mathcal{B}(D^+ \rightarrow K^+ K^- \pi^+)$	$(0.97 \pm 0.04 \pm 0.04)\%$	-0.9%



Our branching fractions are corrected for FSR (so they include  $\gamma$ 's)

Using our measured luminosity of  $55.8 \pm 0.6 \text{ pb}^{-1}$  we obtain:

$$\sigma(e^+ e^- \rightarrow D^0 \bar{D}^0) = (3.60 \pm 0.07 \pm 0.07) \text{ nb} \quad \sigma(e^+ e^- \rightarrow D^+ D^-) = (2.79 \pm 0.07 \pm 0.10) \text{ nb}$$

$$\sigma(e^+ e^- \rightarrow D \bar{D}) = (6.39 \pm 0.10 \pm 0.17) \text{ nb}$$

(PRL 96, 092002)

$$\text{CLEO-c inclusive: } \sigma(e^+ e^- \rightarrow \psi(3770) \rightarrow \text{hadrons}) = (6.38 \pm 0.08^{+0.41}_{-0.30}) \text{ nb}$$

# Single Tag Yields (281 pb<sup>-1</sup>)

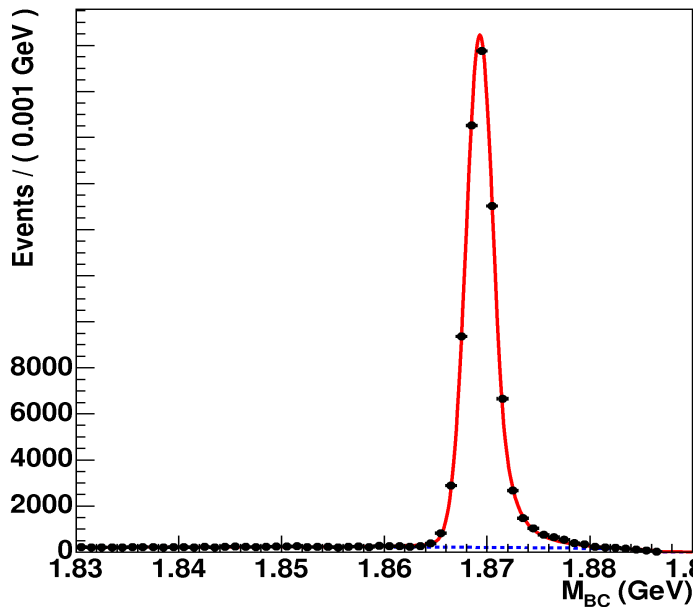
Extract yields from

$$m_{BC} = \sqrt{E_{\text{beam}}^2 - P_D^2}$$

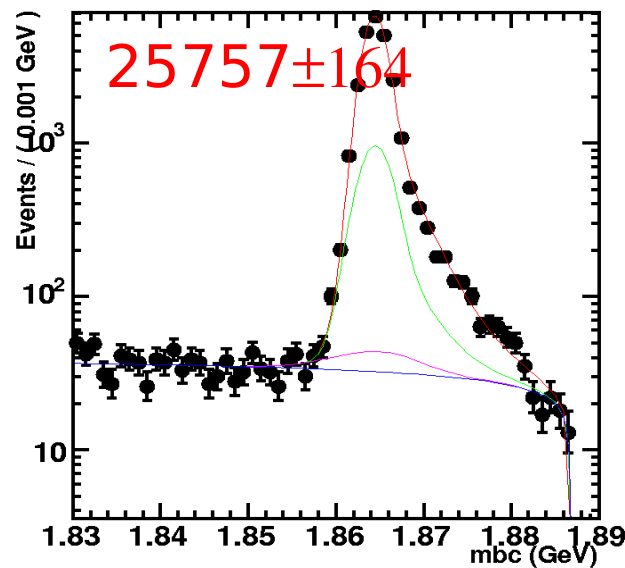
Lineshape includes

- ◆ Detector resolution
- ◆ ISR in  $e^+e^- \rightarrow \psi(3770)$
- ◆  $\psi(3770)$  lineshape
- ◆ Beam energy spread

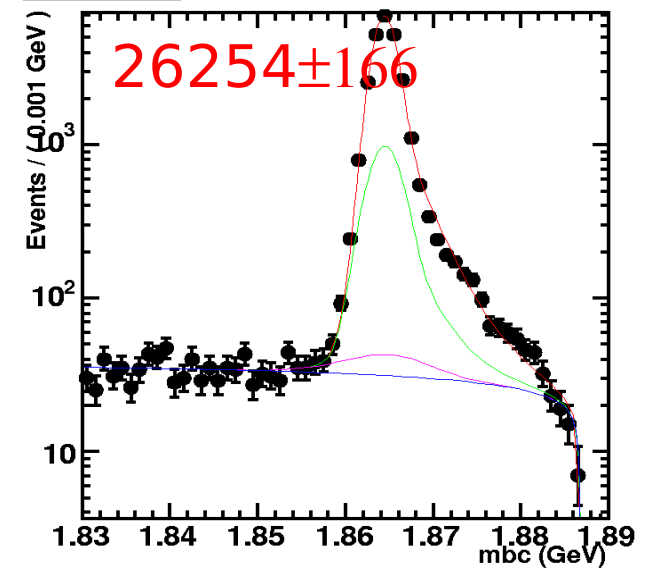
Linear scale



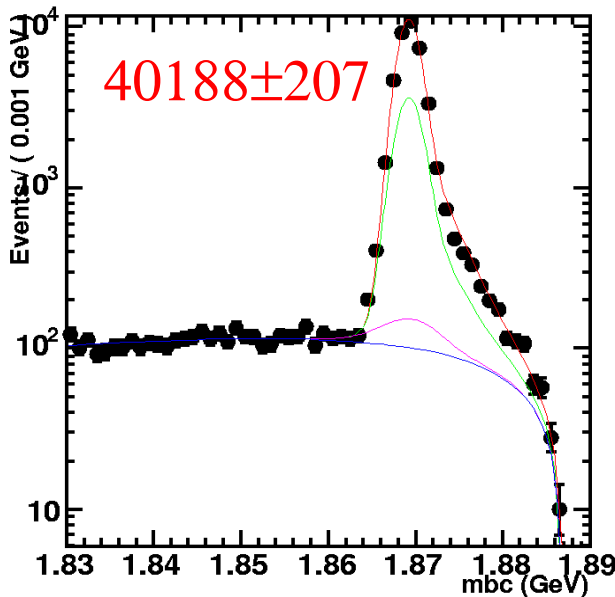
$D^0 \rightarrow K^- \pi^+$



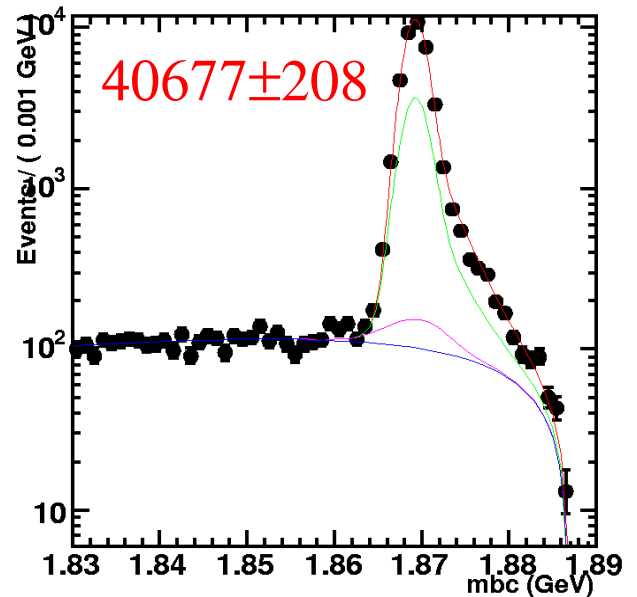
$D^0 \rightarrow K^+ \pi^-$



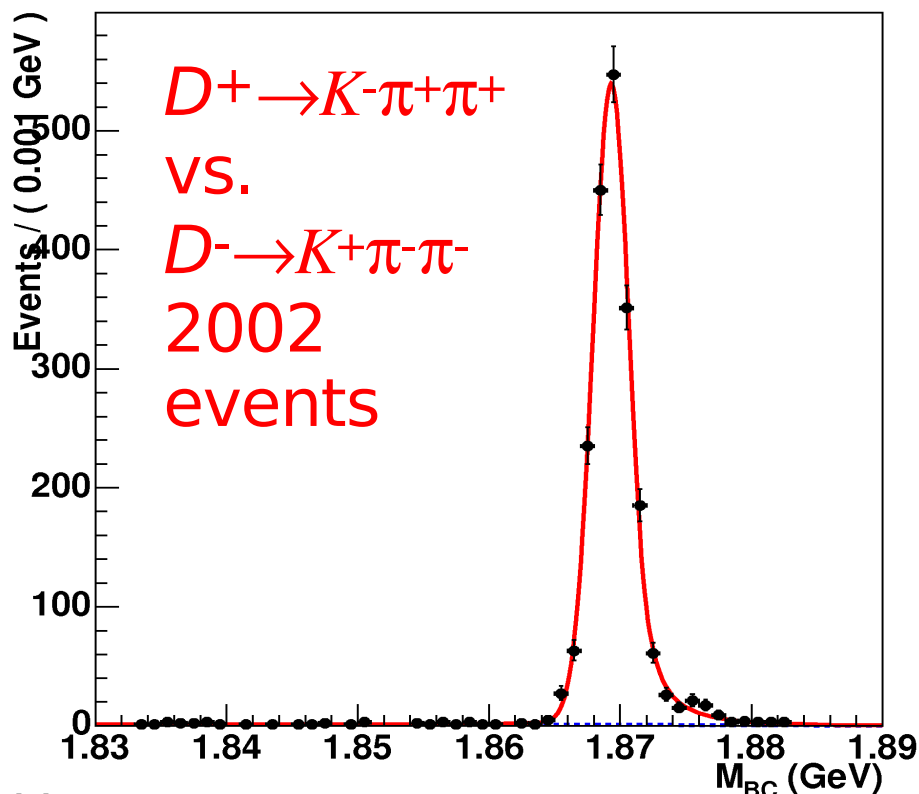
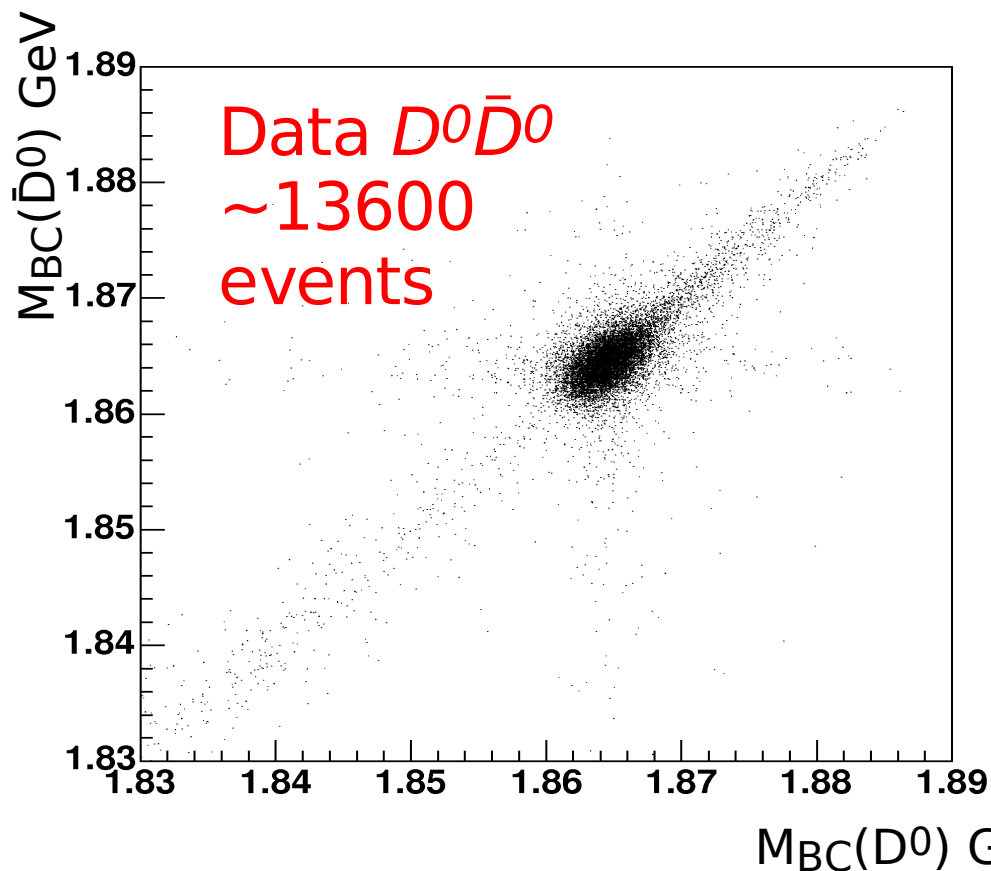
$D^+ \rightarrow K^- \pi^+ \pi^+$



$D^+ \rightarrow K^+ \pi^- \pi^-$



# Double Tag Yields (281 pb<sup>-1</sup>)



- Very clean signals in fully reconstructed events
- The statistical errors on the double tag yields set the scale of errors on the branching fractions



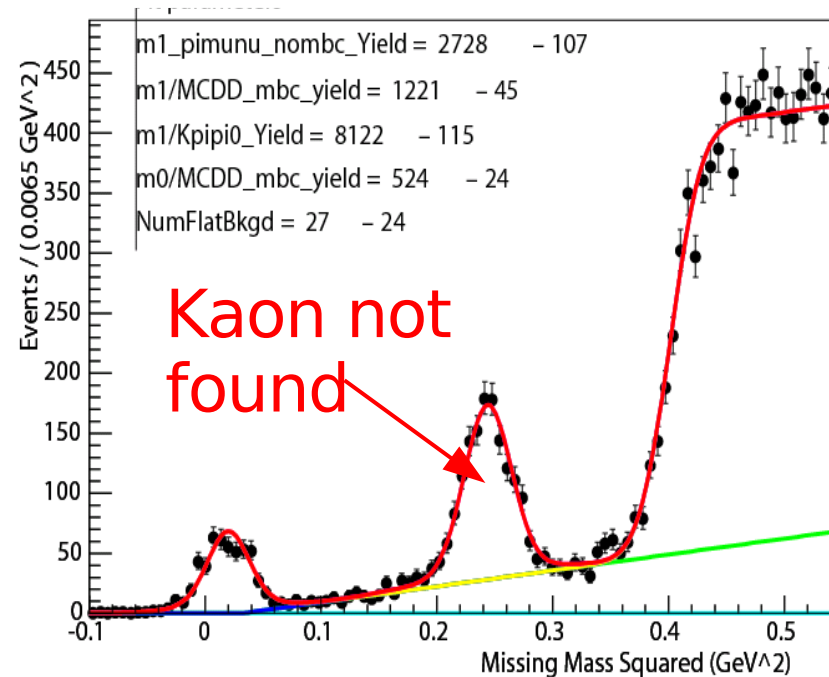
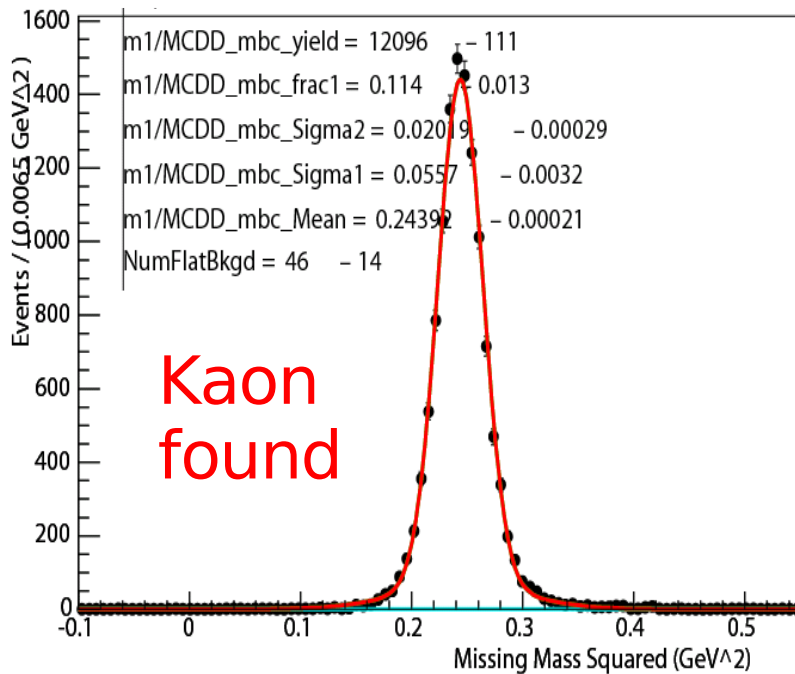
# Systematics

- Some systematics improve with more data.

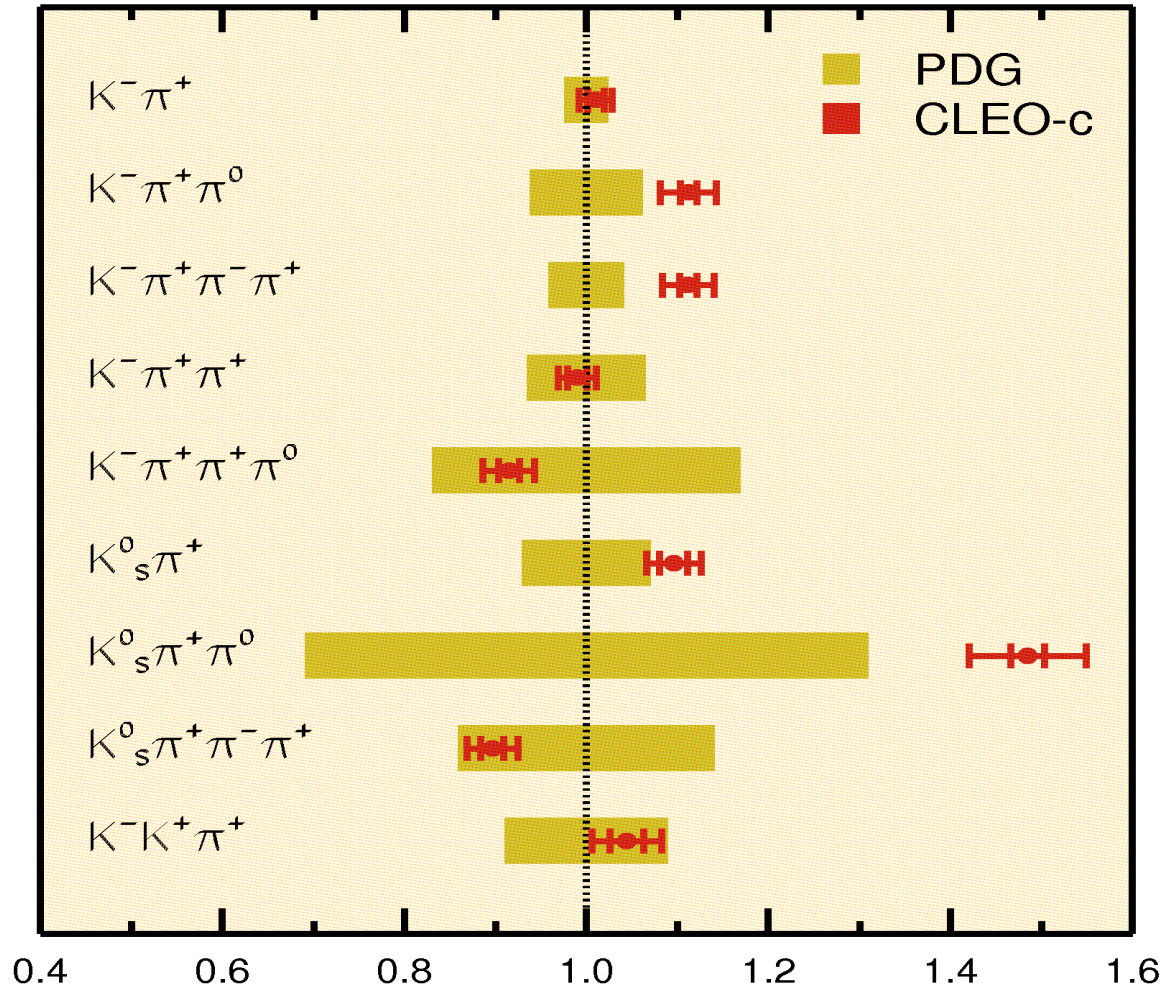
<u>Systematic</u>	<u>Old Value (56 pb<sup>-1</sup>)</u>	<u>New Value (281 pb<sup>-1</sup>)</u>
Data processing	0.3%	0.0%
Background shape	0.5%	0.5%
Double DCSD interference	0.8%	0.8%
Tracking efficiency	0.7%	0.3%
$K_S^0$ efficiency	3.0%	1.1%
$\pi^0$ efficiency	2.0%	2.0%
Pion particle ID	0.3%	0.25%
Kaon particle ID	1.3%	0.3%
Trigger simulation	0.0-0.2%	0.0-0.2%
Final state radiation	0.5%	0.5%
$\Delta E$ cuts	1.0-2.5%	0.5-1.0%
Signal shape	0.6%	0.4-0.6%
Resonant substructure	0.4-1.5%	0.3-1.3%
Multiple candidates	0.0-1.3%	0.0-1.3%

# Tracking Efficiencies

- Events that can be fully reconstructed can be used for very clean studies of tracking efficiencies
- We have used  $D\bar{D}$  events and  $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$  events
- Look at recoil mass against  $D^0$ -tag and pion – see how often kaon is found
  - In data we find  $\varepsilon = (90.8 \pm 0.4)\%$



# Preliminary Results for 281 pb<sup>-1</sup>



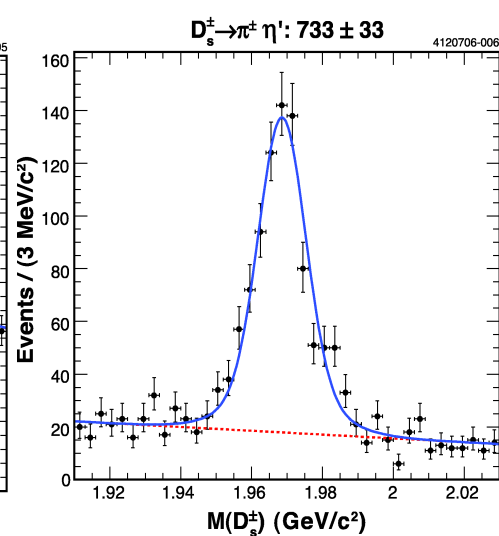
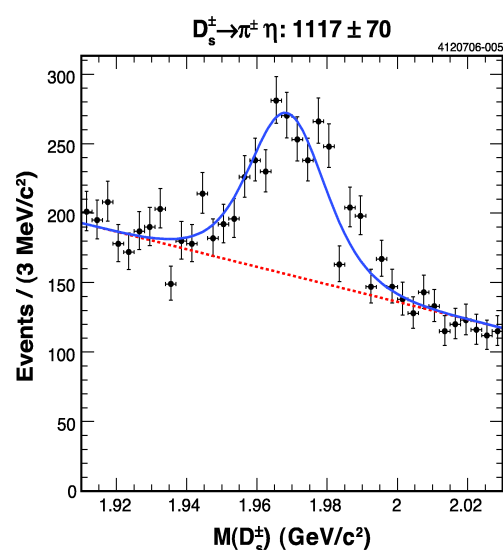
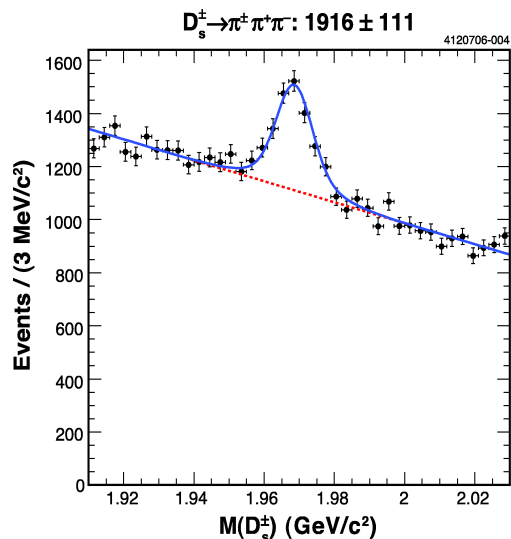
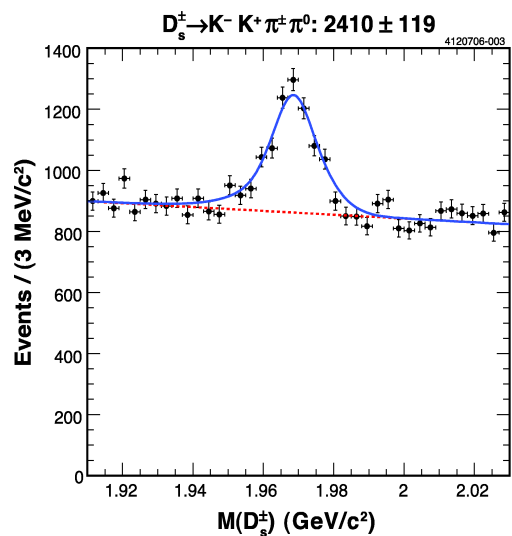
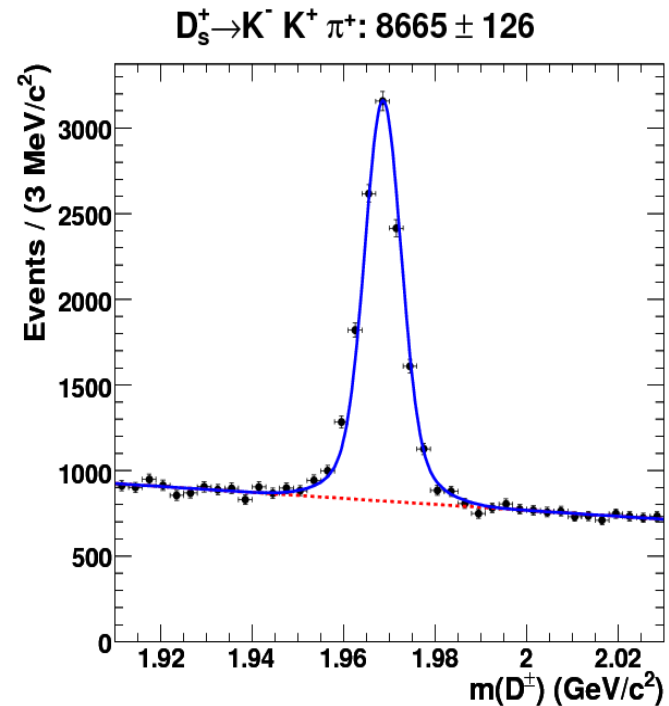
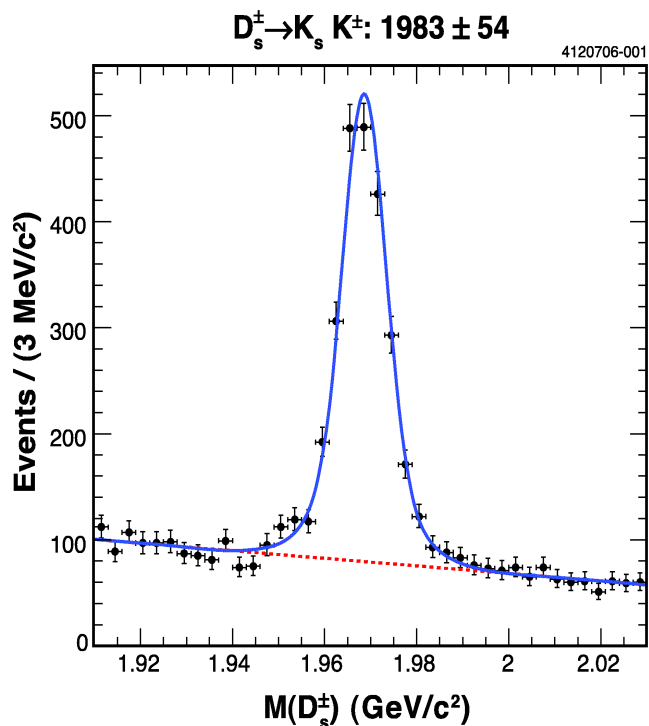
- Statistical error ~1%
- Systematics dominated
  - Will improve some errors
- Final results on 281 pb<sup>-1</sup> later this year.

# $D_S$ Absolute Hadronic Branching Fractions

- Use same technique as for the  $D^0$  and  $D^+$  branching fractions
  - Pairs of  $D_S$  and  $D_S^*$
- Use invariant mass after cut on  $m_{BC}$  for signal extraction
  - Signal will not peak in  $m_{BC}$  unless the  $D_S$  is direct
- We use  $195 \text{ pb}^{-1}$  of data recorded at (or near)  $E_{cm}=4170 \text{ MeV}$
- We study the final states:
  - $K_S K^+$
  - $K^+ K^- \pi^+$
  - $K^+ K^- \pi^+ \pi^0$
  - $\pi^+ \pi^- \pi^+$
  - $\eta \pi^+$
  - $\eta' \pi^+$

# Single Tag Yields

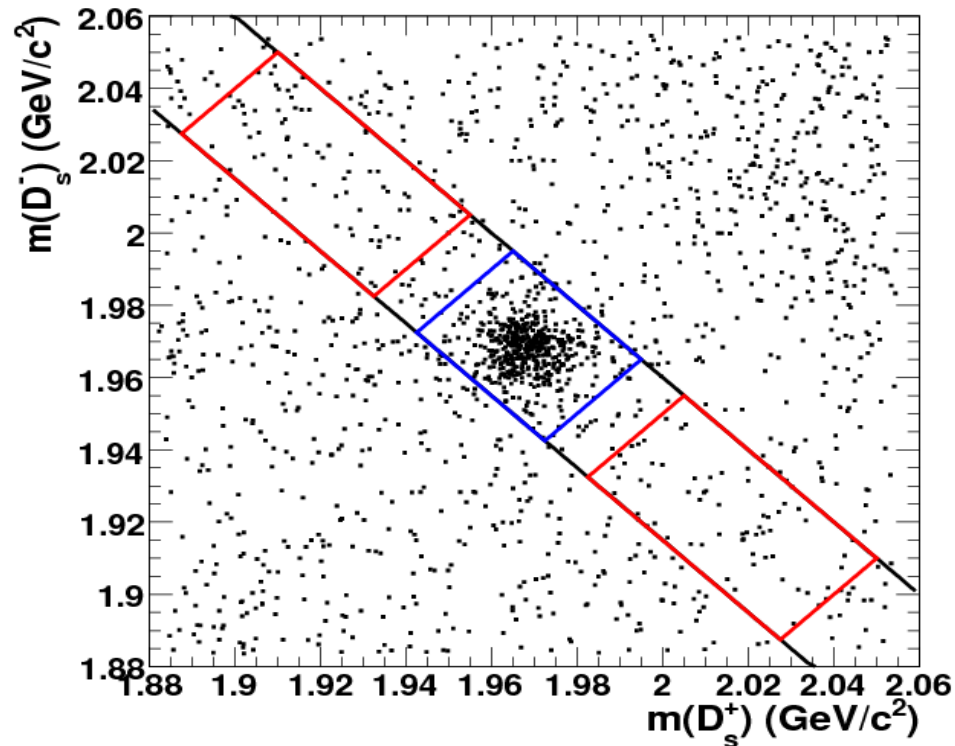
Mode	$D_s^+$	$D_s^-$
$K_s K^+$	$1055 \pm 39$	$928 \pm 37$
$K^+ K^- \pi^+$	$4316 \pm 89$	$4350 \pm 89$
$K^+ K^- \pi^+ \pi$	$1160 \pm 85$	$1251 \pm 84$
$\pi^+ \pi^- \pi^+$	$970 \pm 80$	$947 \pm 78$
$\eta \pi^+$	$547 \pm 50$	$570 \pm 50$
$\eta' \pi^+$	$362 \pm 23$	$372 \pm 24$





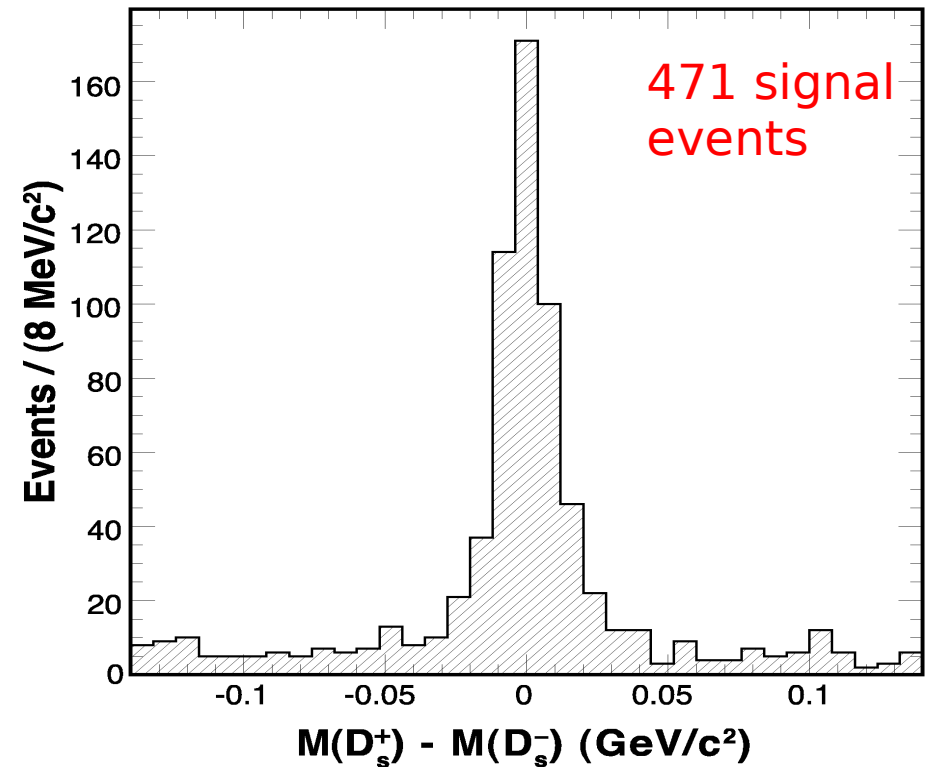
# Double Tag Yields

All double tags



All Double Tags

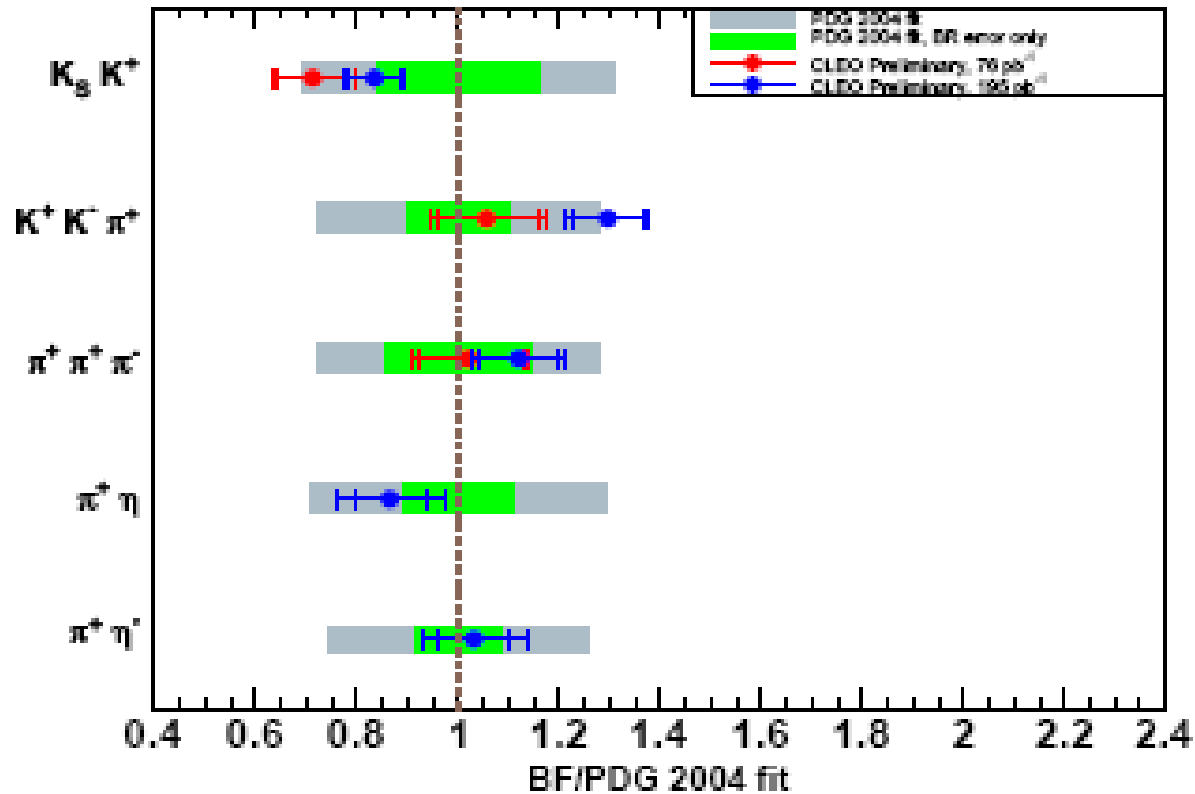
4120706-008



Yields from cut-and-count in blue signal region

	$K_S K^-$	$K^+ K^- \pi^-$	$K^+ K^- \pi^- \pi^0$	$\pi^- \pi^- \pi^+$	$\pi^- \eta$	$\pi^- \eta'$
$K_S K^+$	7.7	27.0	18.7	7.3	4.0	5.0
$K^- K^+ \pi^+$	18.0	104.7	43.7	30.7	12.0	8.0
$K^- K^+ \pi^+ \pi^0$	8.7	35.7	14.0	13.3	1.0	5.7
$\pi^+ \pi^+ \pi^-$	3.3	22.7	16.0	13.3	4.7	4.0
$\pi^+ \eta$	0.0	10.0	2.7	6.0	1.0	1.7
$\pi^+ \eta'$	3.0	10.0	3.0	3.7	1.0	0.0

# $D_S$ Hadronic Branching Fractions



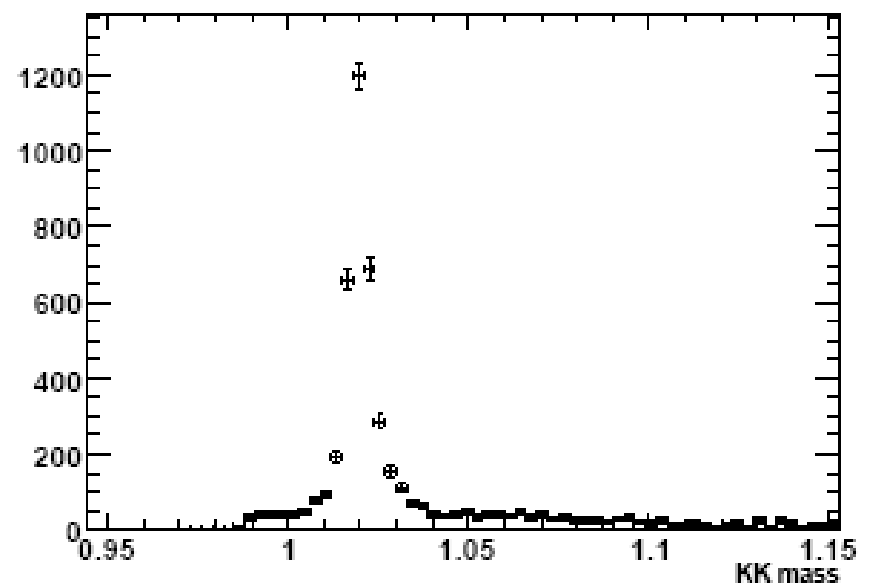
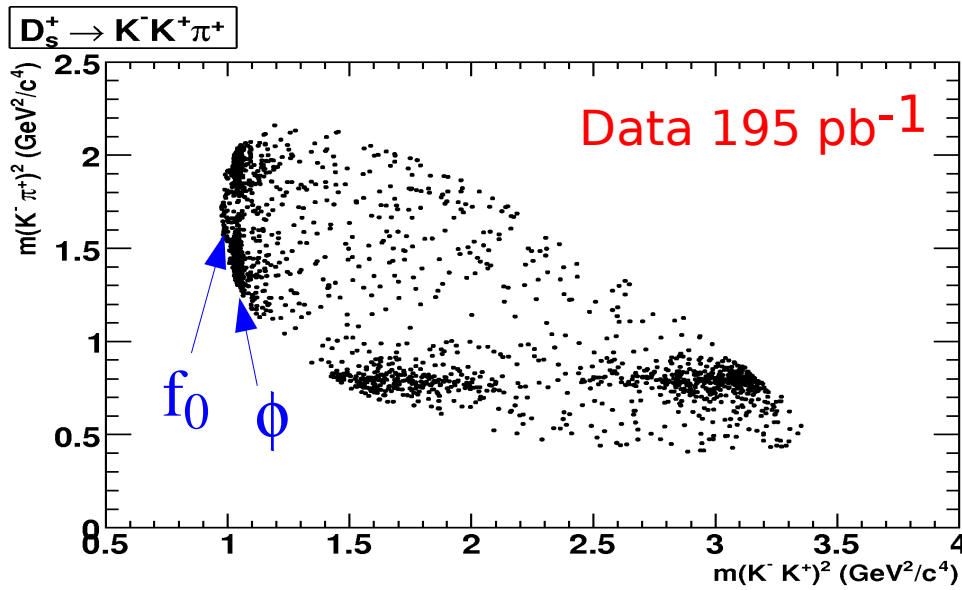
Mode	195 $\text{pb}^{-1}$ (%)	PDG 2004 fit (%)
$\mathcal{B}(K_S K^+)$	$1.50 \pm 0.09 \pm 0.05$	$1.8 \pm 0.55$
$\mathcal{B}(K^- K^+ \pi^+)$	$5.57 \pm 0.30 \pm 0.19$	$4.3 \pm 1.2$
$\mathcal{B}(K^- K^+ \pi^+ \pi^0)$	$5.62 \pm 0.33 \pm 0.51$	—
$\mathcal{B}(\pi^+ \pi^+ \pi^-)$	$1.12 \pm 0.08 \pm 0.05$	$1.00 \pm 0.28$
$\mathcal{B}(\pi^+ \eta)$	$1.47 \pm 0.12 \pm 0.14$	$1.7 \pm 0.5$
$\mathcal{B}(\pi^+ \eta')$	$4.02 \pm 0.27 \pm 0.30$	$3.9 \pm 1.0$

# What about $D_S \rightarrow \phi \pi$ ?

- $D_S \rightarrow \phi \pi$  interferes with  $D_S \rightarrow f_0 \pi$ 
  - $B(D_S \rightarrow \phi \pi)$  is not well defined and we are not quoting it now
  - We can calculate a “partial br. fr.” in a  $m_{KK}$  window around the  $\phi$  mass

$D_S \rightarrow K^+ K^- \pi^+$  partial BF:  
 CLEO- c ( $\pm 10$  MeV around  $\phi$ )  
 **$1.98 \pm 0.12 \pm 0.09$**   
 ( $\sim x2 + O(10\%)$ ) (Preliminary !!)

For reference:  $D_S \rightarrow \phi \pi^+$   
 PDG06:  $4.4 \pm 0.6$   
 BaBar:  $4.8 \pm 0.5 \pm 0.4$   
 ( $1.008 < M(K^+ K^-) < 1.035$  GeV)



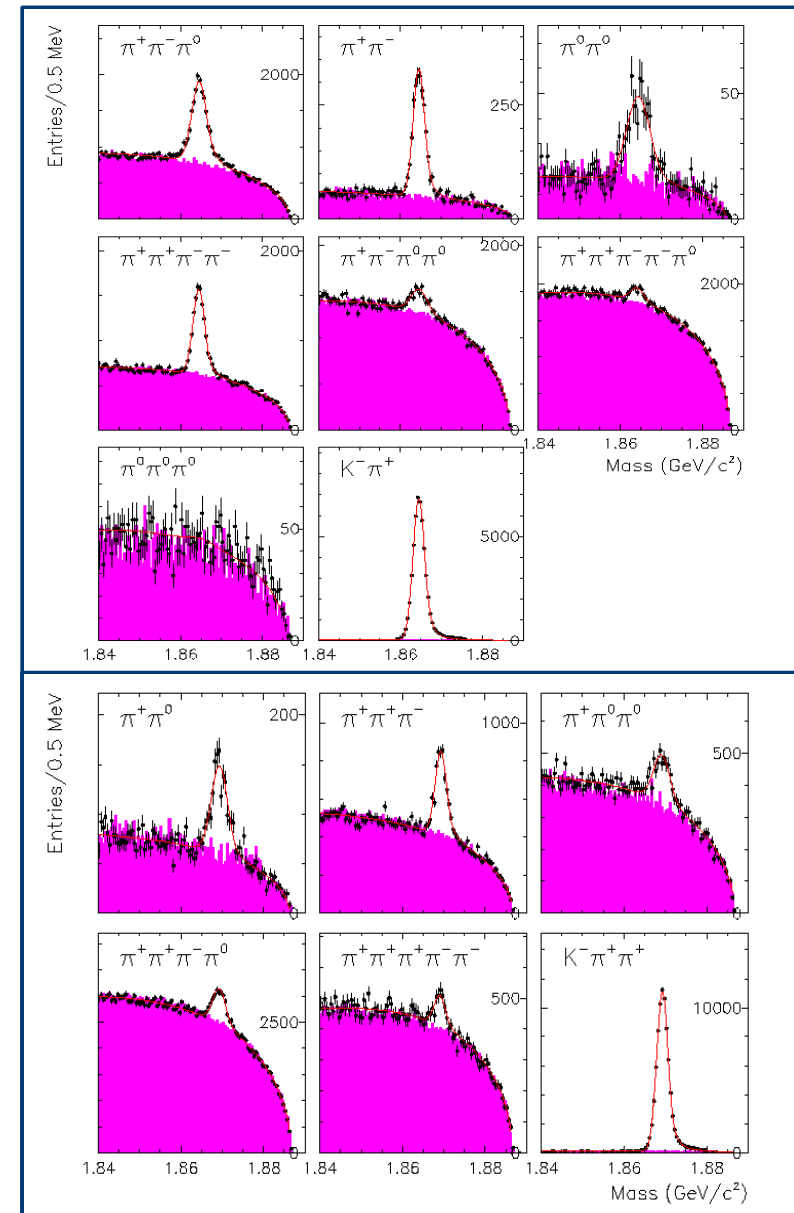
# $D \rightarrow n(\pi^\pm)m(\pi^0)$

(PRL 96, 081802 2006)

- This analysis doesn't use  $D$ -tags.
- Measure relative to normalization mode ( $D^0 \rightarrow K^- \pi^+$  or  $D^+ \rightarrow K^- \pi^+ \pi^+$ )

281 pb<sup>-1</sup>

Mode	$B (\times 10^{-3})$	PDG ( $\times 10^{-3}$ )
$\pi^+ \pi^-$	$1.40 \pm 0.04 \pm 0.03$	$1.38 \pm 0.05$
$\pi^0 \pi^0$	$0.78 \pm 0.05 \pm 0.04$	$0.84 \pm 0.22$
$\pi^+ \pi^- \pi^0$	$13.3 \pm 0.2 \pm 0.5$	$11 \pm 4$
$\pi^0 \pi^0 \pi^0$	$< 0.30$	---
$\pi^+ \pi^+ \pi^- \pi^-$	$7.42 \pm 0.14 \pm 0.27$	$7.3 \pm 0.5$
$\pi^+ \pi^- \pi^0 \pi^0$	$10.2 \pm 0.6 \pm 0.7$	---
$\pi^+ \pi^+ \pi^- \pi^0$	$4.31 \pm 0.44 \pm 0.18$	---
$\pi^+ \pi^0$	$1.23 \pm 0.06 \pm 0.06$	$1.33 \pm 0.22$
$\pi^+ \pi^+ \pi^-$	$3.36 \pm 0.10 \pm 0.16$	$3.1 \pm 0.4$
$\pi^+ \pi^0 \pi^0$	$4.80 \pm 0.27 \pm 0.34$	---
$\pi^+ \pi^+ \pi^- \pi^0$	$11.7 \pm 0.4 \pm 0.7$	---
$\pi^+ \pi^+ \pi^+ \pi^- \pi^-$	$1.67 \pm 0.18 \pm 0.17$	$1.82 \pm 0.25$
$\eta \pi^+$	$3.56 \pm 0.24 \pm 0.21$	$3.0 \pm 0.6$
$\eta \pi^0$	$0.61 \pm 0.14 \pm 0.05$	---
$\omega \pi^+ \pi^-$	$1.66 \pm 0.47 \pm 0.10$	---



# Inclusive $\eta$ , $\eta'$ , and $\phi$ Production in $D$ and $D_S$ Decays

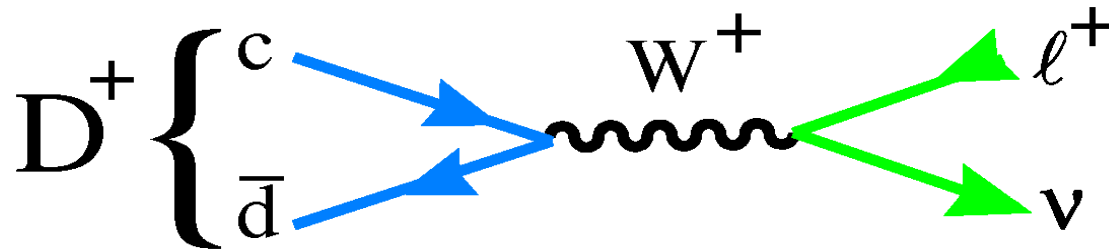
- Tag one  $D$  or  $D_S$  and look at the recoil
  - 281 pb<sup>-1</sup> for  $D^0$  and  $D^+$
  - 71 pb<sup>-1</sup> for  $D_S$
- We see that the production of  $\eta$ ,  $\eta'$ , and  $\phi$  is larger in  $D_S$  decays than in  $D$  decays.
- Important branching fractions for studying  $B_S$  decays.

$B$	$\eta$ (%)	PDG
$D^0$	$9.4 \pm 0.4 \pm 0.6$	<13%
$D^+$	$5.7 \pm 0.5 \pm 0.5$	<13%
$D_S^+$	$23.7 \pm 3.1 \pm 1.9$	-

$B$	$\eta'$ (%)	PDG
$D^0$	$2.6 \pm 0.2 \pm 0.2$	-
$D^+$	$1.0 \pm 0.2 \pm 0.1$	-
$D_S^+$	$8.7 \pm 1.9 \pm 0.6$	-

$B$	$\phi$ (%)	PDG
$D^0$	$1.0 \pm 0.1 \pm 0.1$	$1.7 \pm 0.8$
$D^+$	$1.1 \pm 0.1 \pm 0.2$	<1.8
$D_S^+$	$16.1 \pm 1.2 \pm 0.6$	$18^{+15}_{-10}$

$$D^+ \rightarrow \mu^+ \nu_\mu \text{ and } f_{D^+}$$

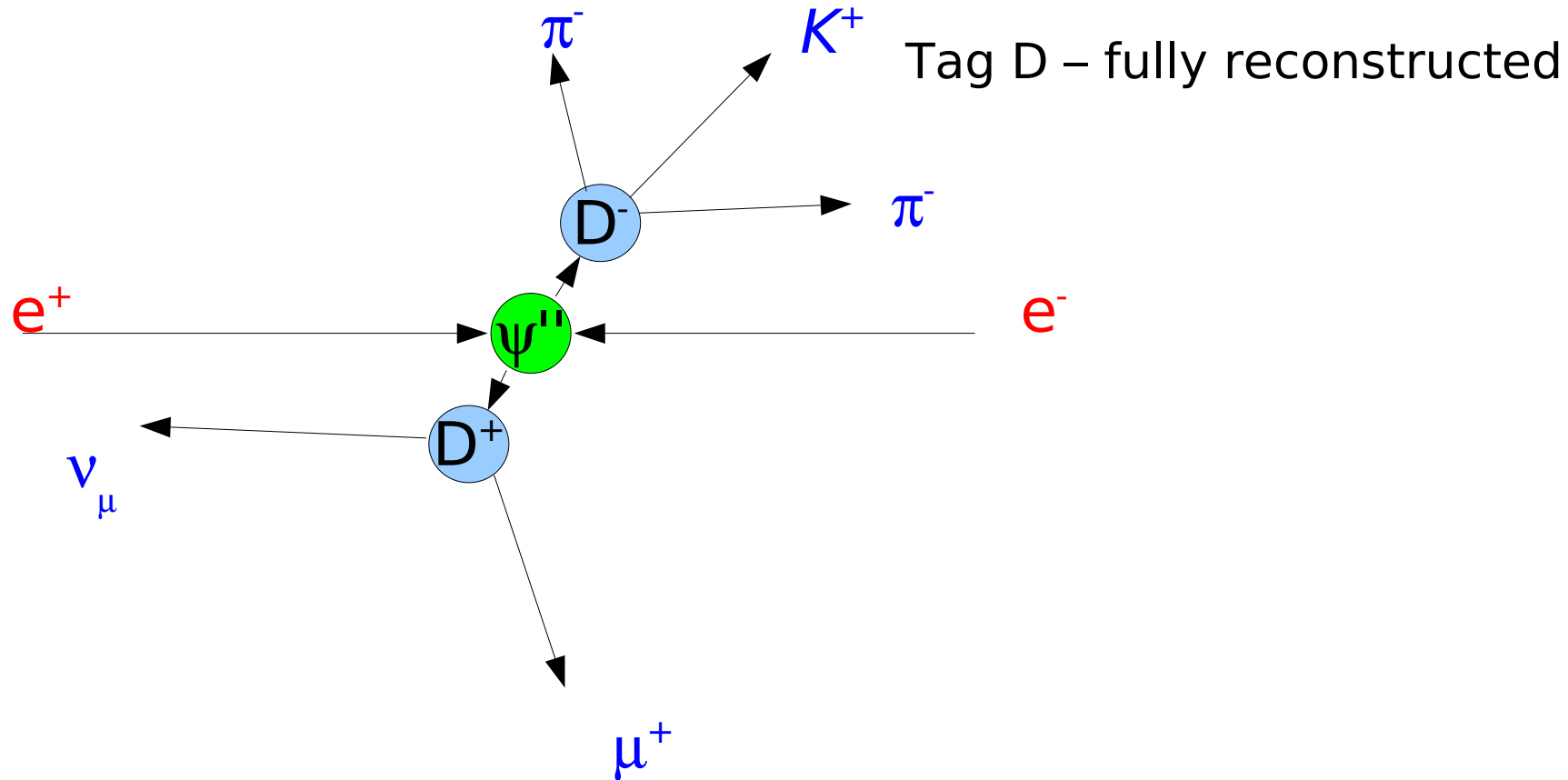


$$\Gamma(D^+ \rightarrow l^+ \nu) = \frac{G_F^2}{8\pi} f_{D^+}^2 m_l^2 M_{D^+} \left(1 - \frac{m_l^2}{M_{D^+}^2}\right)^2 |V_{cd}|^2$$

- Rate of e: $\mu$ : $\tau$  is  $\sim 10^{-4}:1:2.65$
- A precise measurement of  $f_D$  allows precise comparison with theoretical calculations, such as lattice QCD.
- This will help determining  $f_B$ .



# Analysis Technique

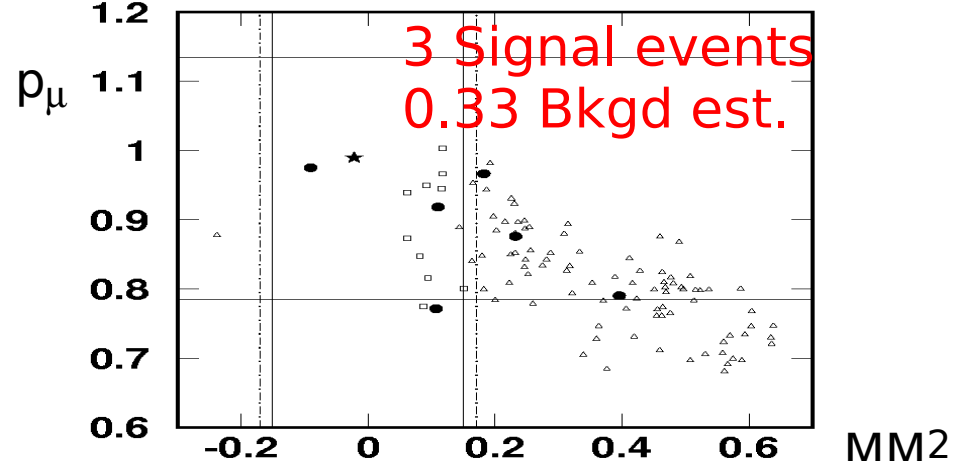
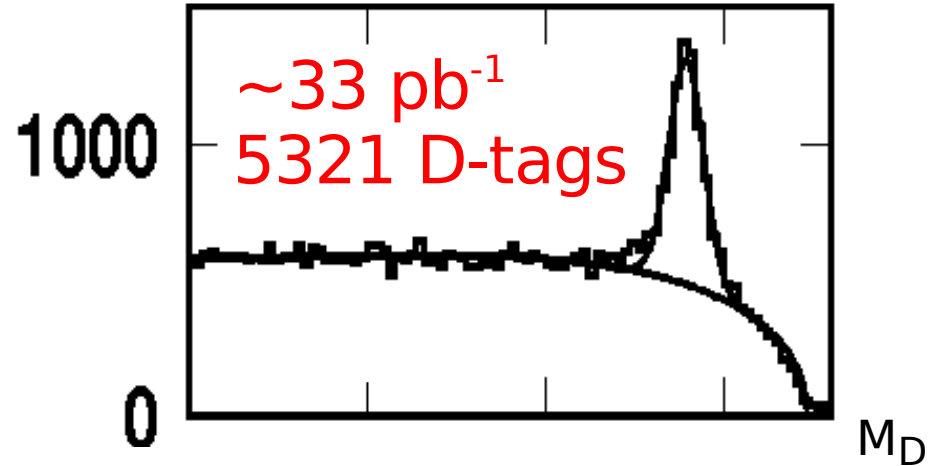
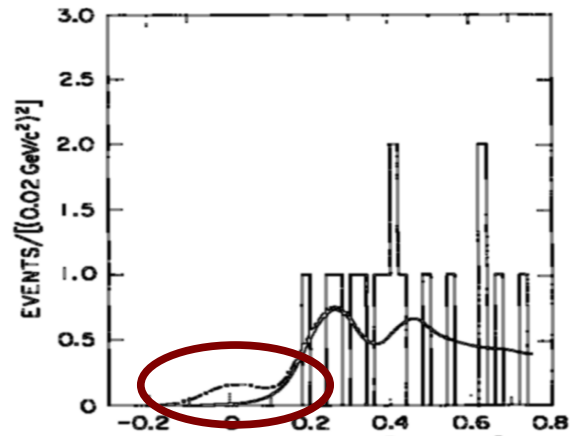
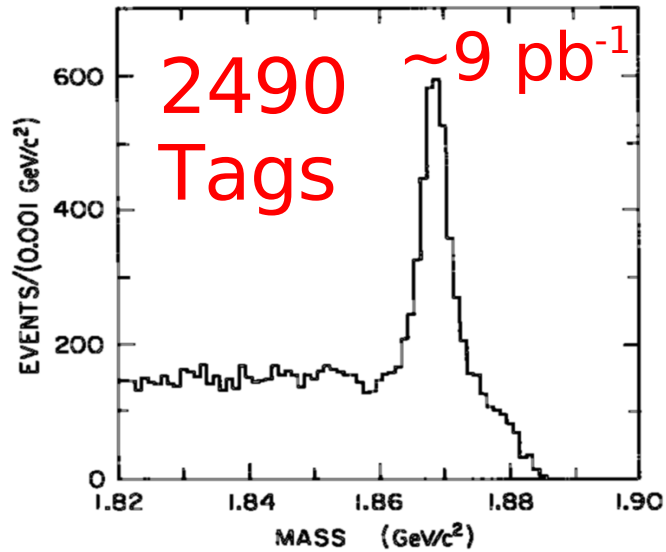


- At threshold produce only  $D^+D^-$ , no additional pions.
- Detect muon and make sure it recoiled against neutrino.
  - Extract signal in  $M_{\text{miss}}^2$  which peaks at 0.

# MARK III and BES Results

MARK III PRD 60, 1375

BES II PLB 610 (2005), 183



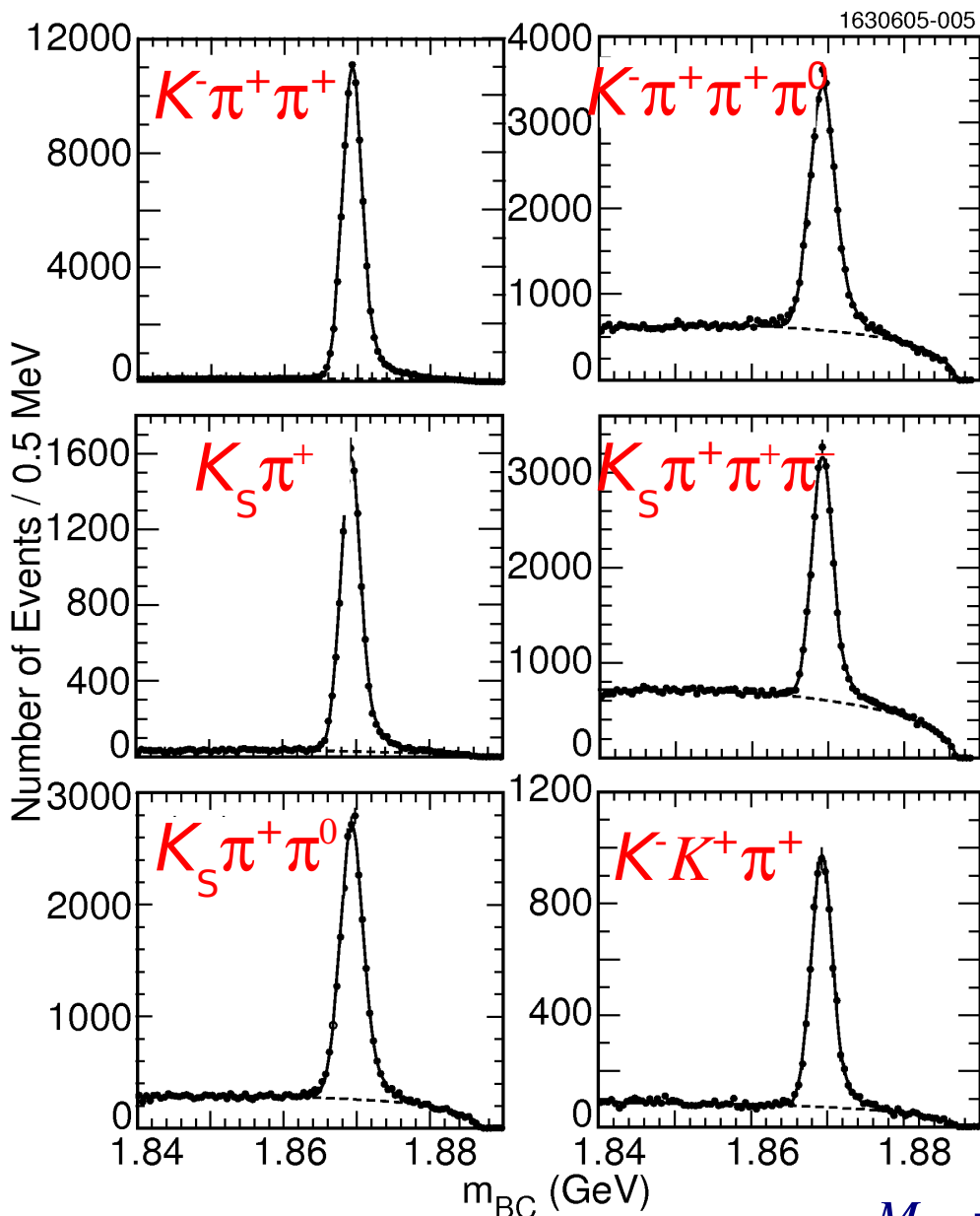
$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu_\mu) < 7.2 \times 10^{-4}$$

$$f_{D^+} < 290 \text{ MeV}$$

$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu_\mu) = (12.2_{-5.3}^{+11.1} \pm 0.10) \times 10^{-4}$$

$$f_{D^+} = (371_{-119}^{+129} \pm 25) \text{ MeV}$$

# CLEO-c $D$ -tag Reconstruction



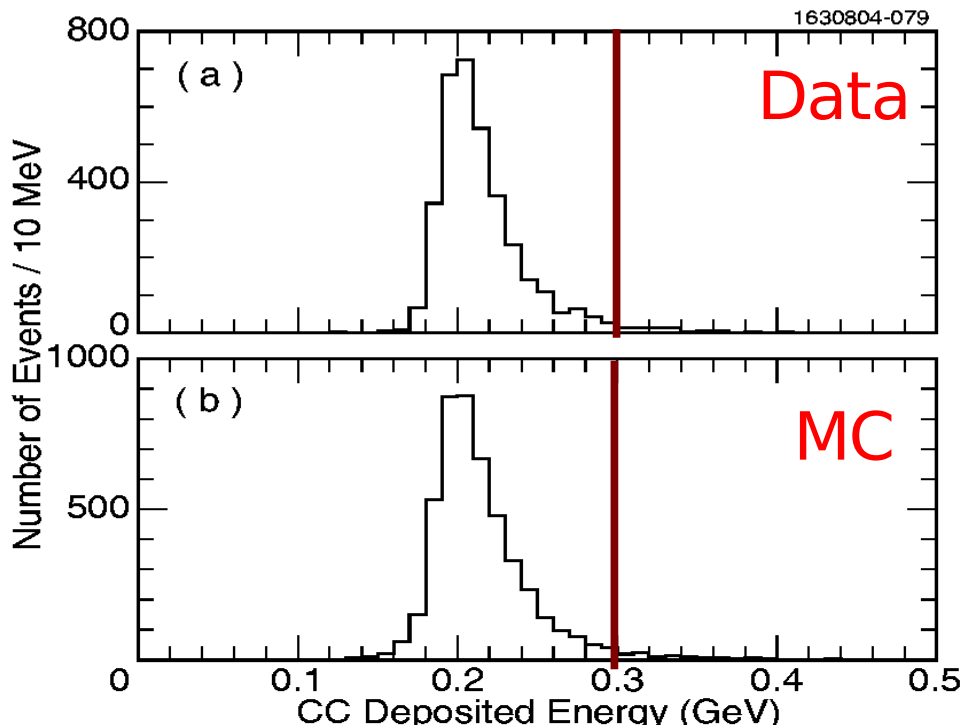
- 281 pb<sup>-1</sup>
- Six tag modes used
- ~160,000 reconstructed  $D^\pm$

Mode	Signal	Background
$K^+ \pi^- \pi^-$	$77387 \pm 281$	1868
$K^+ \pi^- \pi^- \pi^0$	$24850 \pm 214$	12825
$K_S \pi^-$	$11162 \pm 136$	514
$K_S \pi^- \pi^- \pi^+$	$18176 \pm 255$	8976
$K_S \pi^- \pi^0$	$20244 \pm 170$	5223
$K^+ K^- \pi^-$	$6535 \pm 95$	1271
Sum	$158354 \pm 496$	30677

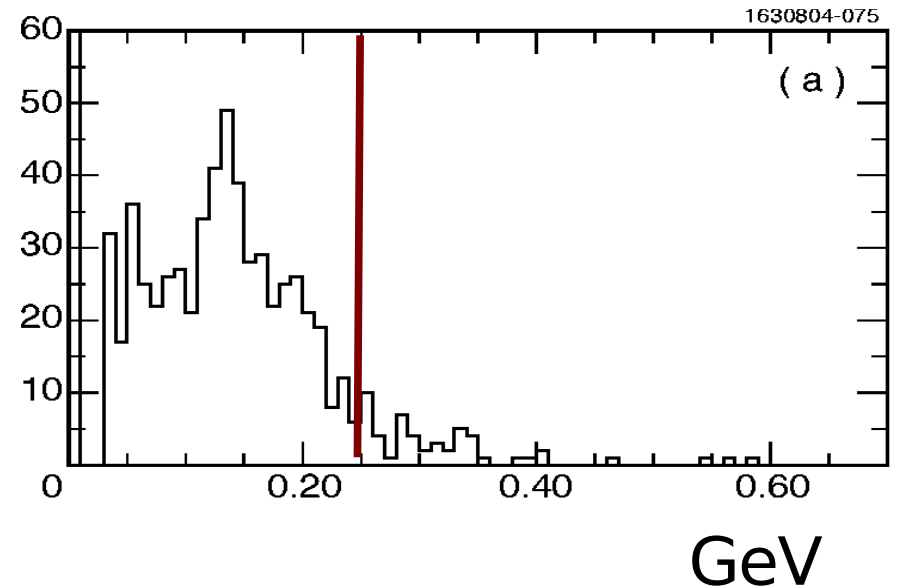
$$M_{BC} = \sqrt{E_{\text{beam}}^2 - |p(D)|^2}$$

# Signal Side Selection

- Require one track consistent with coming from the IP for the muon.
  - Muon candidate deposit less than **300 MeV** in EM calorimeter
- No additional track from IP
- Veto background from  $D^+ \rightarrow \pi^+ \pi^0$ 
  - Require no unmatched showers over **250 MeV**



Highest energy unmatched cluster



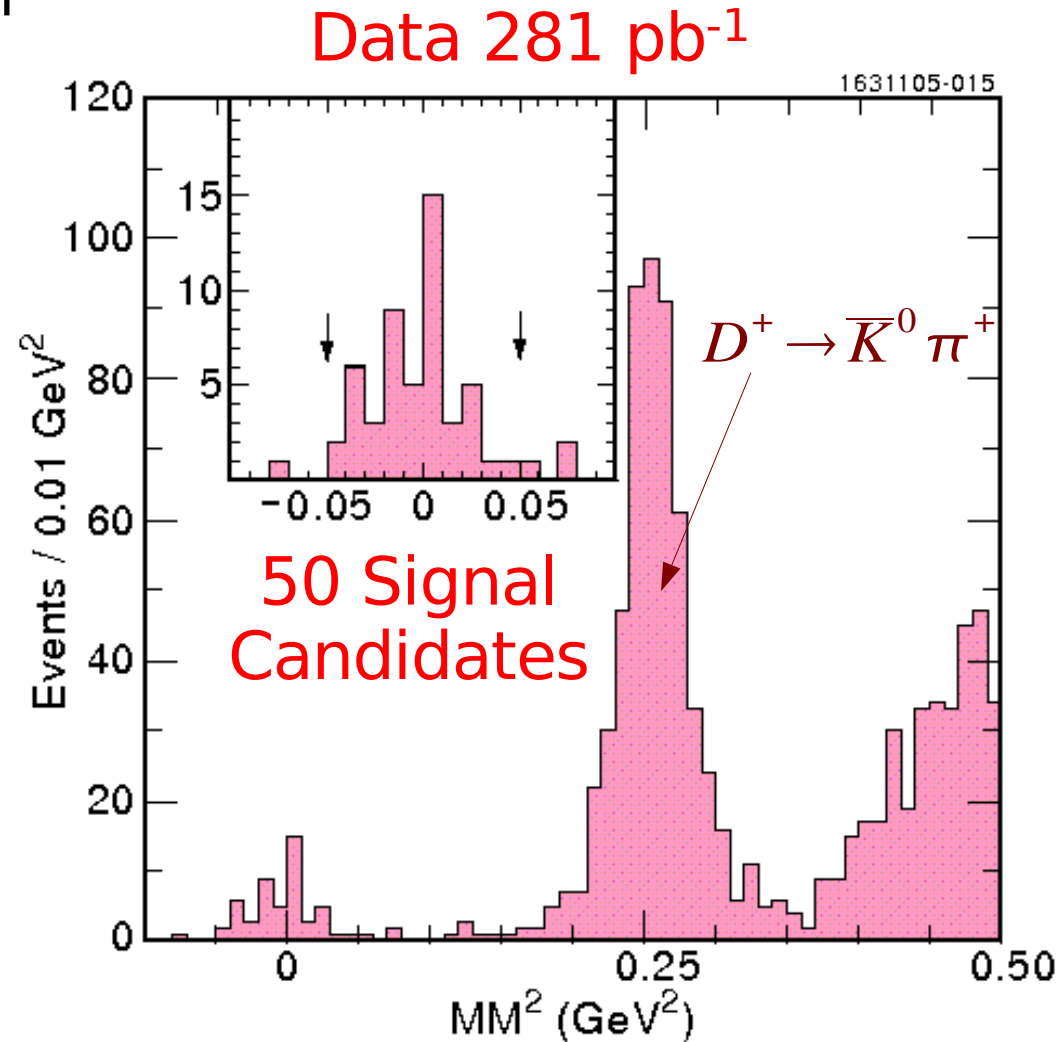
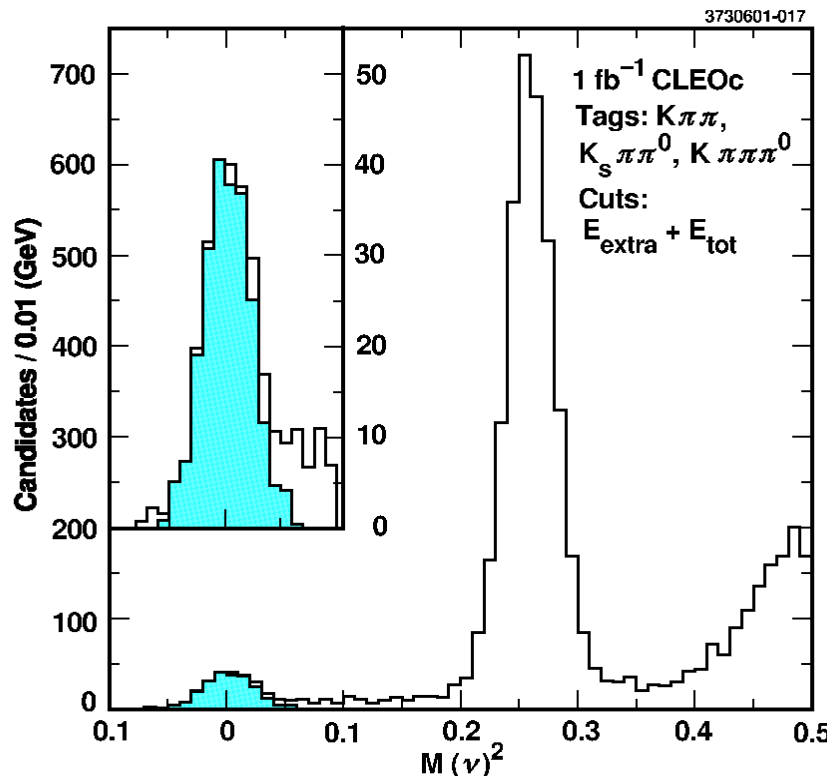
# Signal Extraction

- For events with  $\mu$  candidate form

$$MM^2 = (E_{beam} - E_{\mu})^2 - (-\vec{p}_D - \vec{p}_{\mu})^2$$

- Signal will peak at  $MM^2 = m_{\nu}^2 = 0$

“Yellow book” MC Study



# $D^+ \rightarrow \mu^+ \nu_\mu$ Results

- 50 signal candidate events with the following backgrounds

Background	$\mathcal{B}$ (%)	# of events
$D^+ \rightarrow \pi^+ \pi^0$	$0.13 \pm 0.02$	$1.40 \pm 0.18 \pm 0.22$
$D^+ \rightarrow K^0 \pi^+$	$2.77 \pm 0.18$	$0.33 \pm 0.19 \pm 0.02$
$D^+ \rightarrow \tau^+ \nu$	$2.6 \times \mathcal{B}(D^+ \rightarrow \mu^+ \nu)$	$1.08 \pm 0.15 \pm 0.16$
$D^0 \bar{D}^0, D^+ D^-$	—	$< 0.4, < 0.4, 90\% \text{ C.L.}$
continuum	—	$< 1.2 \text{ } 90\% \text{ C.L.}$
Total		$2.81 \pm 0.30 \pm_{-0.27}^{+0.84}$

- With 158,354  $D^+$  tags and an efficiency of 67.7% for signal events to satisfy the selection criteria given a  $D^+$  tag we obtain:

$$Br(D^+ \rightarrow \mu^+ \nu) = (4.40 \pm 0.66_{-0.12}^{+0.09}) \times 10^{-4} \quad f_{D^+} = (222.6 \pm 16.7_{-3.4}^{+2.8}) \text{ MeV}$$

PRL 95, 251801 (2005)

- We also obtain  $Br(D^+ \rightarrow e^+ \nu) < 2.4 \times 10^{-5}$  at 90 C.L.



# Search for $D \rightarrow \tau \nu_\tau$

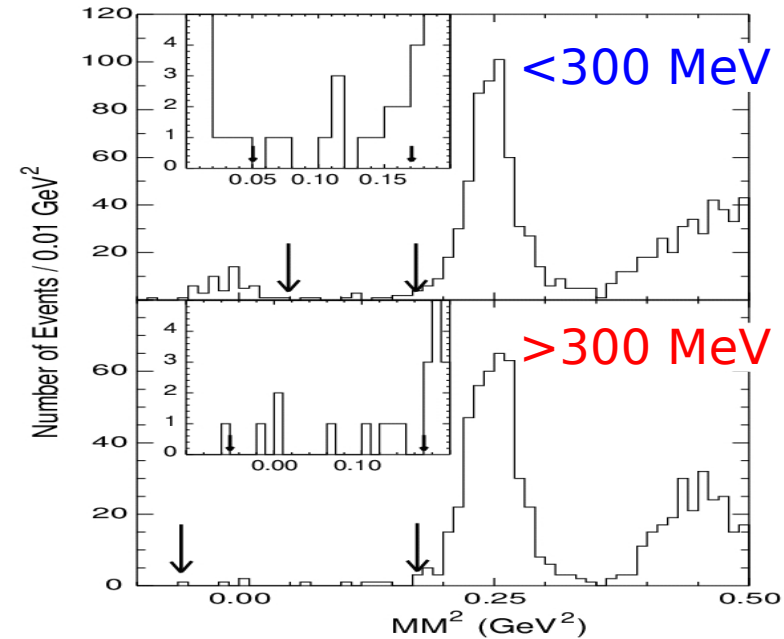
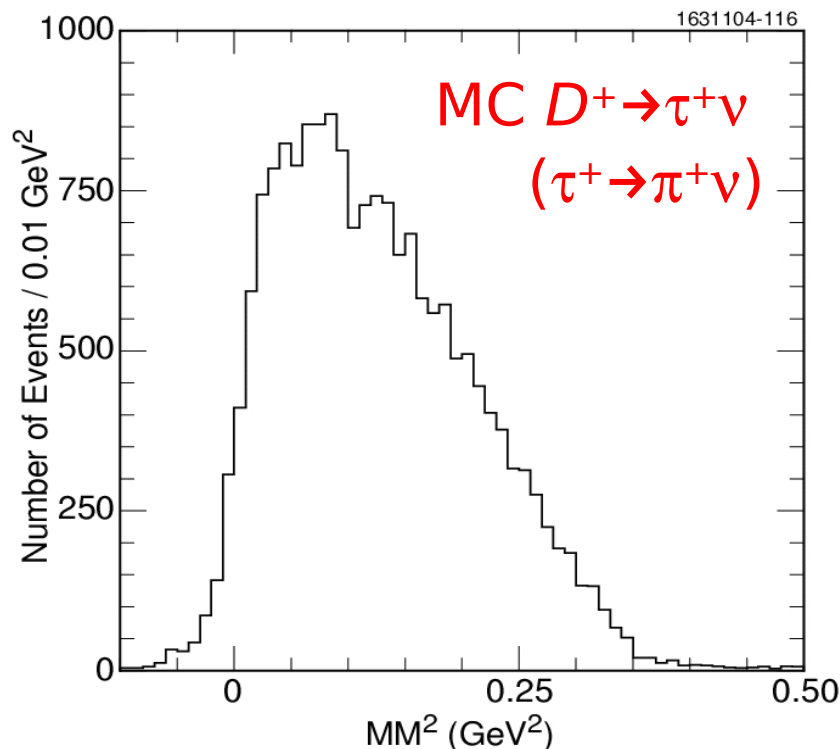
281pb<sup>-1</sup> hep-ex/0604043

(accepted by PRD)

Look for  $D^+ \rightarrow \tau^+ \nu$  ( $\tau^+ \rightarrow \pi^+ \nu$ ) in events with tags selected as for  $D^+ \rightarrow \mu^+ \nu$ .

Sample subdivided based on energy deposit of candidate track: (a) <300 MeV and (b) >300 MeV.

MM<sup>2</sup> small due to  $m_\tau$  close to  $m_D$



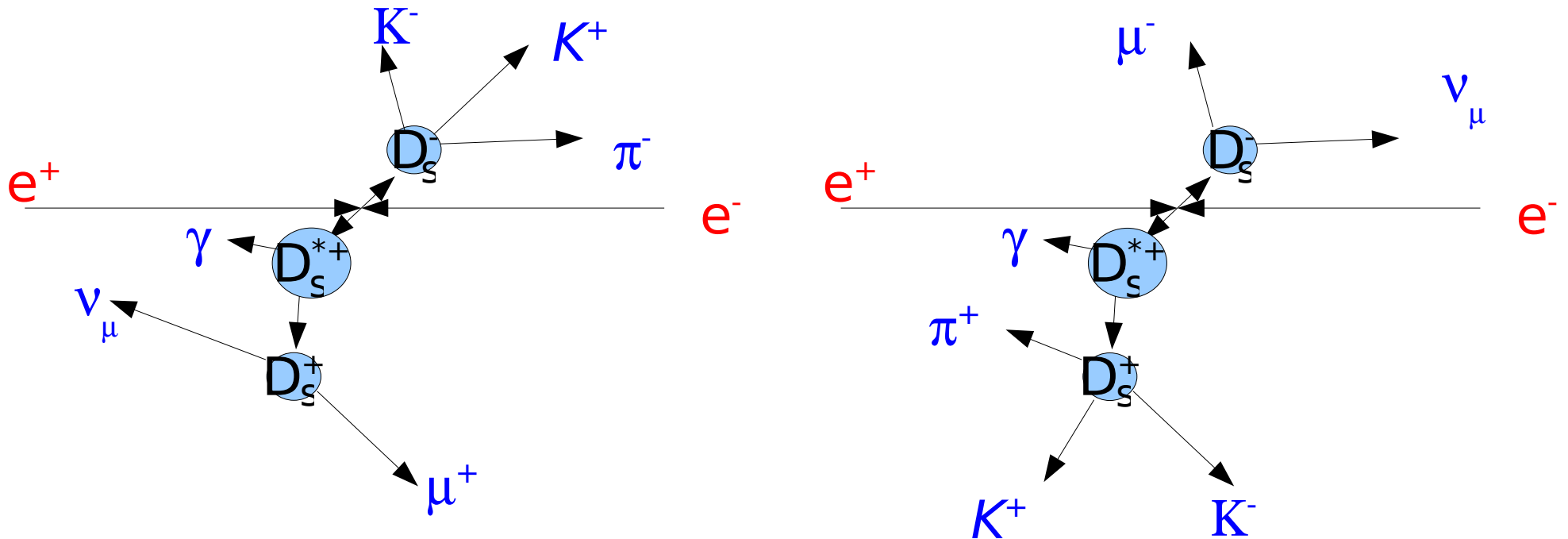
	(a)	(b)
Signal Region	12	8
Estimated BG	$6.1 \pm 0.6 \pm 0.3$	$5.0 \pm 0.6 \pm 0.2$
Net	$5.9 \pm 3.5 \pm 0.3$	$3.0 \pm 2.9 \pm 0.2$

$$BF(D^+ \rightarrow \tau^+ \nu) < 2.1 \times 10^{-3} \text{ (90\% CL)}$$

$$\text{SM} : BF(D^+ \rightarrow \tau^+ \nu) = (1.1 \pm 0.2) \times 10^{-3}$$

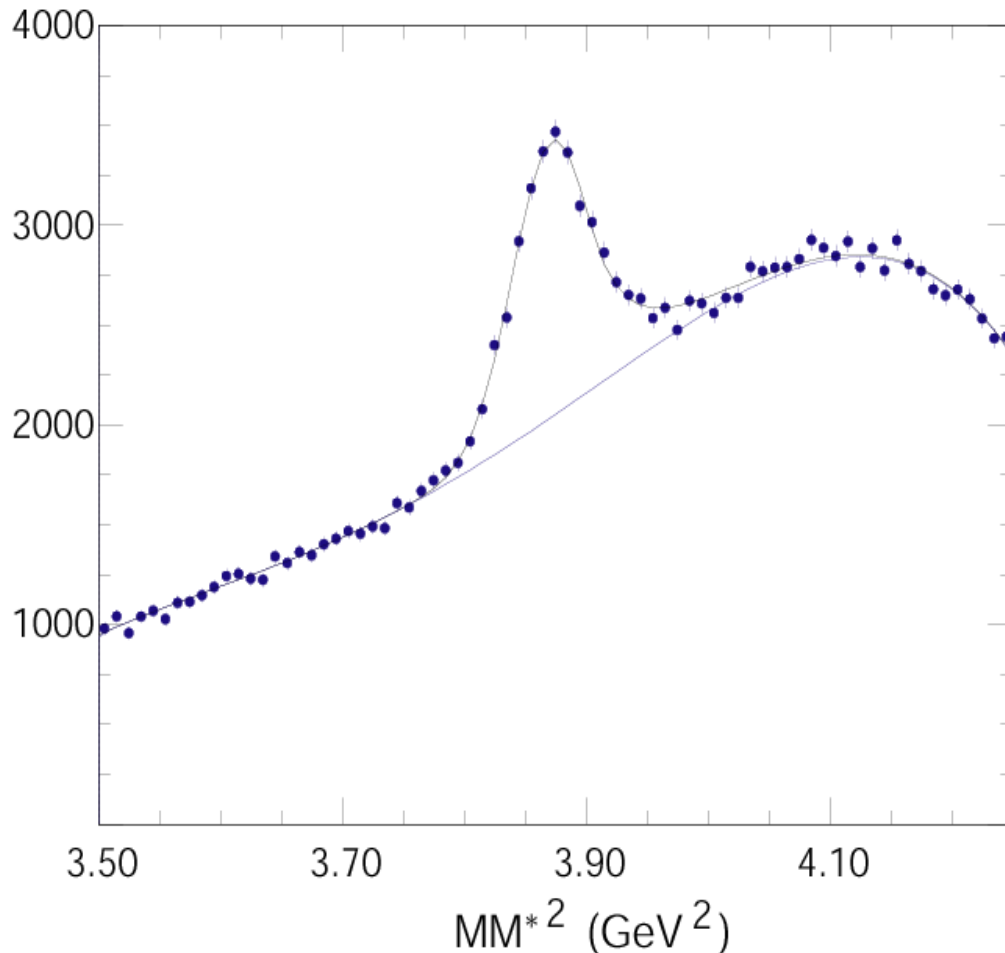
# $D_S \rightarrow \mu \nu_\mu$

- CLEO-c has used  $\sim 200 \text{ pb}^{-1}$  to study  $D_S \rightarrow \mu \nu_\mu$
- Signal  $D_S$  can come directly or from  $D_S^*$

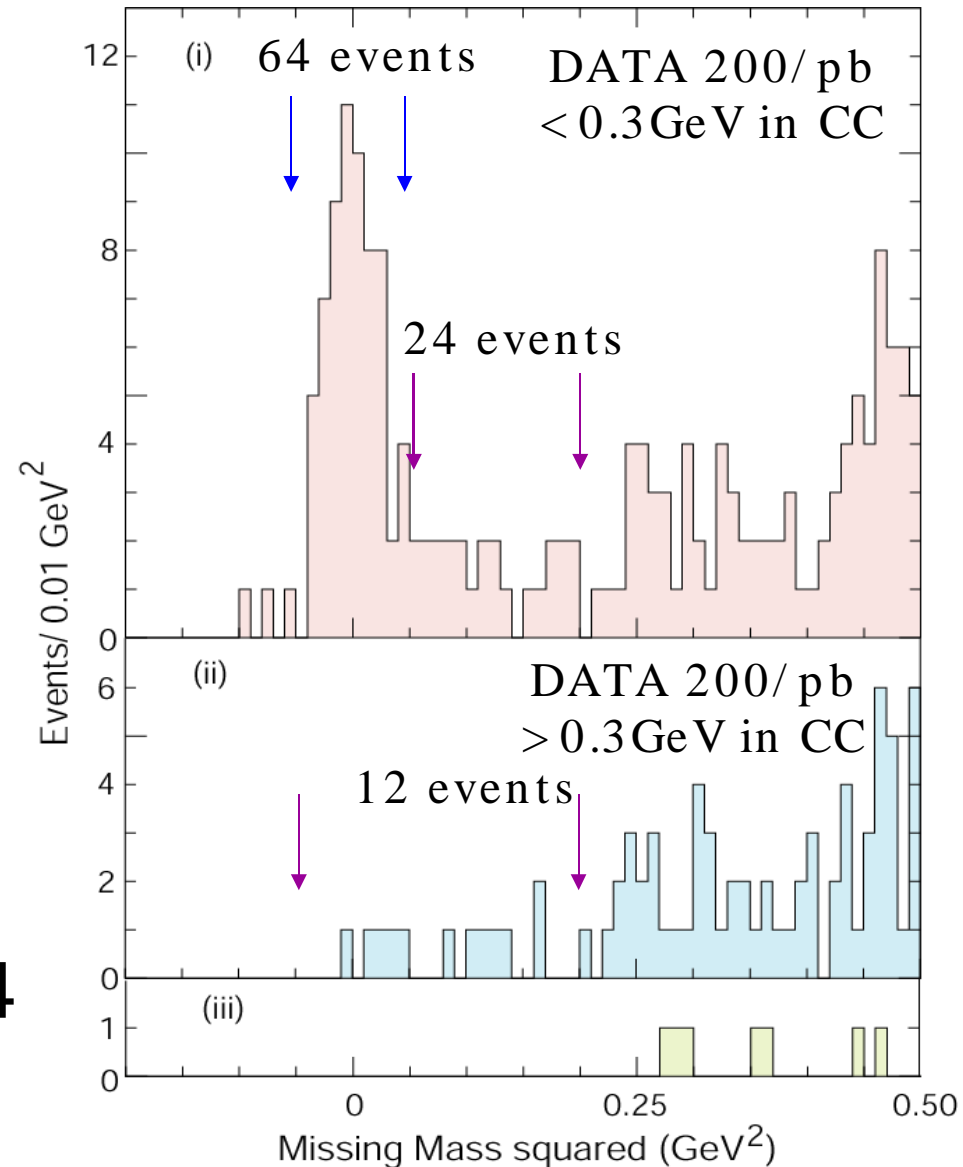


- Form  $\chi^2$  with both hypothesis for where the photon comes from. Keep best.
- Look for signal in missing mass.

# Tag Yields and Signal



- Total of  $11880 \pm 399 \pm 504$  tags, after the selection on  $MM^2$ .

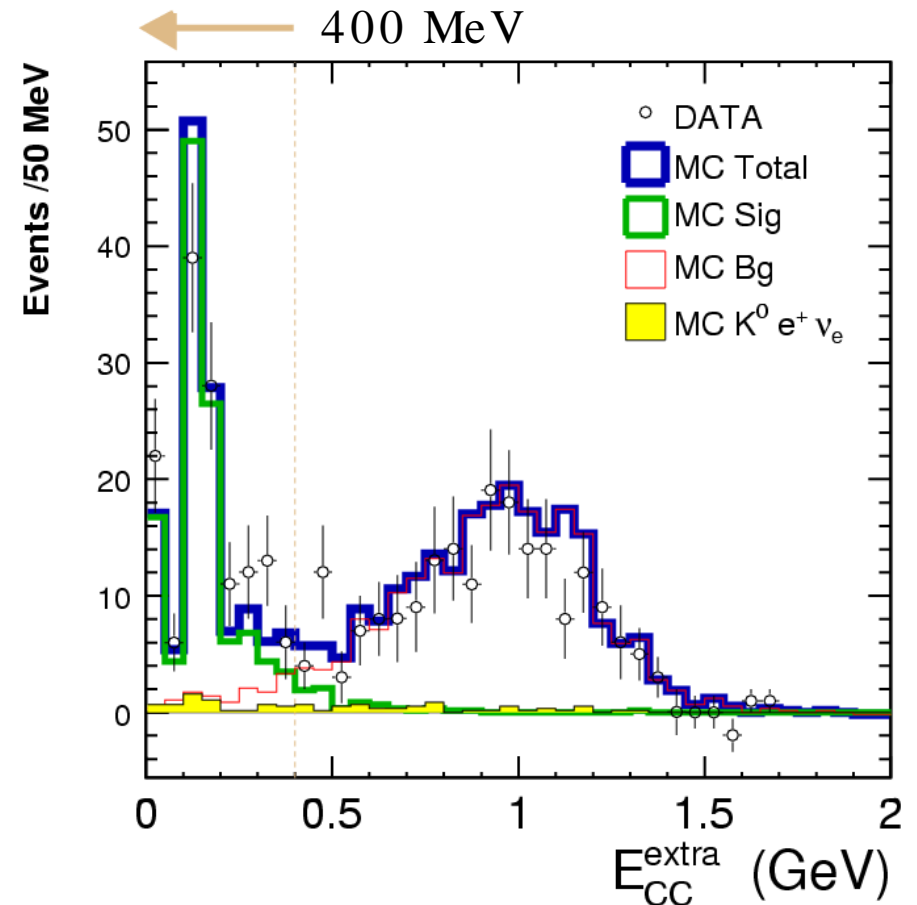


# $D_S \rightarrow \mu \nu_\mu$ and $D_S \rightarrow \tau \nu_\tau$

- $D_S^+ \rightarrow \mu^+ \nu$ 
  - 64 signal events, 2 background, use SM to calculate  $\tau \nu$  yield near 0  $MM^2$  based on known  $\tau \nu / \mu \nu$  ratio
  - $B(D_S^+ \rightarrow \mu^+ \nu) = (0.657 \pm 0.090 \pm 0.028)\%$
- $D_S^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \pi^+ \nu$ 
  - Sum case (i)  $0.2 > MM^2 > 0.05 \text{ GeV}^2$  & case (ii)  $MM^2 < 0.2 \text{ GeV}^2$ . Total of 36 signal and 4.8 bkgrnd
  - $B(D_S^+ \rightarrow \tau^+ \nu) = (7.1 \pm 1.4 \pm 0.03)\%$
- By summing both cases above, find
  - $f_{D_S} = 282 \pm 16 \pm 7 \text{ MeV}$
  - $B^{\text{eff}}(D_S^+ \rightarrow \mu^+ \nu) = (0.664 \pm 0.076 \pm 0.028)\%$
- $B(D_S^+ \rightarrow e^+ \nu) < 3.1 \times 10^{-4}$

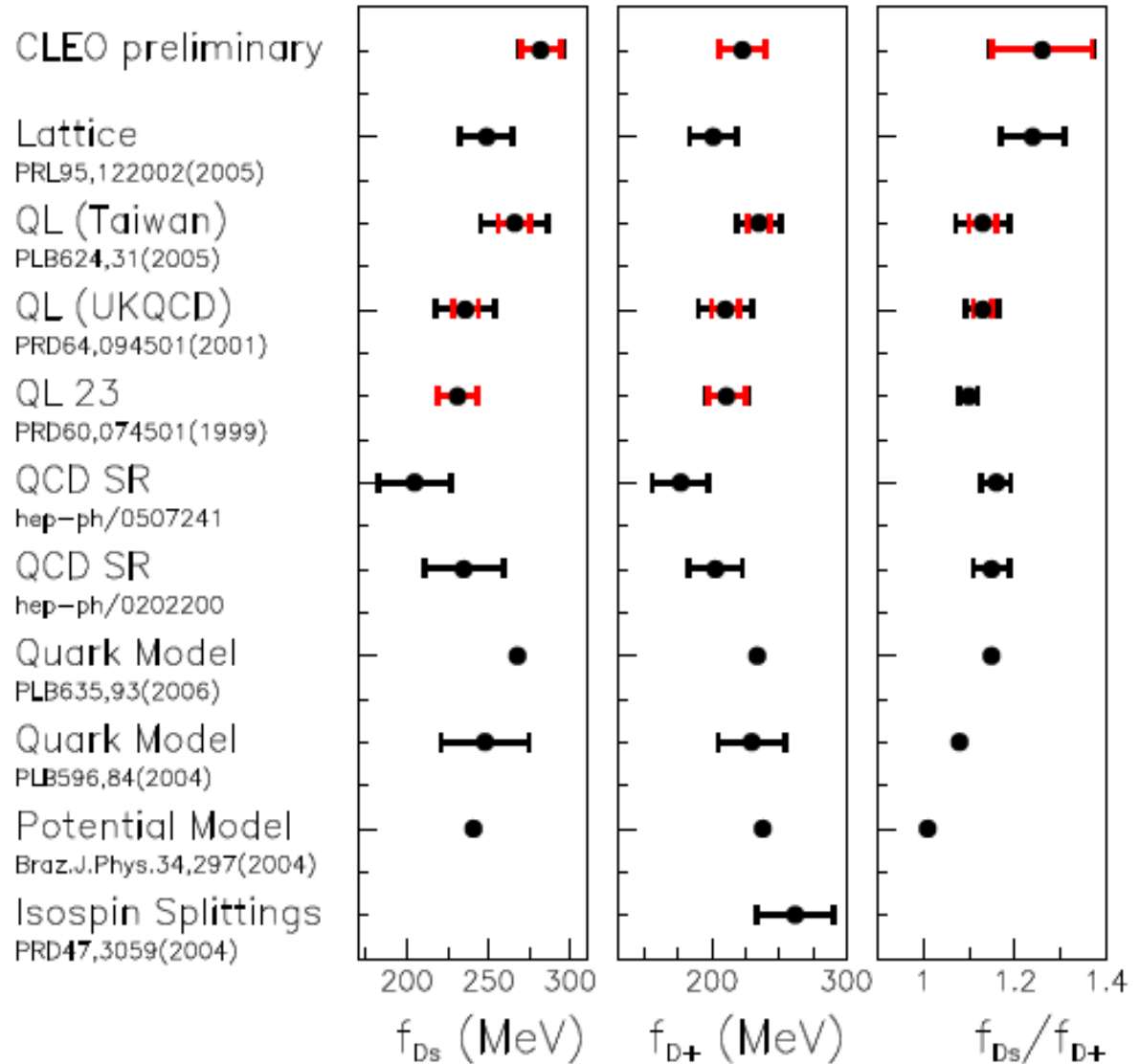
# $D_S \rightarrow \tau \nu_\tau, \tau \rightarrow e \nu \nu$

- An alternative is to look for  $D_S \rightarrow \tau \nu_\tau, \tau \rightarrow e \nu \nu$
- $B(D_S \rightarrow \tau \nu_\tau) \times B(\tau \rightarrow e \nu \nu) \approx 1\%$ 
  - Relatively large compared to  $B(D_S \rightarrow X e \nu) \approx 8\%$
- Reconstruct tag  $D_S$  and  $e$
- Veto extra tracks
- Look for signal with little extra energy in EM-calorimeter
- Do not need to find  $\gamma$
- $B(D_S^+ \rightarrow \tau^+ \nu) = (6.29 \pm 0.78 \pm 0.52)\%$
- $f_{D_S} = 278 \pm 17 \pm 12 \text{ MeV}$



# Comparison to Theory

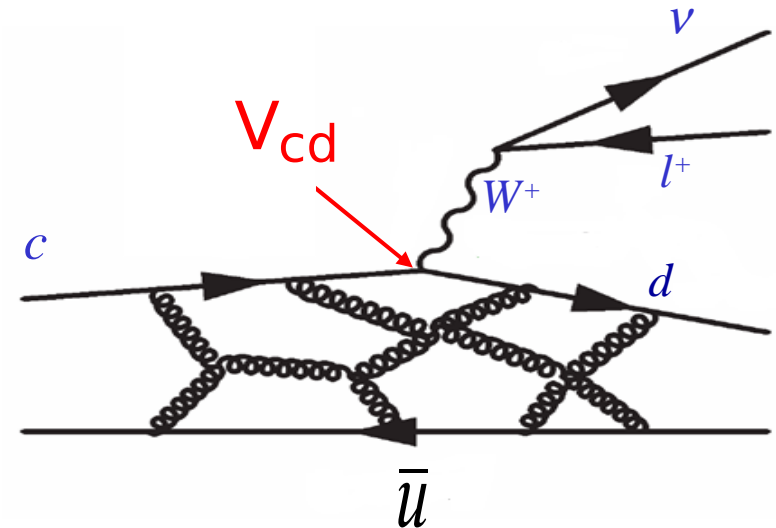
- CLEO results consistent with most (recent) predictions.
- For precision comparisons we need more data.
- Using Lattice results for decay constants we get  $|V_{cd}/V_{cs}| = 0.22 \pm 0.03$ .





# Semileptonic Decays

- Semileptonic decays are easier to describe theoretically than hadronic decays
  - The non-perturbative strong physics is parameterized in form factors.
  - For  $m_l=0$  we have
    - one form factor for  $D \rightarrow (K, \pi) e \nu$
    - three form factors for  $D \rightarrow K^* e \nu$

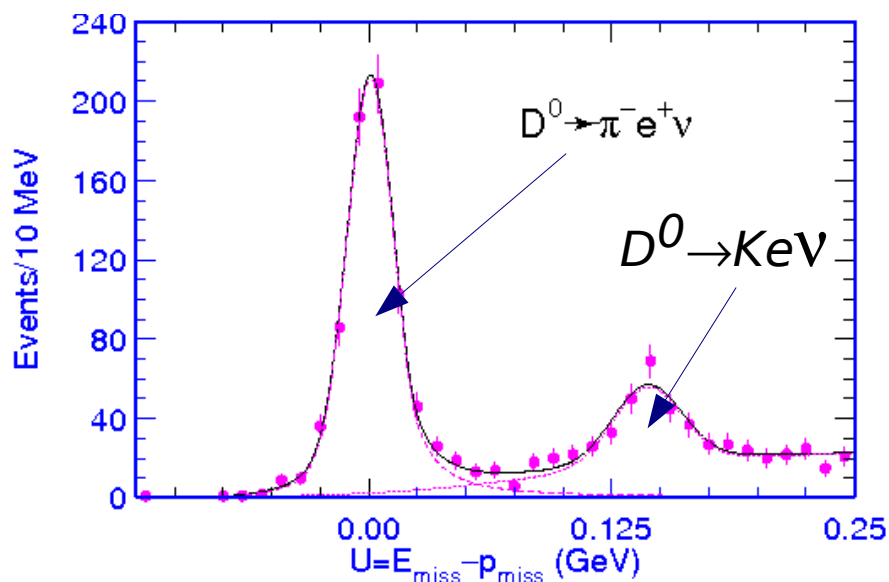


- CLEO-c measures
  - Inclusive and exclusive branching fractions
  - CKM matrix elements ( $V_{cd}$  and  $V_{cs}$ )
  - Form factors
- The clean environment and excellent detector will allow the first precise studies of Cabibbo suppressed semileptonic  $D$  decays
- We only use electrons; muons are too soft to be cleanly identified.

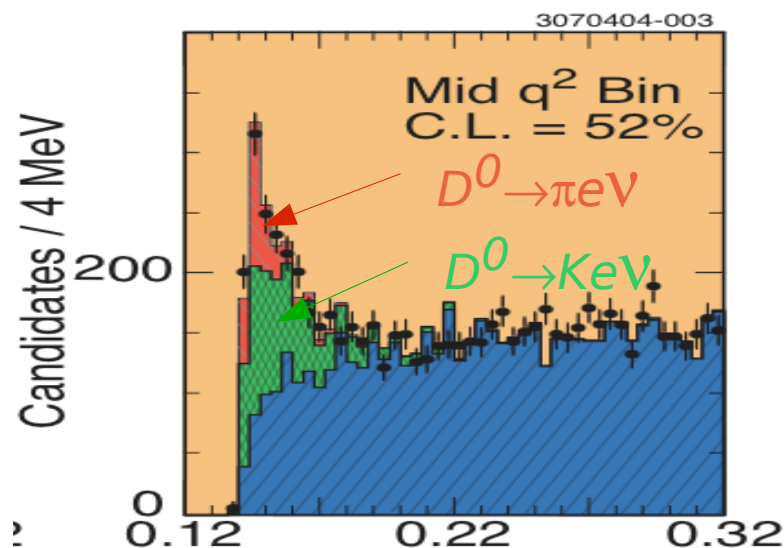
# Exclusive Branching Fractions

- The exclusive decays are studied by finding an electron and reconstructing the hadronic system recoiling against a  $D$ -tag.
- The signal is extracted by studying the variable  $U = E_{\text{miss}} - |\mathbf{P}_{\text{miss}}|$
- For the signal events, with one missing neutrino  $U$  peaks at zero
- $D \rightarrow K e \nu$  and  $D \rightarrow \pi e \nu$  are kinematically separated

CLEO-c 281 pb<sup>-1</sup> (Preliminary)

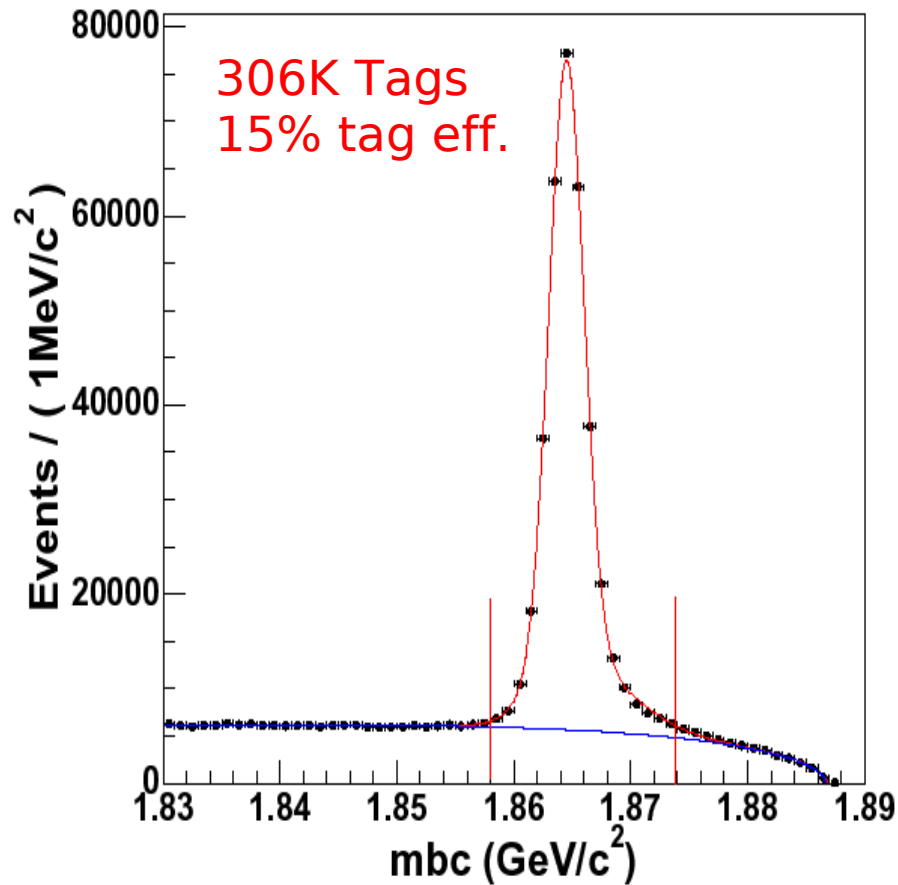


CLEO-III 7 fb<sup>-1</sup> (PRL 94:011802, 2005)

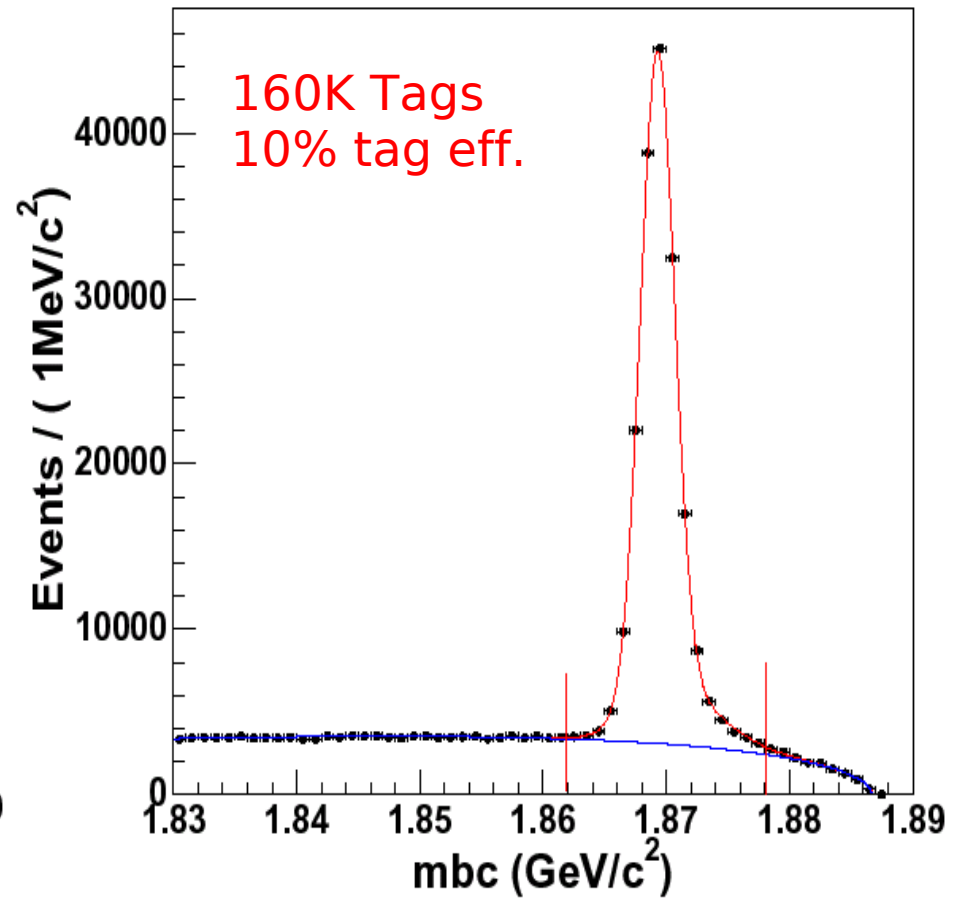


# Semileptonic with Tag

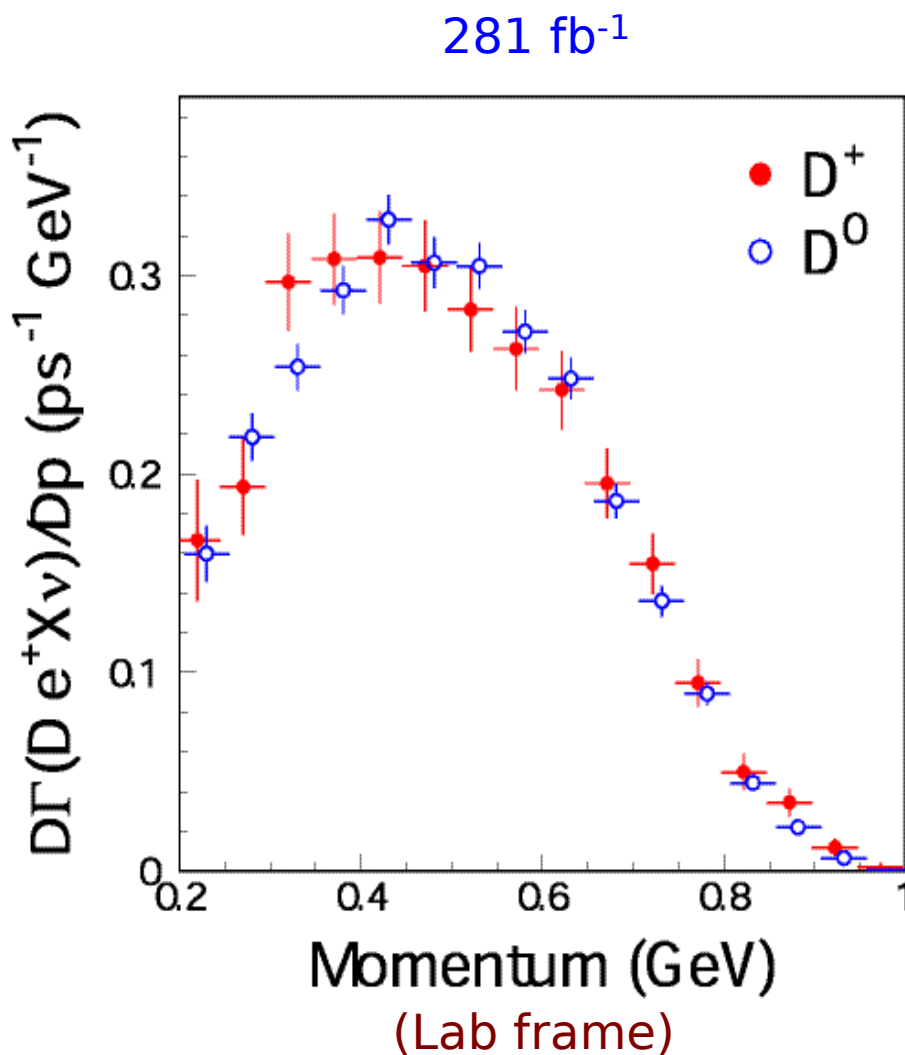
$D^0$  Tags



$D^+$  Tags



# Inclusive Semileptonic *D* decays



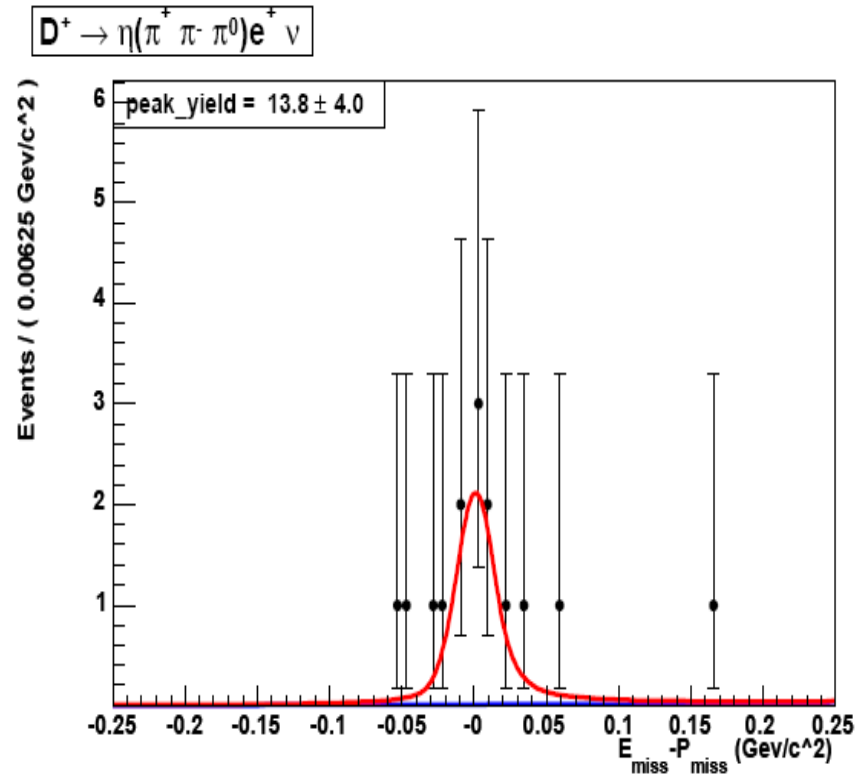
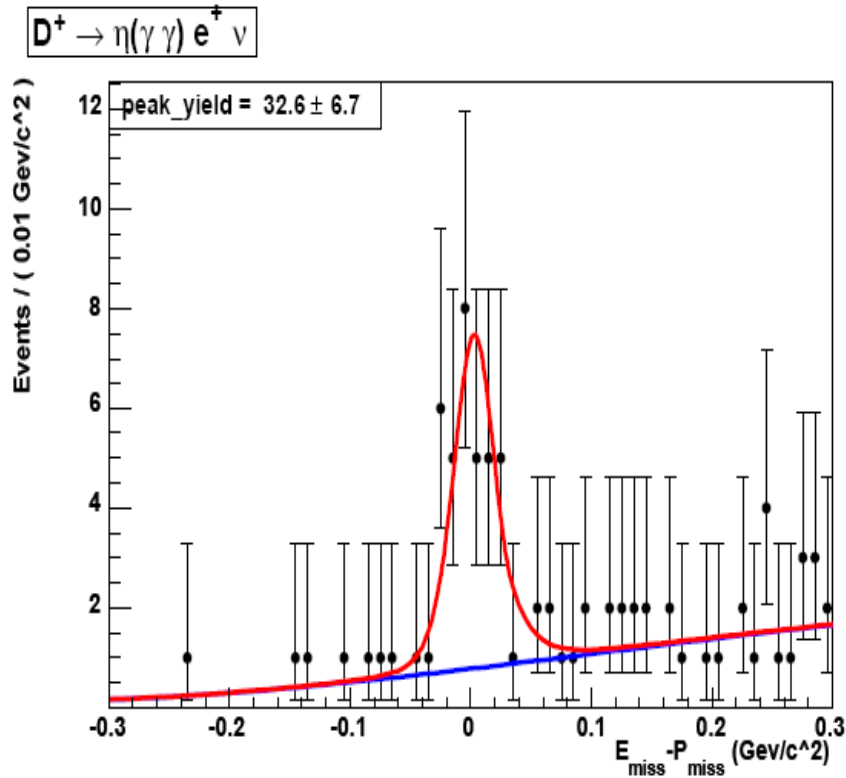
- This analysis uses only the cleanest tags:  $D^0 \rightarrow K^- \pi^+$  and  $D^+ \rightarrow K^- \pi^+ \pi^+$
- Correct for  $e$  momentum cut
- Obtain the branching fractions
 
$$Br(D^0 \rightarrow X e \nu_e) = (6.46 \pm 0.17 \pm 0.13) \%$$

$$Br(D^+ \rightarrow X e \nu_e) = (16.13 \pm 0.20 \pm 0.33) \%$$
- Using the measured lifetimes we obtain
 
$$\frac{\Gamma(D^+ \rightarrow X e \nu_e)}{\Gamma(D^0 \rightarrow X e \nu_e)} = (0.985 \pm 0.028 \pm 0.015)$$
- The sum of exclusive final state

$$\sum_i Br(D^0 \rightarrow X_i e \nu_e) = (6.1 \pm 0.2 \pm 0.2) \%$$

$$\sum_i Br(D^+ \rightarrow X_i e \nu_e) = (15.1 \pm 0.5 \pm 0.5) \%$$

# First observation of $D^+ \rightarrow \eta e^+ \nu$



CLEO- c preliminary

$$B(D^+ \rightarrow \eta e^+ \nu) = (1.29 \pm 0.19 \pm 0.07) \times 10^{-3}$$

$$B(D^+ \rightarrow \eta' e^+ \nu)_{\text{combined}} < 3 \times 10^{-4} \text{ (90\% C.L.)}$$

$$B(D^+ \rightarrow \phi e^+ \nu) < 2 \times 10^{-4} \text{ (90\% C.L.)}$$

PDG- 2004

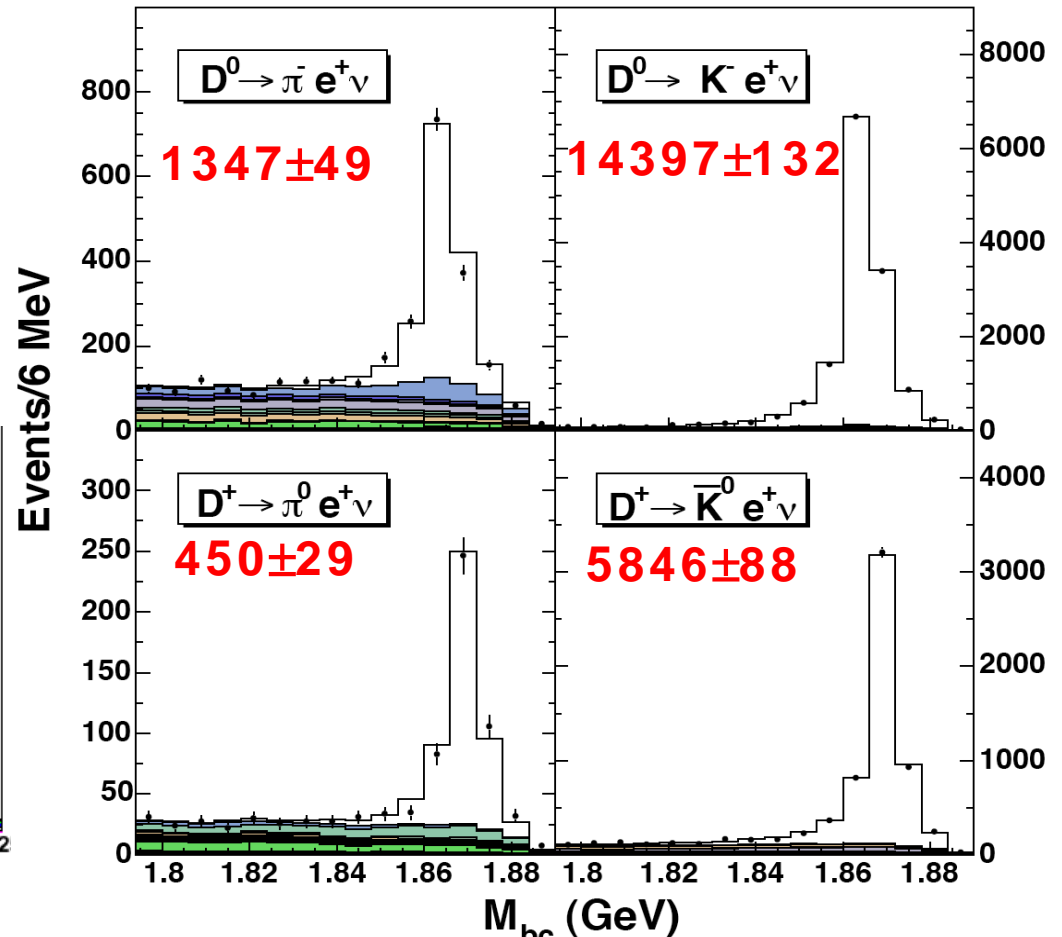
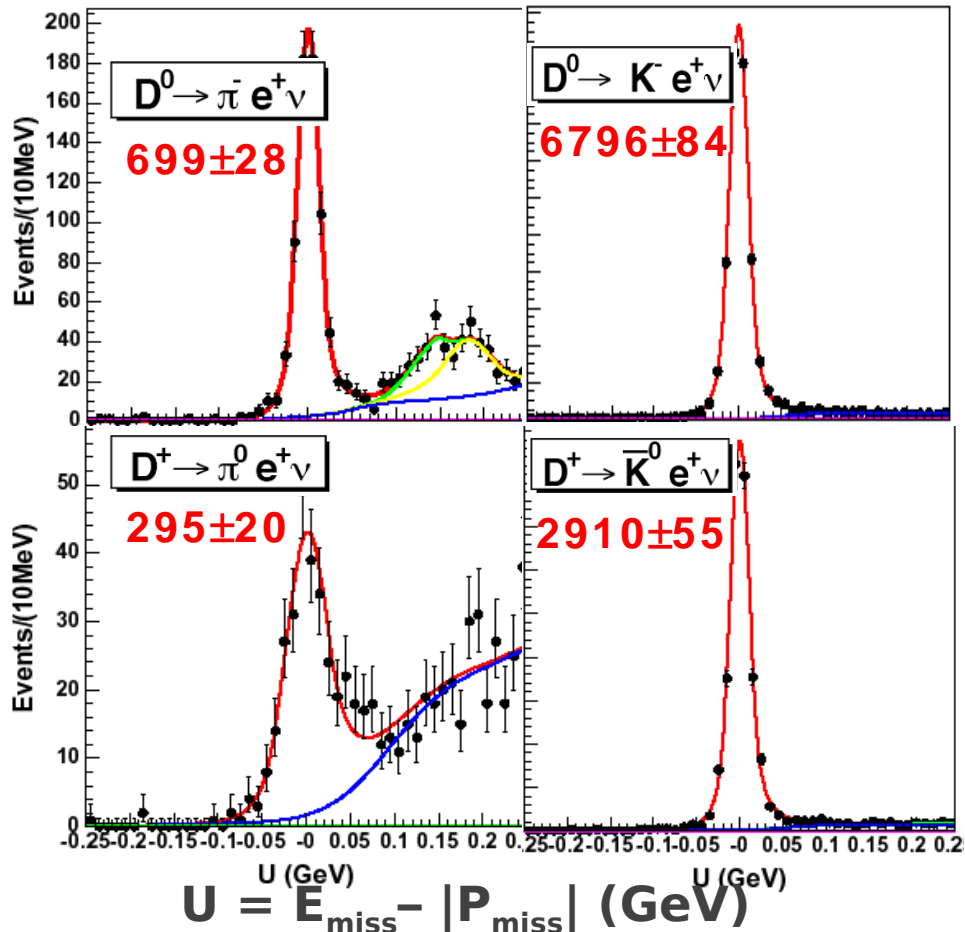
$$B(D^+ \rightarrow \eta l^+ \nu) < 5 \times 10^{-3} \text{ (90\% C.L.)}$$

$$B(D^+ \rightarrow \eta' \mu^+ \nu) < 1.1\% \text{ (90\% C.L.)}$$

$$B(D^+ \rightarrow \phi e^+ \nu) < 2.09\% \text{ (90\% C.L.)}$$

# Exclusive Signals (281 pb<sup>-1</sup>)

Tag Preliminary Untag



$$\Delta E = E_{K(\pi)} + E_e + |\mathbf{p}_{\text{miss}}| - E_{\text{beam}}$$

$$M_{bc} = \sqrt{E_{\text{beam}}^2 - (\mathbf{p}_{K(\pi)} + \mathbf{p}_e + \zeta \mathbf{p}_{\text{miss}})^2}$$

Tag and Untag analysis have 40% overlap and should not be averaged

# Branching Fraction Results

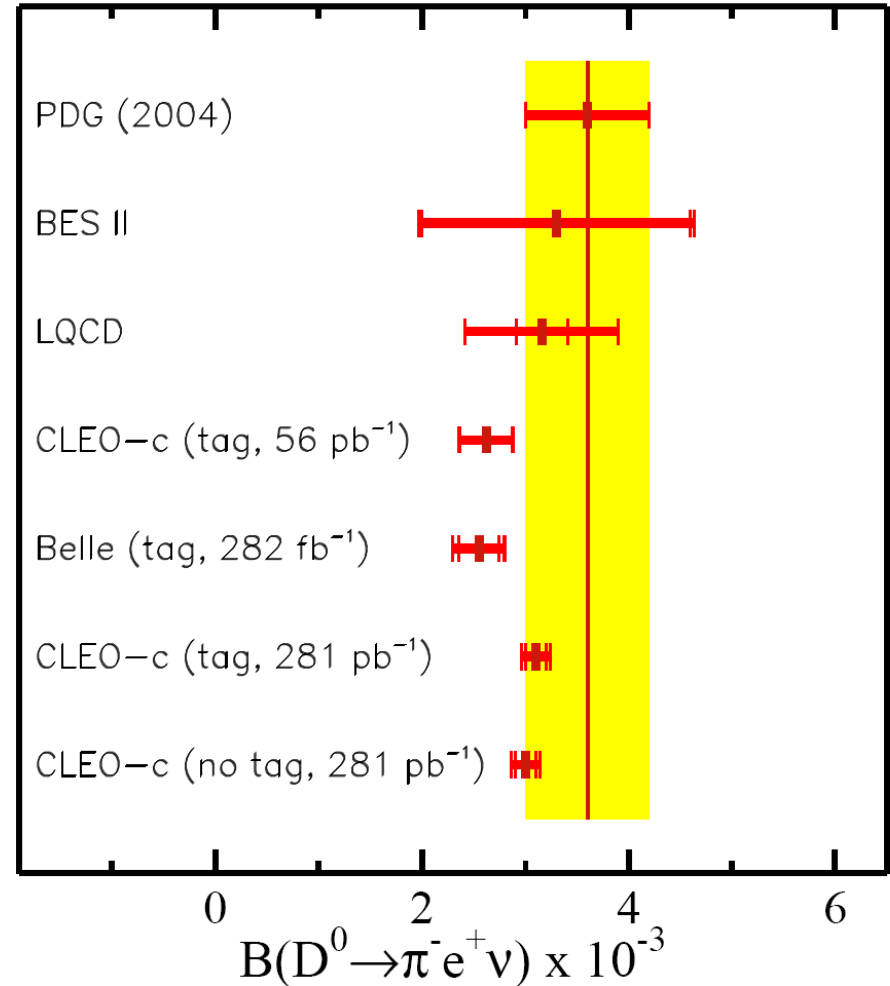
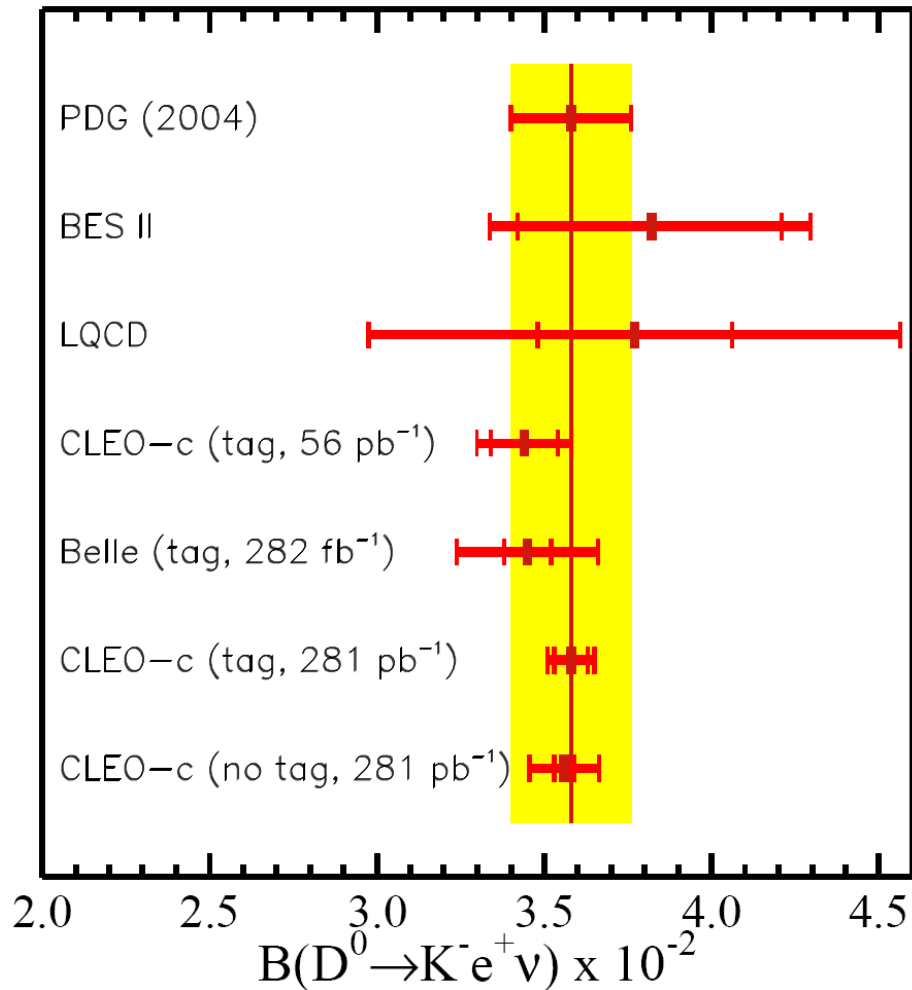
<i>D</i> Decay	Tag	Br. Frac. (%)	Untag	PDG (%)
$D^0 \rightarrow K^- e^+ \nu$	$3.58 \pm 0.05 \pm 0.05$	$3.56 \pm 0.03 \pm 0.11$	$3.62 \pm 0.16$	$3.62 \pm 0.16$
$D^0 \rightarrow \pi^- e^+ \nu$	$0.309 \pm 0.012 \pm 0.006$	$0.301 \pm 0.011 \pm 0.010$	$0.311 \pm 0.030$	$0.311 \pm 0.030$
$D^+ \rightarrow \bar{K}^0 e^+ \nu$	$8.86 \pm 0.17 \pm 0.20$	$8.75 \pm 0.13 \pm 0.30$	$7.2 \pm 0.8$	$7.2 \pm 0.8$
$D^+ \rightarrow \pi^0 e^+ \nu$	$0.397 \pm 0.027 \pm 0.028$	$0.383 \pm 0.025 \pm 0.016$	$0.38 \pm 0.19$	$0.38 \pm 0.19$

Ratio	Measured (%)	PDG (%)	Ratio	Measured
$\frac{D^0 \rightarrow \pi^- e^+ \nu}{D^0 \rightarrow K^- e^+ \nu}$	$8.5 \pm 0.3 \pm 0.1$	$8.6 \pm 0.7$	$\frac{\Gamma(D^0 \rightarrow \pi^- e^+ \nu)}{\Gamma(D^+ \rightarrow \pi^0 e^+ \nu)}$	$1.95 \pm 0.15 \pm 0.14$ $1.99 \pm 0.15 \pm 0.10$
$\frac{D^+ \rightarrow \pi^0 e^+ \nu}{D^+ \rightarrow \bar{K}^0 e^+ \nu}$	$4.4 \pm 0.3 \pm 0.1$	$4.6 \pm 1.4 \pm 1.7$	$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu)}$	$1.02 \pm 0.02 \pm 0.02$ $1.03 \pm 0.02 \pm 0.04$



# Comparison to Other Exp.

**CLEO-c 281 pb<sup>-1</sup> Preliminary**



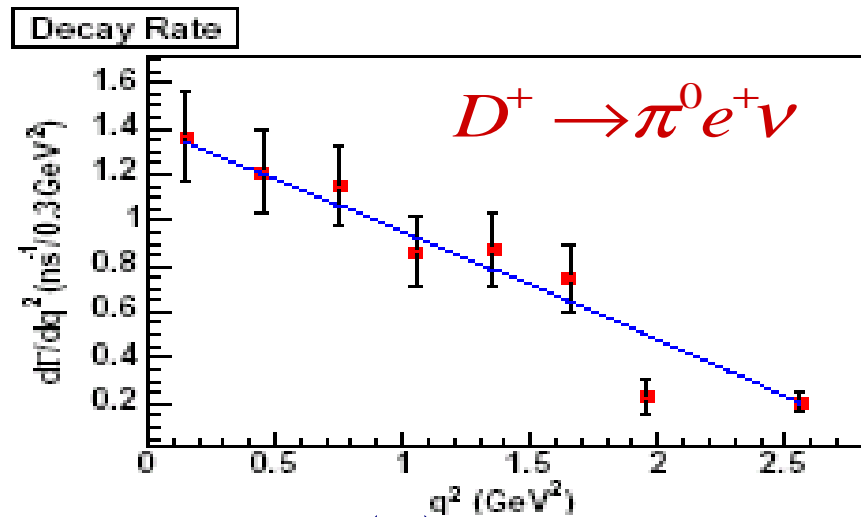
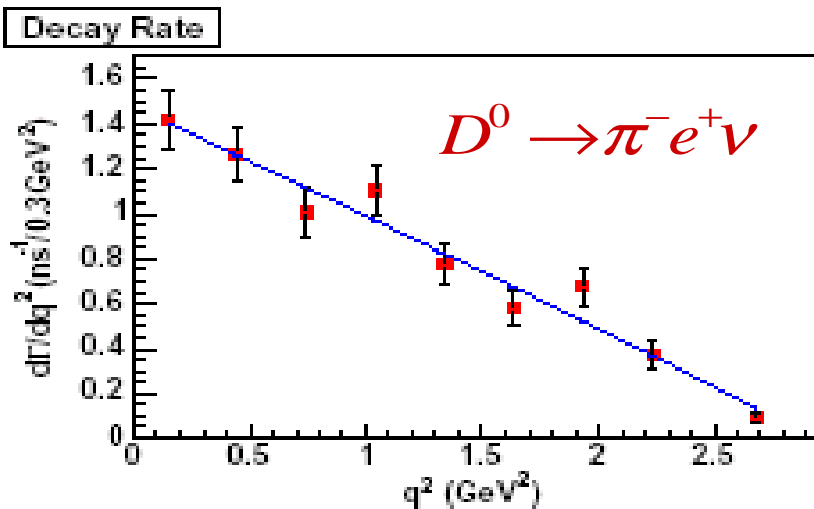
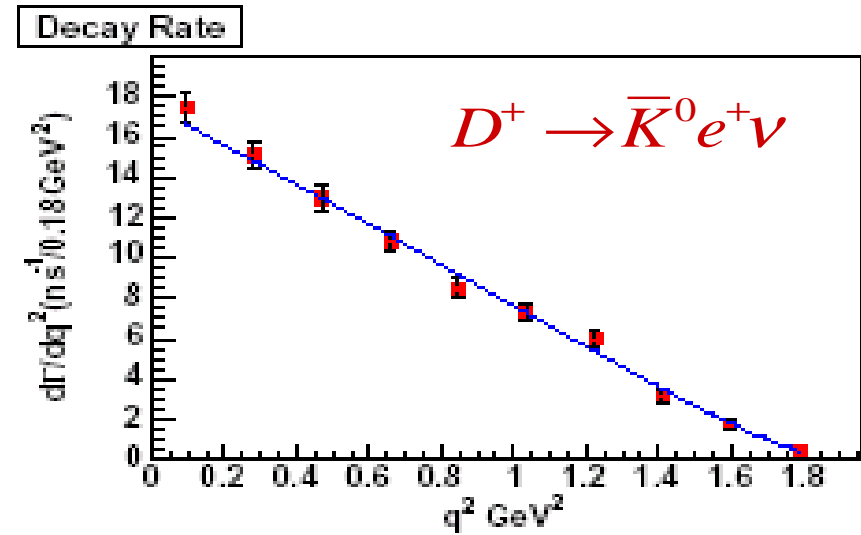
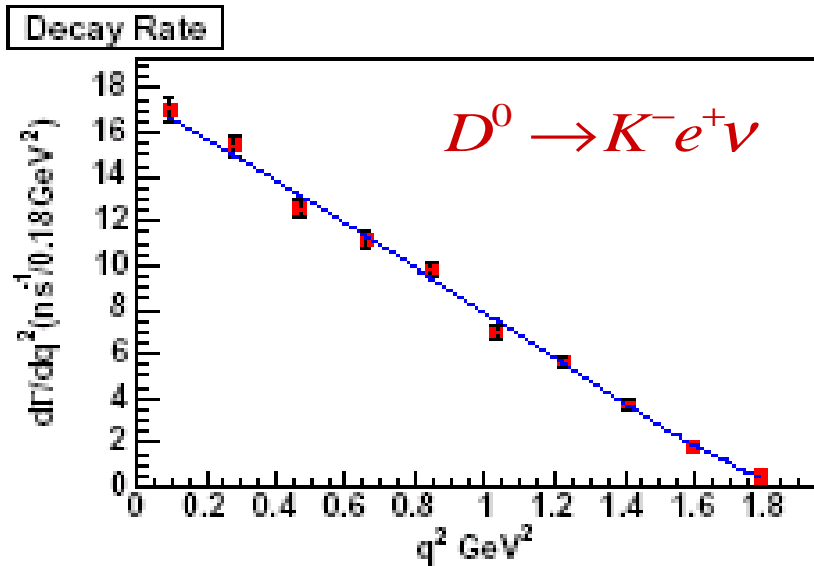
# Form Factors in $D \rightarrow K e \nu$ and $D \rightarrow \pi e \nu$

- The differential decay rate is given by

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cq}|^2 p_K^3 |f_+(q^2)|^2$$

- $q^2 = m_{e\nu}^2$
- As we use electrons the form factor corresponding to a scalar  $W$  has a negligible contribution to the rate.
- The observed  $q^2$  distribution is fit to extract form factor information.

# Form Factor Fit (Tag)



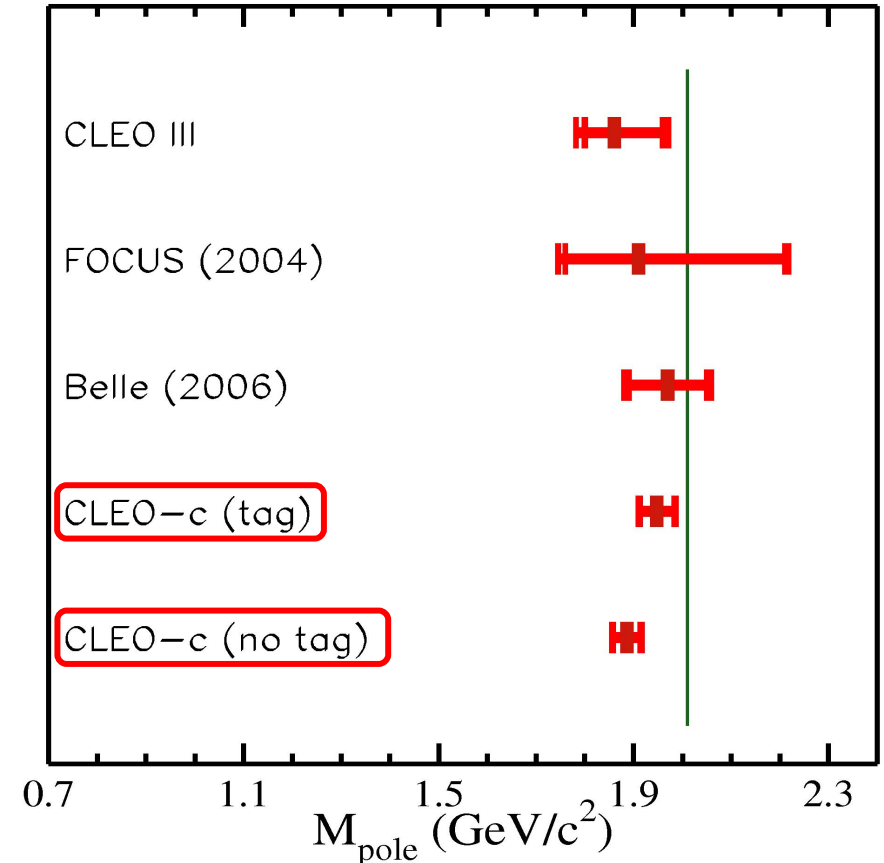
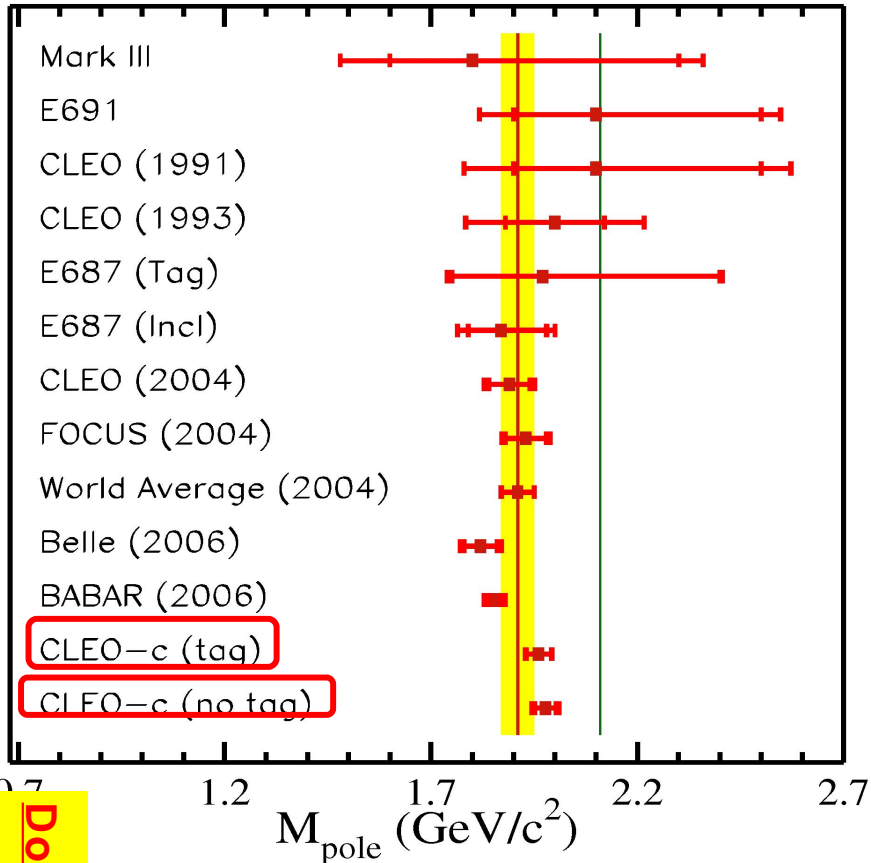
$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{\text{pole}}^2}$$

$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{D(s)^*}^2} \times \frac{1}{1 - \alpha q^2/M_{D(s)^*}^2}$$

# Pole Mass

$D \rightarrow Ke^+ \nu$

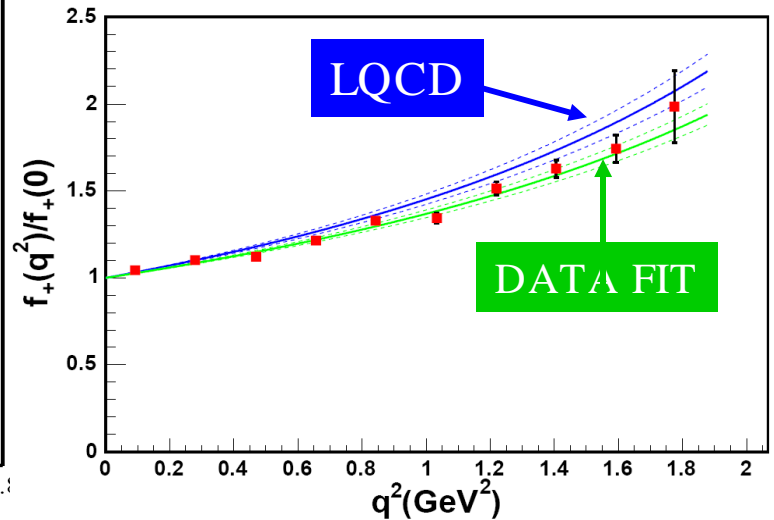
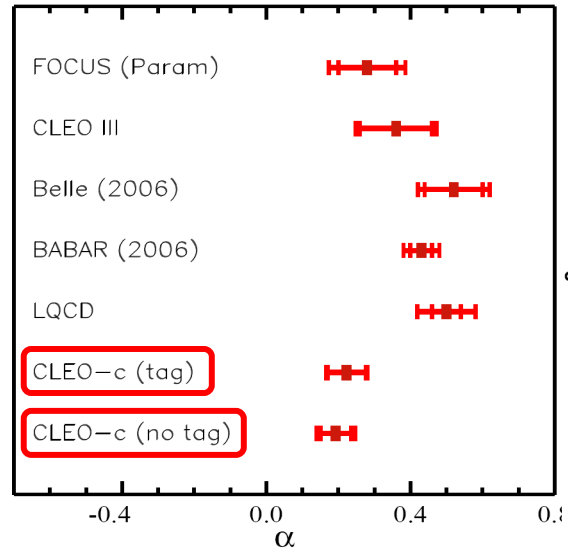
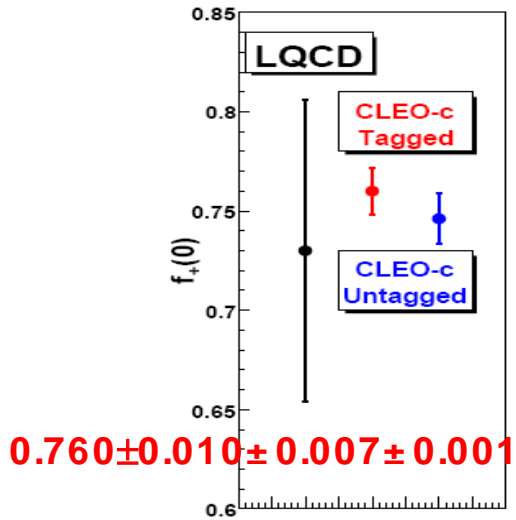
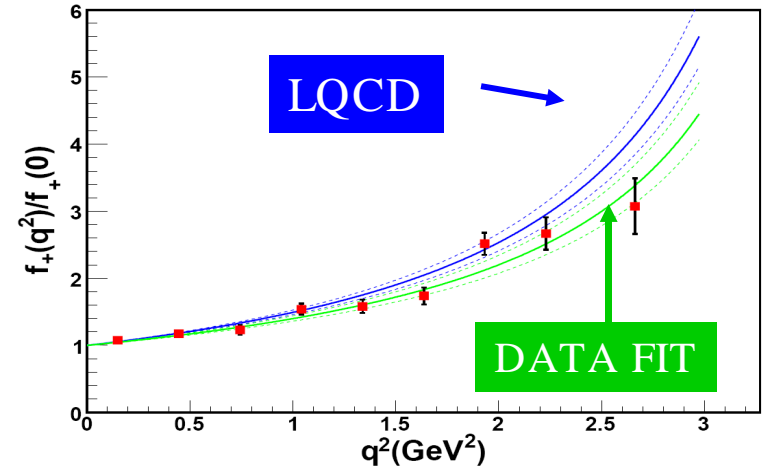
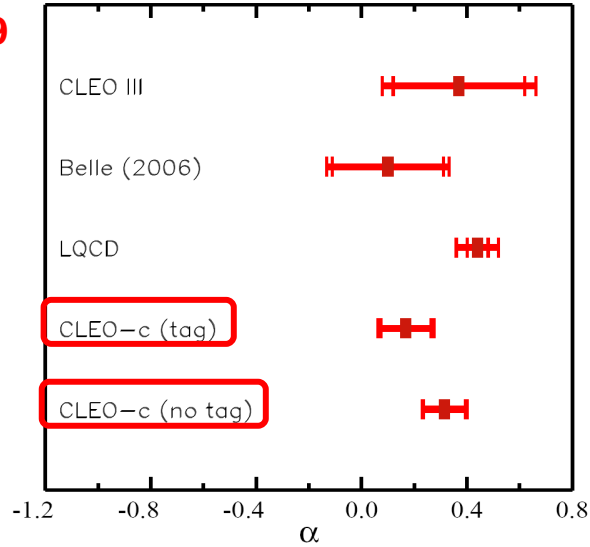
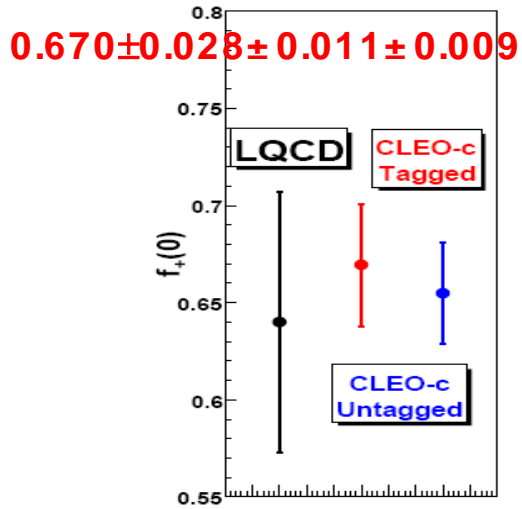
$D \rightarrow \pi e^+ \nu$



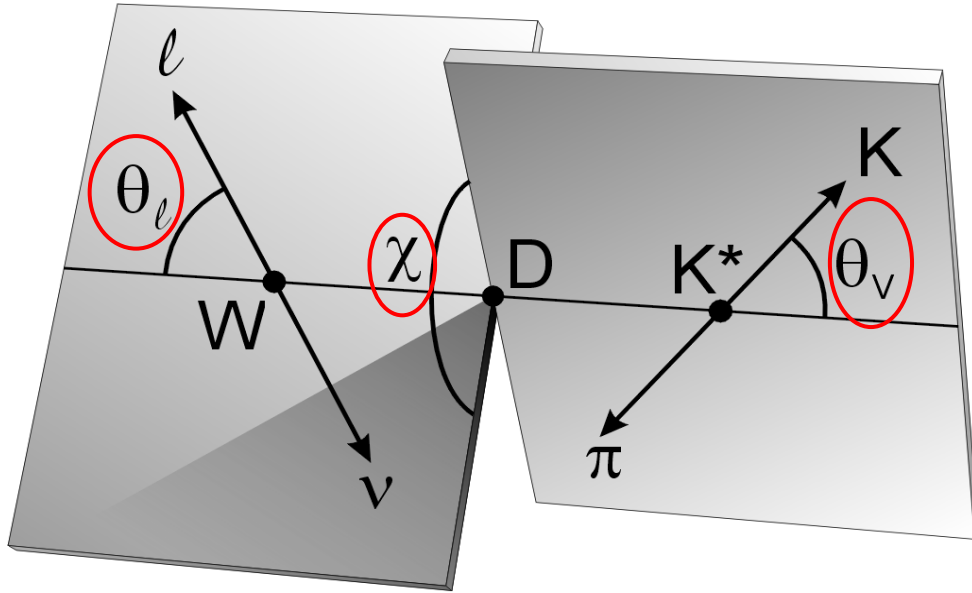
Don't average!

Decay Mode	$M_{\text{pole}}$ (Tag)	$M_{\text{pole}}$ (Untag)
$D \rightarrow Ke^+ \nu$ (av. $D^0$ & $D^+$ )	$1.96 \pm 0.03 \pm 0.01$	$1.98 \pm 0.03 \pm 0.02$
$D \rightarrow \pi e^+ \nu$ (av. $D^0$ & $D^+$ )	$1.95 \pm 0.04 \pm 0.02$	$1.88 \pm 0.03 \pm 0.02$

# Form Factors and LQCD



# $D \rightarrow "K^*" e \nu$ Form Factors



- Focus has seen evidence for a S-wave component of the  $K\pi$ .
- Fit the  $\theta_l$  and  $\theta_v$  distributions as a function of  $q^2$  to extract the helicity amplitudes.

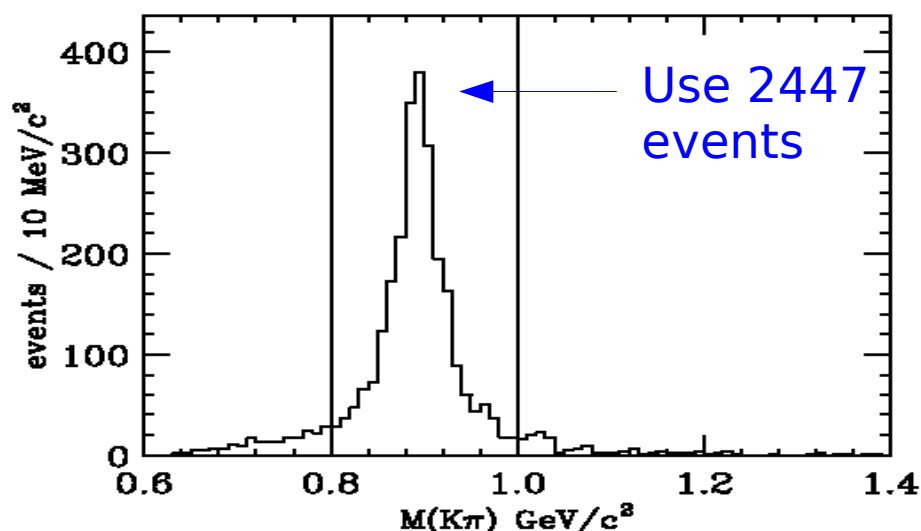
$$|A|^2 = \frac{q^2}{8} \left| \begin{array}{l} (1 + \cos \theta_l) \sin \theta_v e^{i\chi} \text{ BW } H_+(q^2) \\ -(1 - \cos \theta_l) \sin \theta_v e^{-i\chi} \text{ BW } H_-(q^2) \\ -2 \sin \theta_l \left( \cos \theta_v \text{ BW } H_0(q^2) + A e^{i\delta} h_0(q^2) \right) \end{array} \right|^2$$

Focus found A 7% of BW peak if they assumed

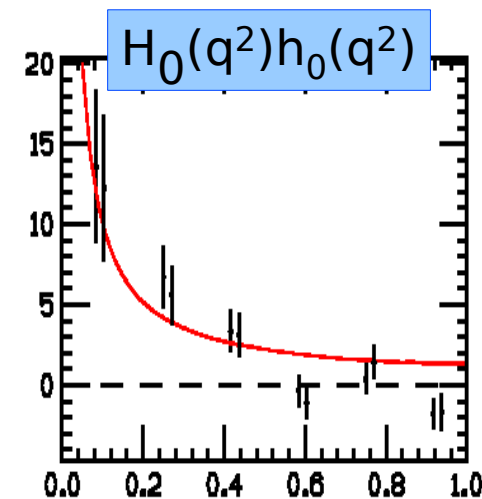
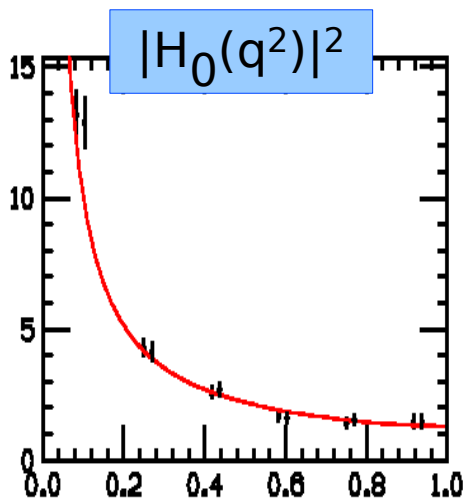
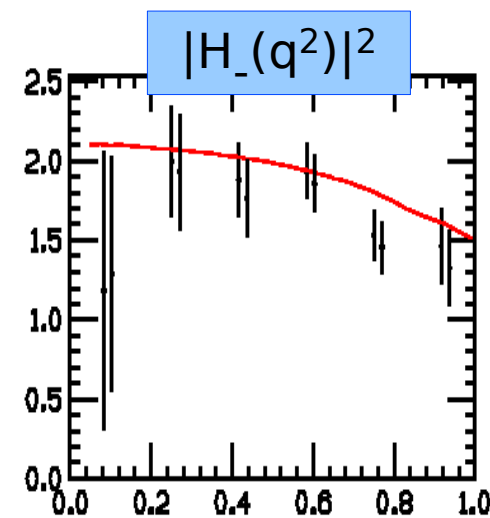
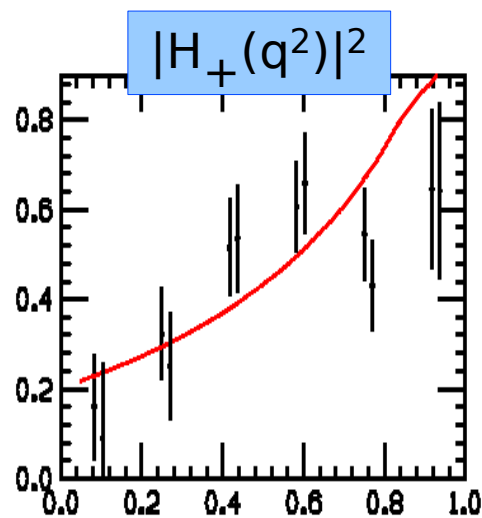
$$h_0(q^2) = H_0(q^2)$$

# $D \rightarrow K^* e \nu$ Form Factor Results

Preliminary



- Non-parametric fit
- Clear evidence for S-wave





# Summary-Outlook

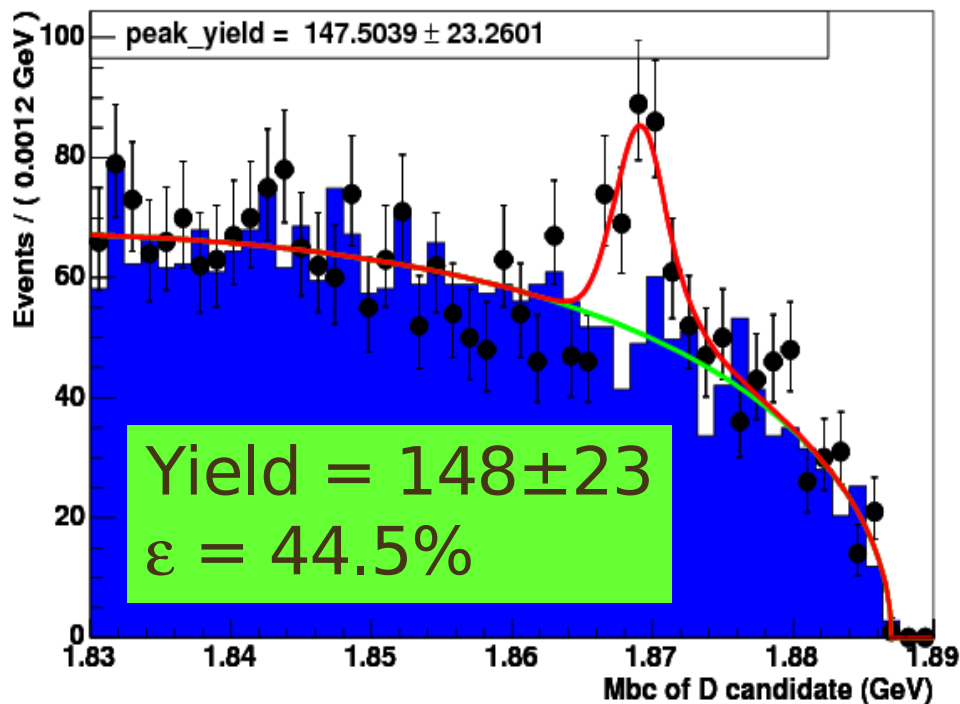
- CLEO-c has recorded 281 pb<sup>-1</sup> at  $\psi(3770)$ 
  - Absolute hadronic branching fractions
  - Leptonic decays
  - Semileptonic decays
- Recorded  $\sim 330$  pb<sup>-1</sup> at  $E_{\text{cm}} \approx 4170$  MeV
  - Analyzed  $\sim 200$  pb<sup>-1</sup> for hadronic and leptonic  $D_s$  decays
- Goal is to take  $\sim 750$  pb<sup>-1</sup> at  $E_{\text{cm}} \approx 4170$  MeV and at  $\psi(3770)$  before the CLEO-c run ends in April 2008.
  - Leptonic decays can make full use of statistics
  - Cabibbo favored hadronic and semileptonic decays are starting to become systematics limited at the  $\psi(3770)$
  - $D_s$  decays will remain statistics limited

# $D^+ \rightarrow K^+ \pi^0$

- Reconstruct  $K^+$  using RICH (some  $dE/dx$ ),  $\pi^0 \rightarrow \gamma\gamma$ .
- Require  $-40 < E_{\text{cand}} - E_{\text{beam}} < 35$  MeV
  - Fit  $M_{\text{bc}}$  spectrum
- Normalize to  $D^+ \rightarrow K^- \pi^+ \pi^+$

$$B(D^+ \rightarrow K^+ \pi^0) = (2.25 \pm 0.36 \pm 0.15 \pm 0.07) \times 10^{-4}$$

$M_{\text{bc}}$  Distribution

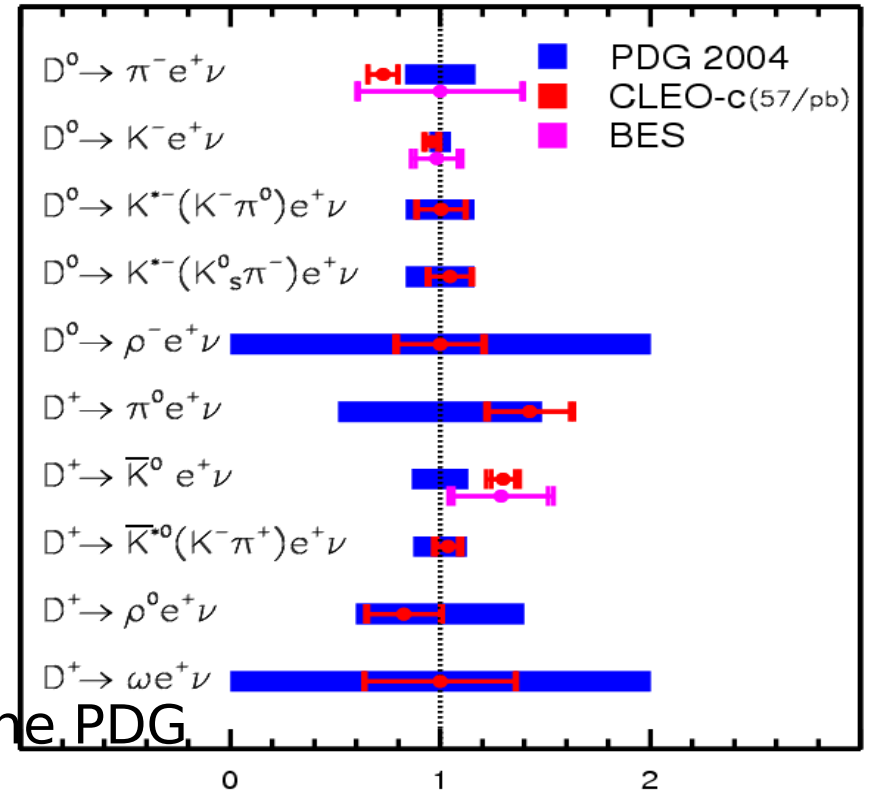


BaBar ( $124 \text{ fb}^{-1}$ ) finds:

$$B(D^+ \rightarrow K^+ \pi^0) = (2.25 \pm 0.46 \pm 0.24 \pm 0.16) \times 10^{-4}$$

# Summary of Exclusive Semileptonic Decays in 56 pb<sup>-1</sup>

Mode	$\mathcal{B}$ (%)	$\mathcal{B}$ (%) (PDG)
$D^0 \rightarrow \pi^- e^+ \nu_e$	$0.26 \pm 0.03 \pm 0.01$	$0.36 \pm 0.06$
$D^0 \rightarrow K^- e^+ \nu_e$	$3.44 \pm 0.10 \pm 0.10$	$3.58 \pm 0.18$
$D^0 \rightarrow K^{*-} (K^- \pi^0) e^+ \nu_e$	$2.11 \pm 0.23 \pm 0.10$	$2.15 \pm 0.35$
$D^0 \rightarrow K^{*-} (\bar{K}^0 \pi^-) e^+ \nu_e$	$2.19 \pm 0.20 \pm 0.11$	$2.15 \pm 0.35$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$0.19 \pm 0.04 \pm 0.01$	—
$D^+ \rightarrow \pi^0 e^+ \nu_e$	$0.44 \pm 0.06 \pm 0.03$	$0.31 \pm 0.15$
$D^+ \rightarrow \bar{K}^0 e^+ \nu_e$	$8.71 \pm 0.38 \pm 0.37$	$6.7 \pm 0.9$
$D^+ \rightarrow \bar{K}^{*0} e^+ \nu_e$	$5.56 \pm 0.27 \pm 0.23$	$5.5 \pm 0.7$
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$0.21 \pm 0.04 \pm 0.01$	$0.25 \pm 0.10$
$D^+ \rightarrow \omega e^+ \nu_e$	$0.16^{+0.07}_{-0.06} \pm 0.01$	—

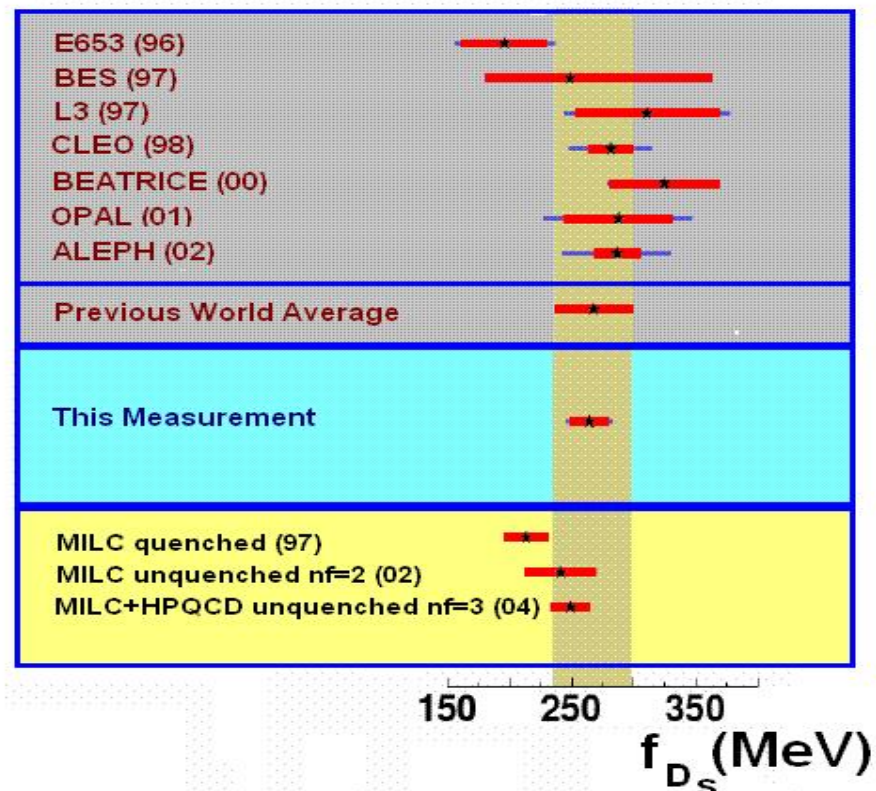
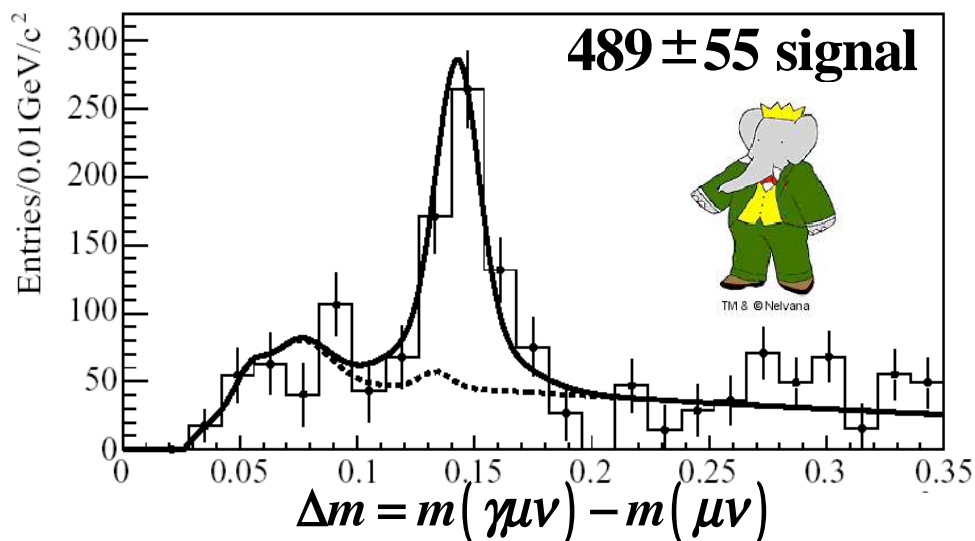


- Most modes are improvements over the PDG
  - Including two first observations
  - $D^0 \rightarrow \rho^- e^+ \nu_e$  and  $D^+ \rightarrow \omega e^+ \nu_e$
- Most systematics can be reduced with more data
- Updating analysis to 281 pb<sup>-1</sup>

# $D_S \rightarrow \mu \nu_\mu$

- Current best measurement from BaBar (230 fb<sup>-1</sup>)
- Use  $D^0, D^+, D_S$  tags to get clean  $e^+e^- \rightarrow cc$  sample
- Have  $489 \pm 55$   $D_S \rightarrow \mu \nu_\mu$  candidates

From P. Patteri (Babar)



$$f_{D_S}^{BaBar} / f_{D^+}^{CLEO} = 1.25 \pm 0.14$$

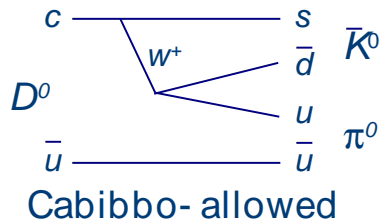
(As expected from LQCD)



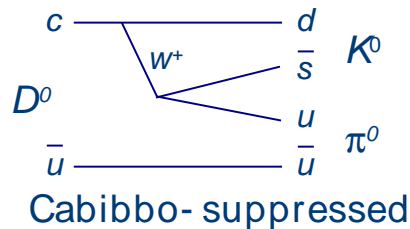
$$\Delta m = m(\gamma \mu \nu) - m(\mu \nu)$$

# $D^0 \rightarrow K_S \pi^0$ and $D^0 \rightarrow K_L \pi^0$

- It is often assumed that  $\Gamma(D \rightarrow K_S X) = \Gamma(D \rightarrow K_L X)$ , but this is not strictly true due to interference effects.



$$\bar{K}^0 = \frac{1}{\sqrt{2}} (K_S^0 - K_L^0)$$



$$K^0 = \frac{1}{\sqrt{2}} (K_S^0 + K_L^0)$$

The physical states of the  $K_S$  and  $K_L$  have different rates due to interference

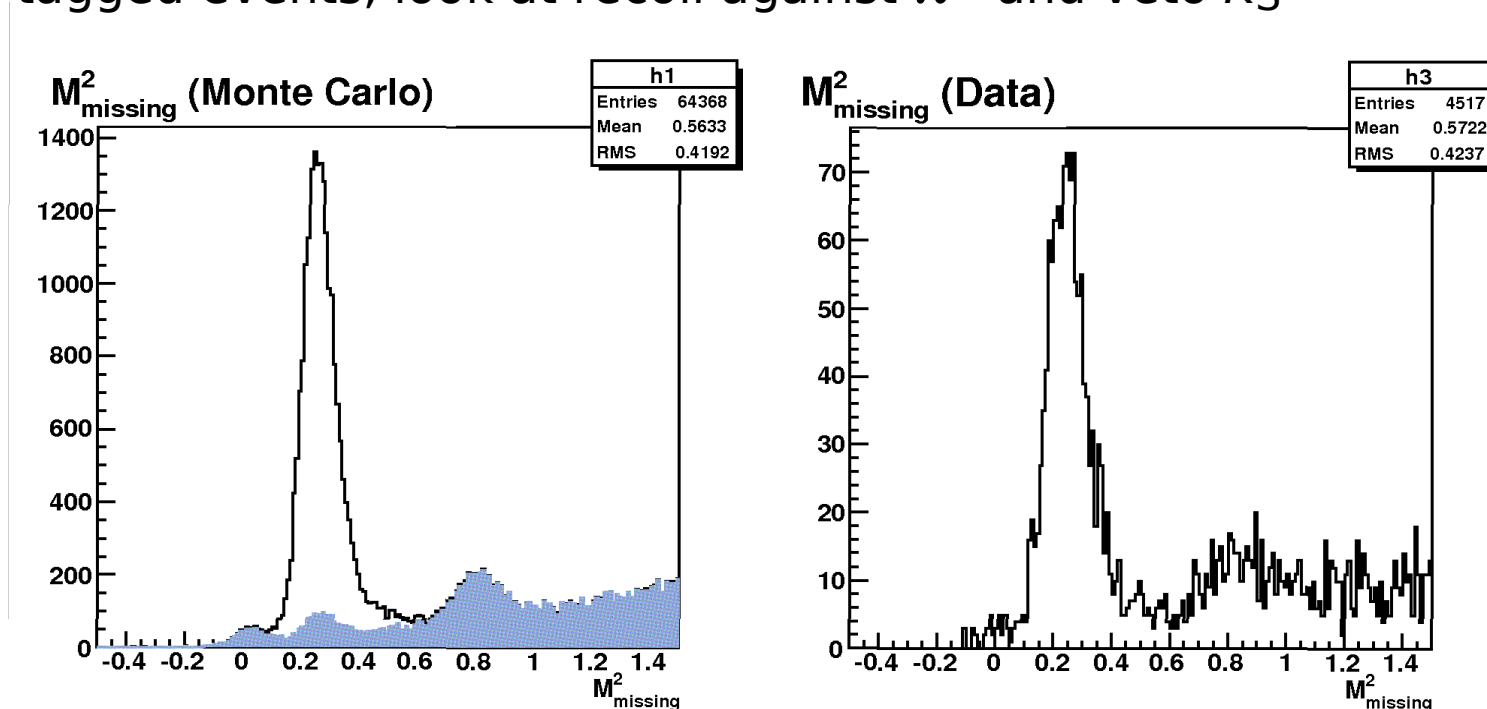
Based on factorization Bigi and Yamamoto (PLB 349, 363 (1995))

Predict

$$\frac{\Gamma(D^0 \rightarrow K_S) - \Gamma(D^0 \rightarrow K_L)}{\Gamma(D^0 \rightarrow K_S) + \Gamma(D^0 \rightarrow K_L)} \approx 0.1$$

# Measuring $D^0 \rightarrow K_L \pi^0$ Preliminary

- CLEO-c is uniquely positioned to measure  $D^0 \rightarrow K_L \pi^0$
- In tagged events, look at recoil against  $\pi^0$  and veto  $K_S$



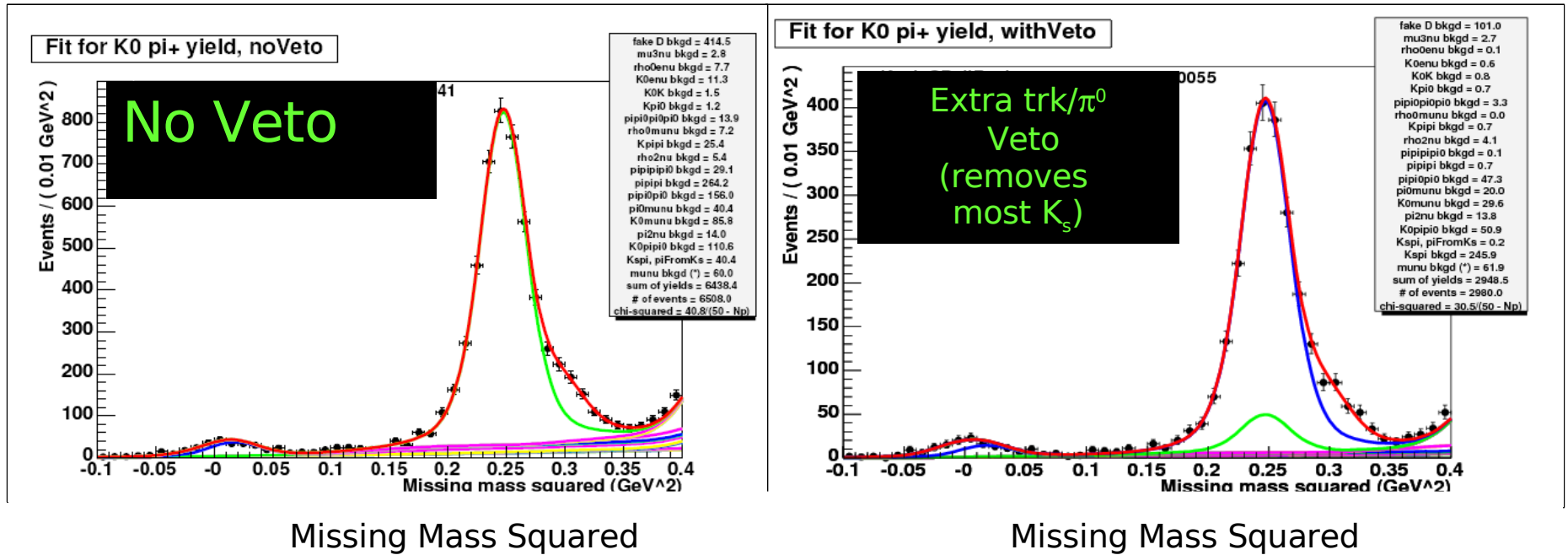
- Correcting for Quantum Correlations
- $B(D^0 \rightarrow K_L^0 \pi^0) = (0.940 \pm 0.046 \pm 0.032)\%$
- $B(D^0 \rightarrow K_S^0 \pi^0) = (1.212 \pm 0.016 \pm 0.039)\%$

$$\frac{\Gamma(D^0 \rightarrow K_S) - \Gamma(D^0 \rightarrow K_L)}{\Gamma(D^0 \rightarrow K_S) + \Gamma(D^0 \rightarrow K_L)} = 0.122 \pm 0.024 \pm 0.030$$

In agreement with theory (factorization)

# $D^+ \rightarrow K_L \pi^+$ vs. $D^+ \rightarrow K_S \pi^+$

- Look for recoil mass against pion in tagged events



	Yield	Efficiency	BF (%)
$K_{S,L}\pi^+$	$4428 \pm 79$	$85.2 \pm 0.1$	$3.095 \pm 0.056$
$K_L\pi^+$	$2023 \pm 54$	$81.8 \pm 0.1$	$1.456 \pm 0.040$

$$\frac{\Gamma(D^+ \rightarrow K_S) - \Gamma(D^+ \rightarrow K_L)}{\Gamma(D^+ \rightarrow K_S) + \Gamma(D^+ \rightarrow K_L)} = 0.030 \pm 0.023 \pm 0.025$$